

# Parametric Face Alignment: Generative and Discriminative Approaches

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PhD Thesis  
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# Acknowledgements

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- **Advisor:** Dr. Jorge Batista

- Institute of Systems and Robotics (ISR) - University of Coimbra  
<http://www.isr.uc.pt/>



- Department of Electrical and Computer Engineering (DEEC) from Faculty of Sciences and Technology of the University of Coimbra (FCTUC)  
<http://www.uc.pt/fctuc/deec/>



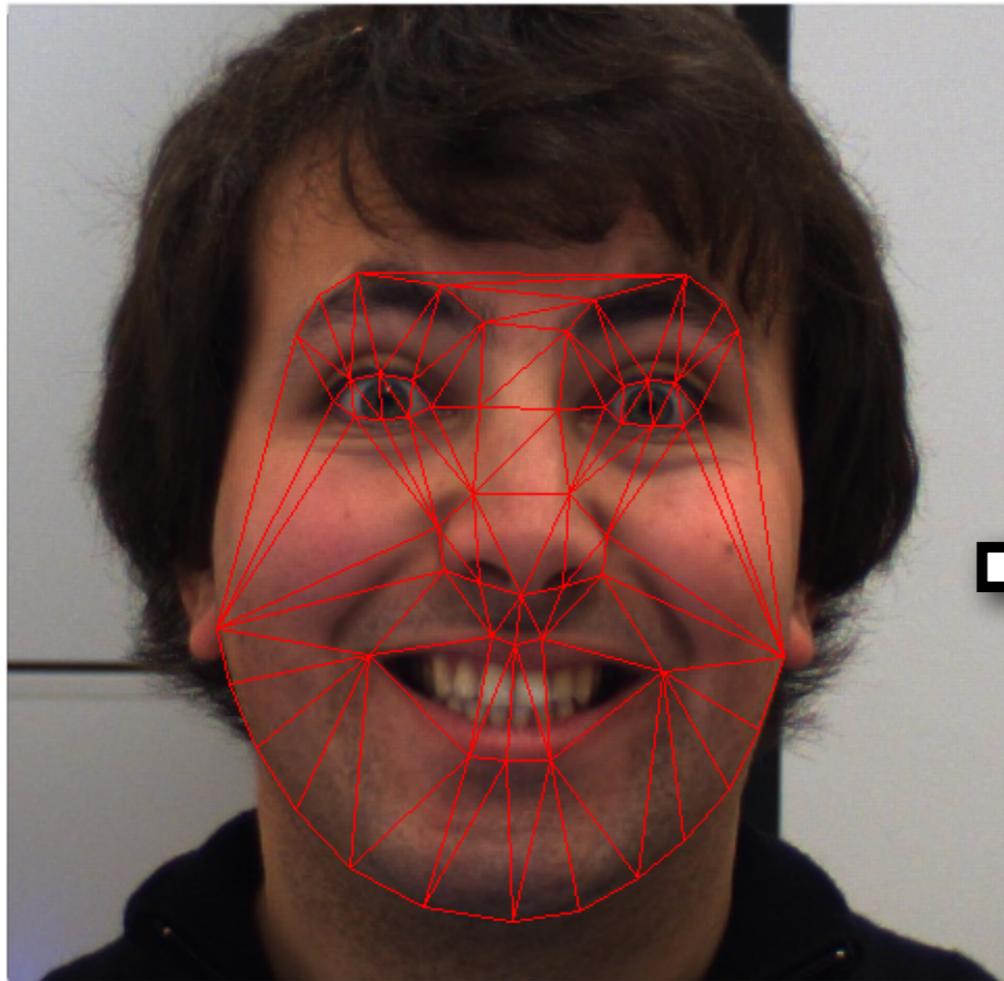
- Research supported by the Portuguese Science Foundation (*Fundação para a Ciência e Tecnologia* - FCT) under the PhD grant SFRH/BD/45178/2008  
<http://www.fct.pt/>



# Introduction

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- **Goal:** Non-Rigid Face Registration
- Model based approaches - Parametric Models of Shape and Appearance



**Normalized Template**



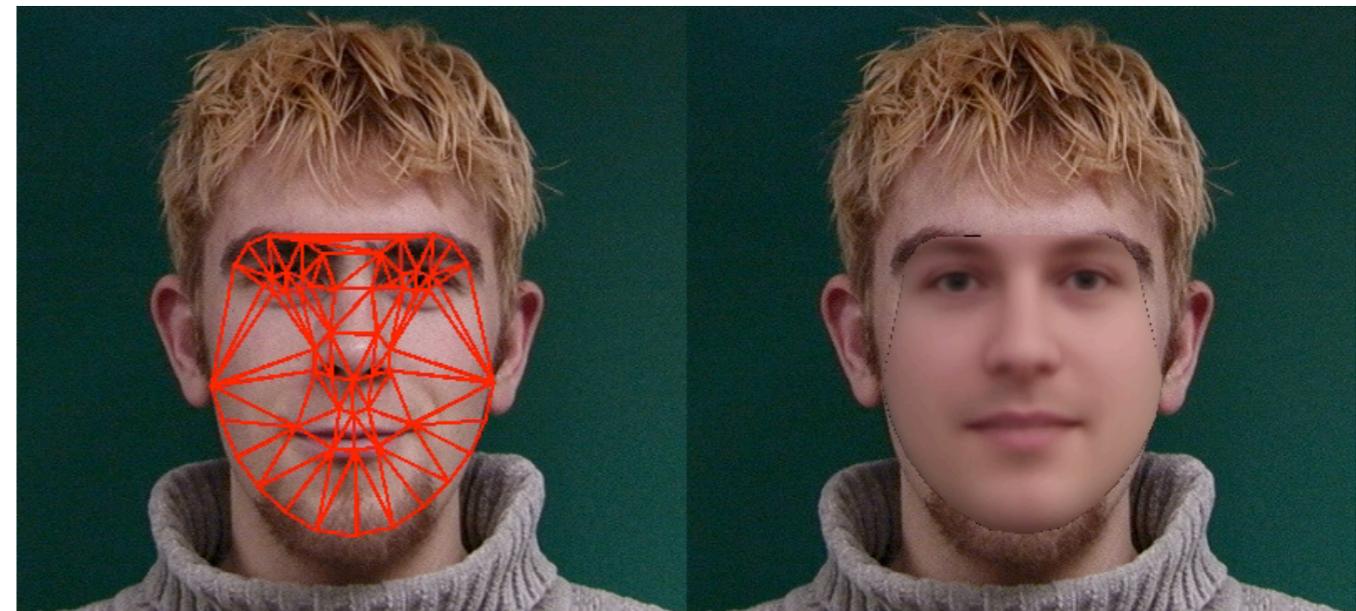
**Required for Several Tasks**

- Face Recognition
- Facial Expr. Recognition
- Tracking
- Head Pose Estimation
- Gaze Estimation
- Image Compression
- ...

**Model's Parameters:  $p, q, \lambda$**

# Parametric Image Alignment

- **Generative / Holistic Appearance Model**

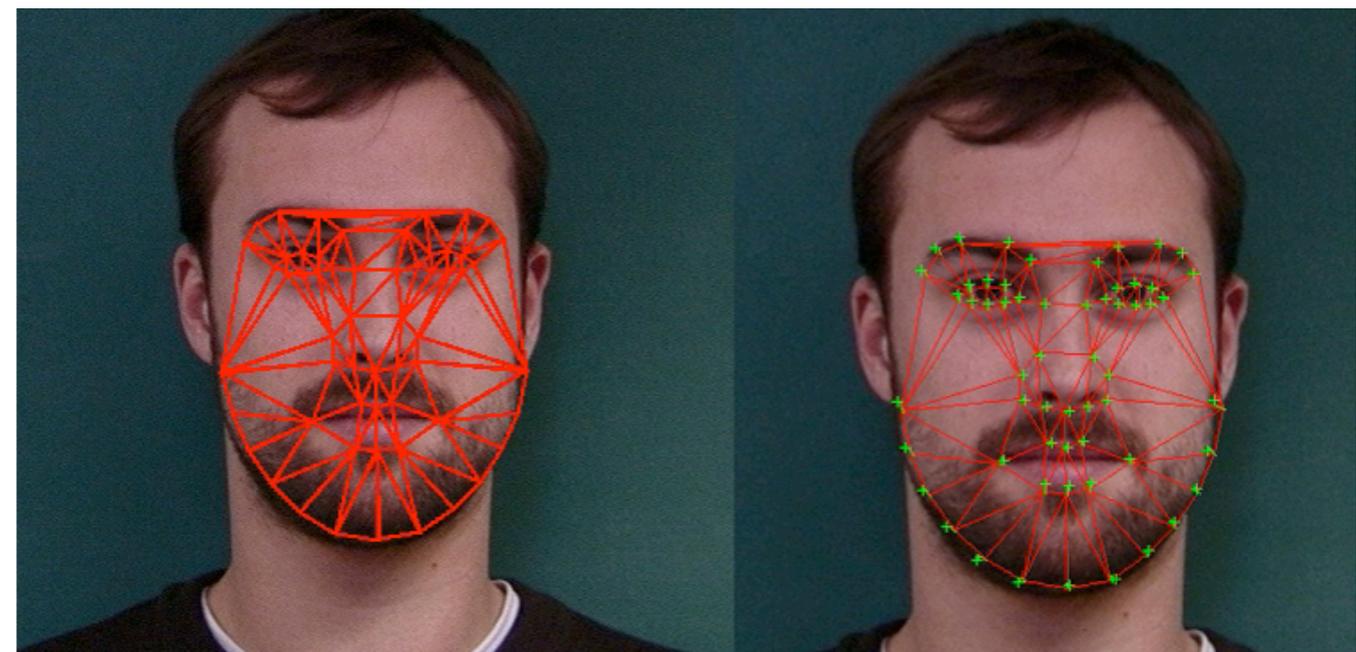


e.g. AAM, 3DMM, 2D+3D AAM

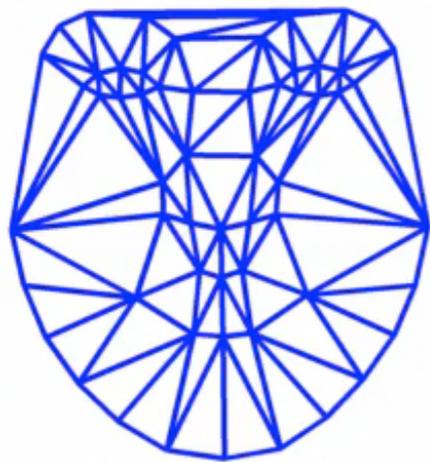
- **Discriminative / Patch Based Appearance Model**



e.g. ASM, CLM, CQF, SCMS



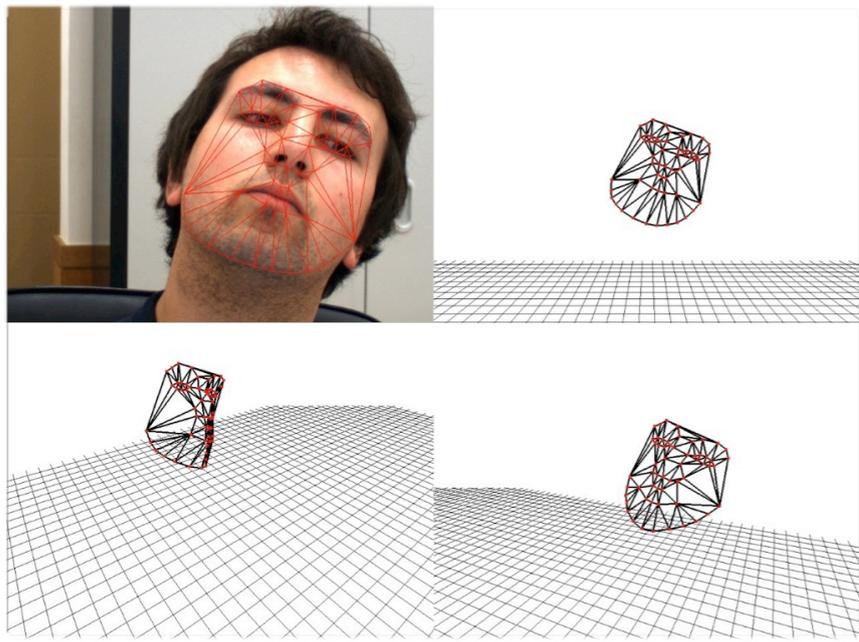
## Shape Model



## Point Distribution Model (PDM)

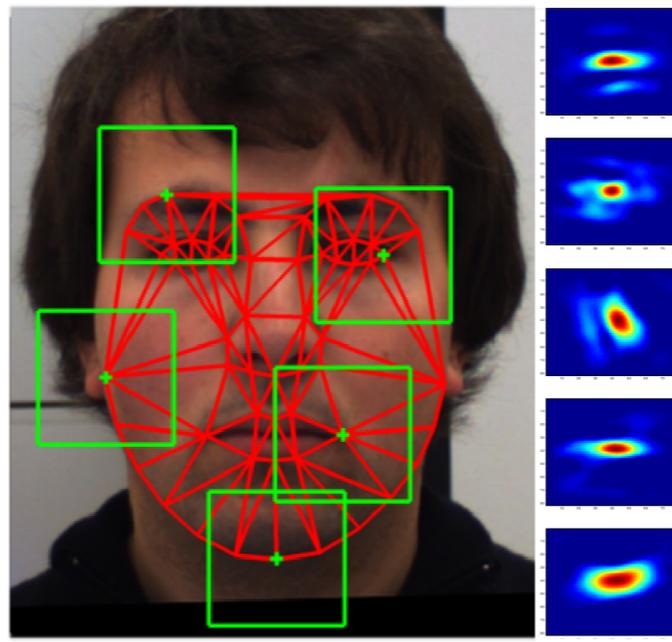
# Overview

## (1) Generative 2.5D AAM



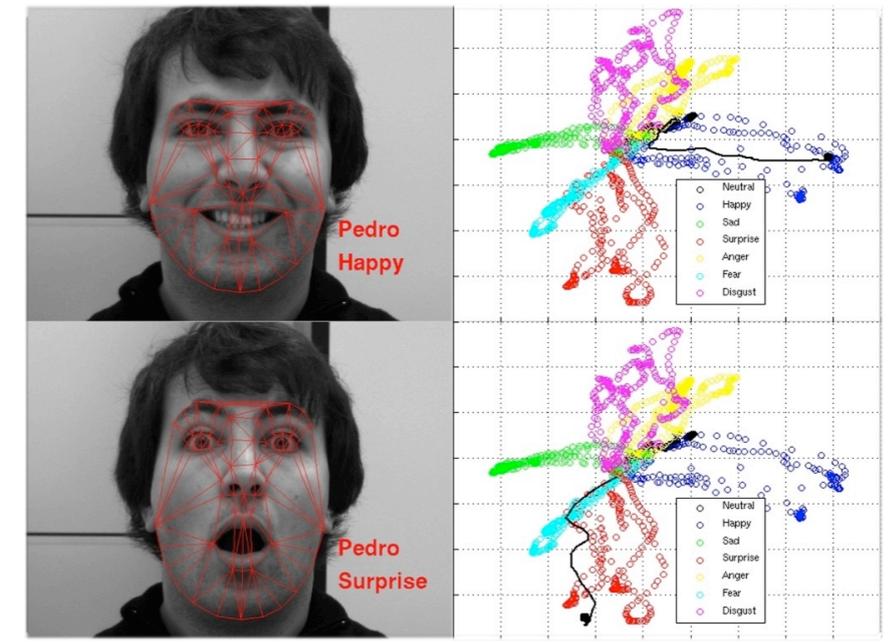
- Extension of the original 2D AAM that deals with a full perspective projection model.

## (2) Discriminative ASM

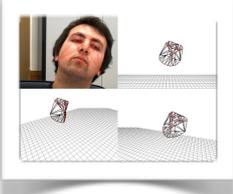


- New Bayesian global optimization strategy that infers the overall alignment using a second order estimate of the PDM parameters.

## (3) Identity / Facial Expression

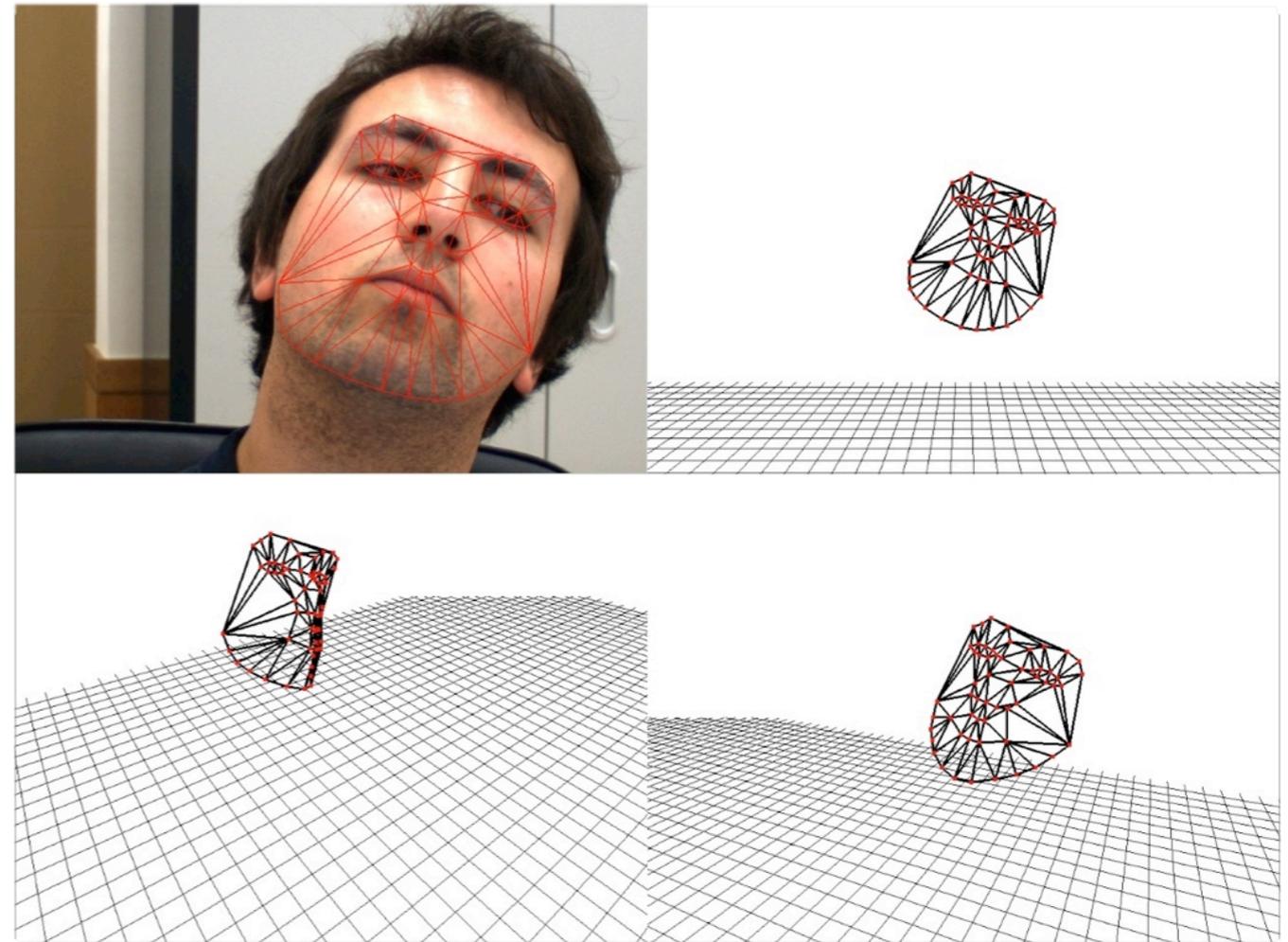


- Identity and facial expression recognition using facial geometry.



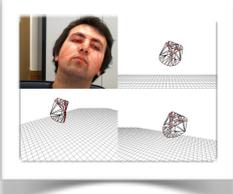
# (1) Generative 2.5D Active Appearance Models

- The 2.5D Active Appearance Models (AAM) combines a 3D PDM and a 2D appearance model.
- Extension of the original 2D AAM that deals with a full perspective projection model.
- Model fitting algorithms:
  - Simultaneous Forwards Additive (SFA).
  - Normalization Forwards Additive (NFA).
  - Efficient Approximations (ESFA, ENFA).
  - Robust to partial and self occlusions.
- Larger convergency radius.
- 3D shape from single images.
- (-) Slower than 2D methods.



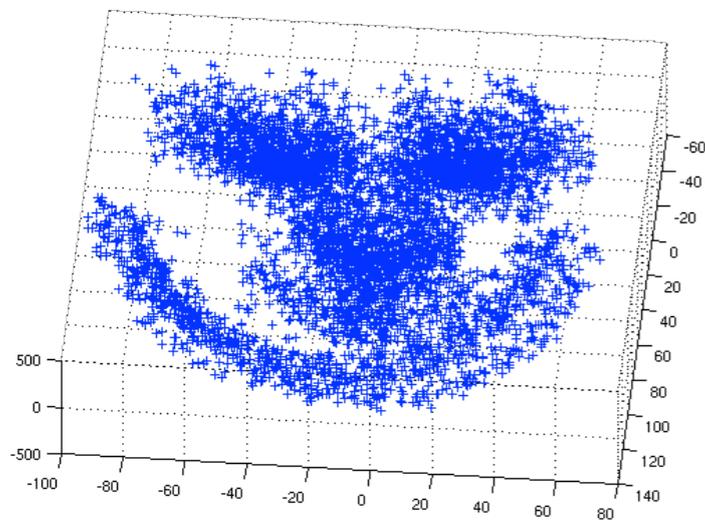
## • Previous Work:

- Active Appearance Models (AAM) - ECCV 1998
- Active Appearance Models Revisited - IJCV 2004
- Generic vs Person Specific AAMs - BMVC 2004
- Real Time Combined 2D+3D AAMs - CVPR 2004

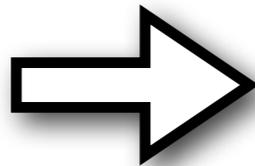


# Parametric Models of Shape and Appearance

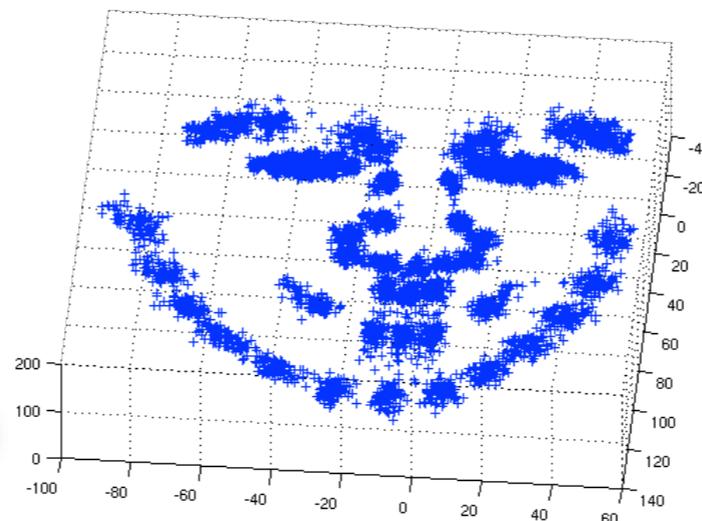
Raw Data



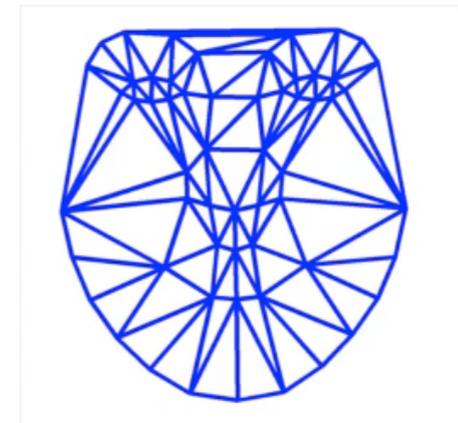
Procrustes Analysis



'Aligned' Data



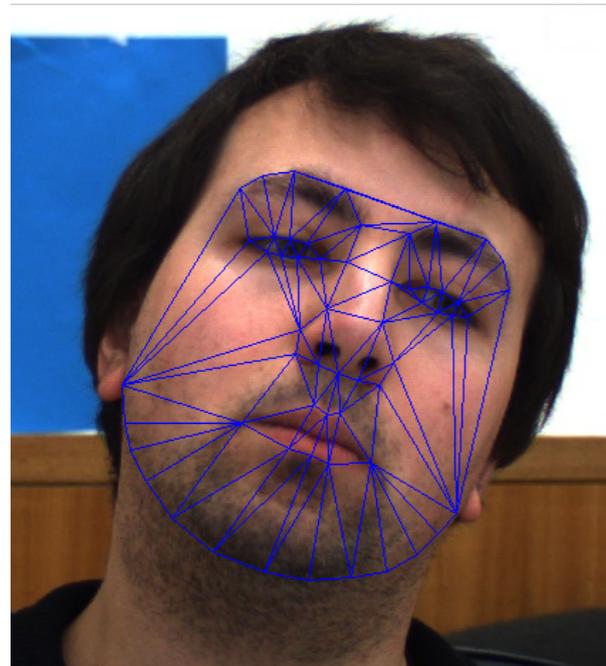
Shape Model



$$s = s_0 + \sum_{i=1}^n p_i \phi_i$$

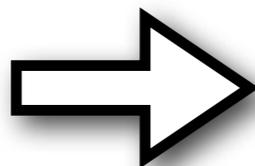


Shape Parameters

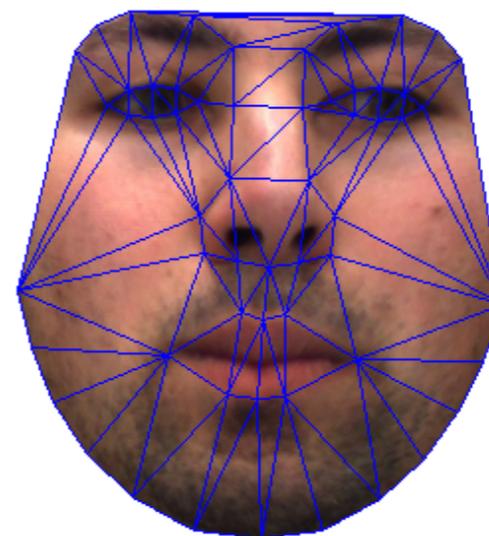


$I(\mathbf{x}_p)$

Piecewise Affine Warp



$$W(\mathbf{x}_p, \mathbf{p}, \mathbf{q})$$



$I(W(\mathbf{x}_p, \mathbf{p}, \mathbf{q}))$

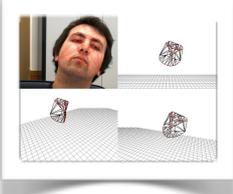
Appearance Model



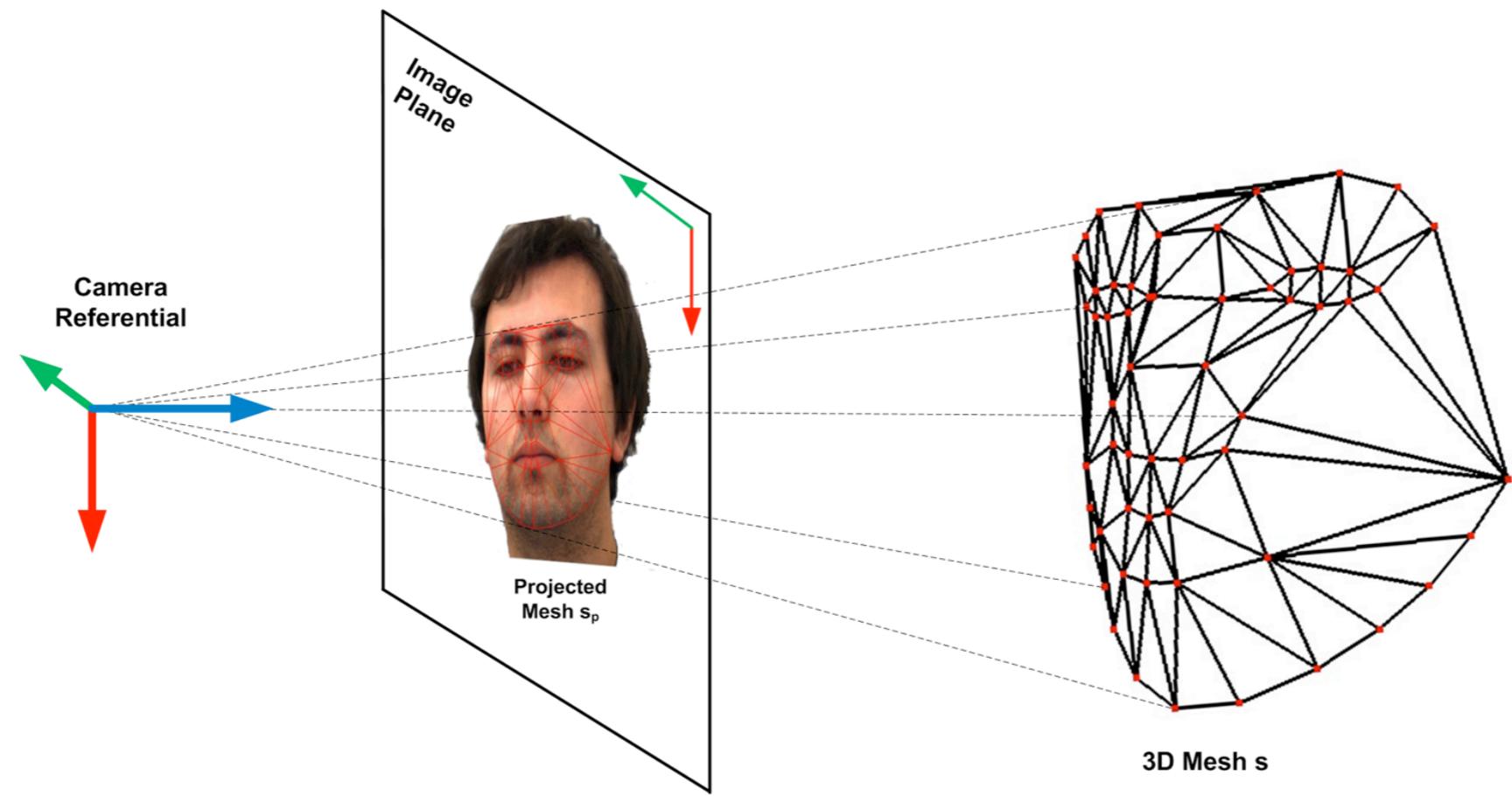
$$A(\mathbf{x}_p) = A_0(\mathbf{x}_p) + \sum_{i=1}^{m+2} \lambda_i A_i(\mathbf{x}_p), \quad \mathbf{x}_p \in s_0$$



Appearance Parameters



# The Shape Model



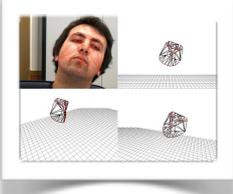
## Full Perspective Projection

$$\begin{bmatrix} w(x_1 \dots x_v) \\ w(y_1 \dots y_v) \\ w \dots w \end{bmatrix} = \underbrace{\begin{bmatrix} f_x & \alpha_s & c_x \\ 0 & f_y & c_y \\ 0 & 0 & 1 \end{bmatrix}}_{\mathbf{K}} \begin{bmatrix} \mathbf{R}_0 & | & \mathbf{t}_0 \end{bmatrix} \begin{bmatrix} s^{x_1} \dots s^{x_v} \\ s^{y_1} \dots s^{y_v} \\ s^{z_1} \dots s^{z_v} \\ 1 \dots 1 \end{bmatrix}$$

## 3D Point Distribution Model (PDM)

$$\mathbf{s} = \mathbf{s}_0 + \sum_{i=1}^n p_i \phi_i + \sum_{j=1}^6 q_j \psi_j^{(t)} + \underbrace{\int_0^{t-1} \sum_{j=1}^6 q_j \psi_j^{(t)} \partial t}_{s_\psi}$$

↑
↑  
 Pose Parameters                      Previous pose updates



# Model Fitting

$$\arg \min_{\mathbf{p}, \mathbf{q}, \lambda} \sum_{\mathbf{x}_p \in s_{0p}} \left[ \text{Image}_1 - \text{Image}_2 \right]^2$$

$$\arg \min_{\mathbf{p}, \mathbf{q}, \lambda} \sum_{\mathbf{x}_p \in s_{0p}} \left[ \mathbf{A}_0(\mathbf{x}_p) + \sum_{i=1}^{m+2} \lambda_i \mathbf{A}_i(\mathbf{x}_p) - \mathbf{I}(\mathbf{W}(\mathbf{x}_p, \mathbf{p}, \mathbf{q})) \right]^2$$

- Additive updates to the parameters

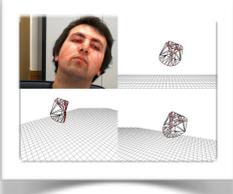
$$\sum_{\mathbf{x}_p \in s_{0p}} \left[ \mathbf{A}_0(\mathbf{x}_p) + \sum_{i=1}^{m+2} (\lambda_i + \Delta \lambda_i) \mathbf{A}_i(\mathbf{x}_p) - \mathbf{I}(\mathbf{W}(\mathbf{x}_p, \mathbf{p} + \Delta \mathbf{p}, \mathbf{q} + \Delta \mathbf{q})) \right]^2$$

- Expanding and holding first order terms

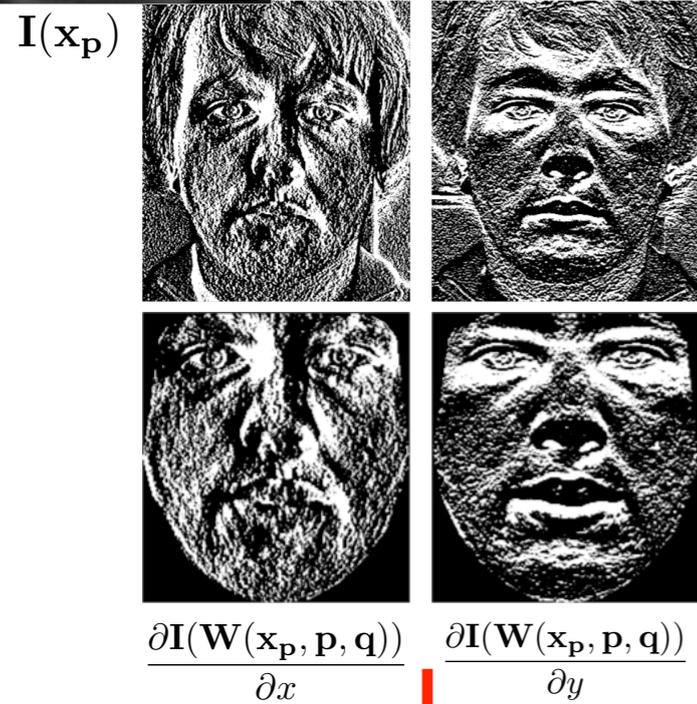
$$\sum_{\mathbf{x}_p \in s_{0p}} \left[ \mathbf{A}_0(\mathbf{x}_p) + \sum_{i=1}^{m+2} \lambda_i \mathbf{A}_i(\mathbf{x}_p) - \mathbf{I}(\mathbf{W}(\mathbf{x}_p, \mathbf{p}, \mathbf{q})) - \mathbf{SD}(\mathbf{x}_p)_{\text{sfa}} \Delta \mathbf{r} \right]^2 \quad \mathbf{r} = \begin{bmatrix} \mathbf{p} \\ \mathbf{q} \\ \lambda \end{bmatrix}$$

- Parameters updates

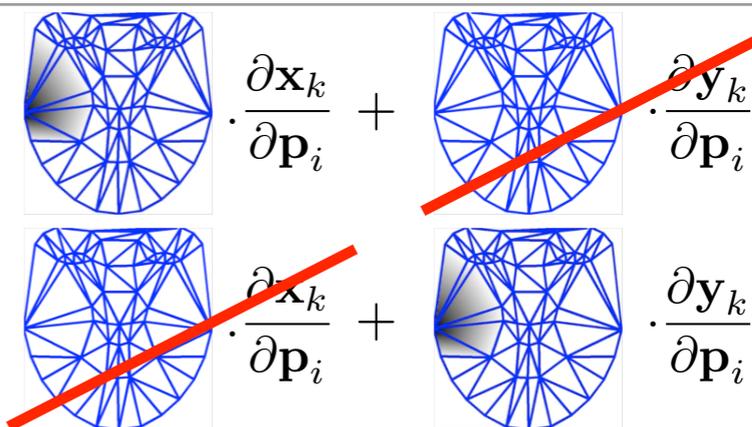
$$\Delta \mathbf{r} = \mathbf{H}_{\text{sfa}}^{-1} \sum_{\mathbf{x}_p \in s_{0p}} \mathbf{SD}(\mathbf{x}_p)_{\text{sfa}}^T \mathbf{E}(\mathbf{x}_p)_{\text{sfa}} \quad \mathbf{r} \leftarrow \mathbf{r} + \Delta \mathbf{r}$$



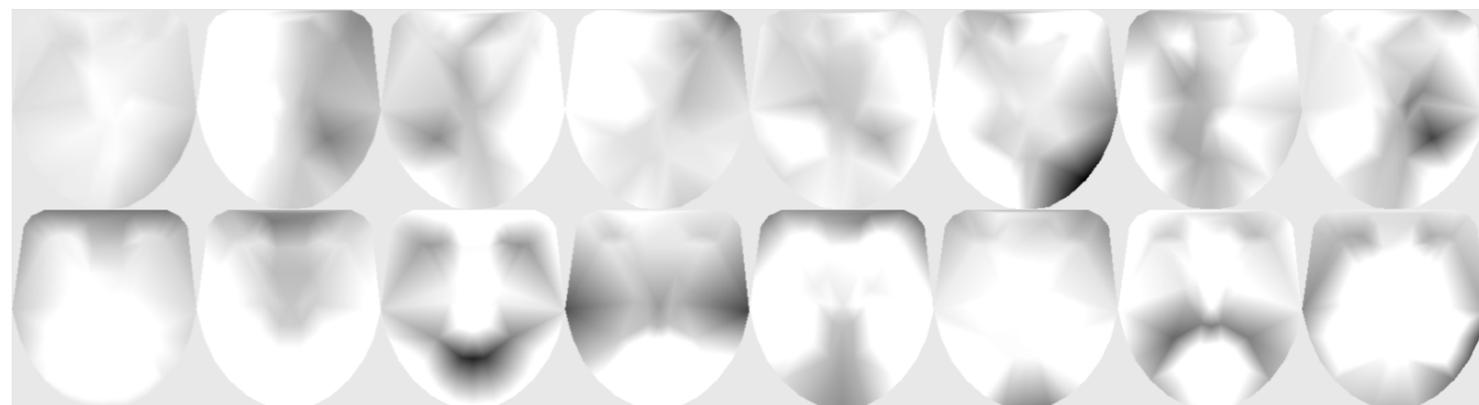
# Simultaneous Forwards Additive (SFA)



The Jacobian of the Warp



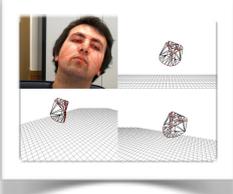
$$\frac{\partial W(x_p, p, q)}{\partial p} = \sum_{k=1}^v \left[ \frac{\partial W(x_p, p, q)}{\partial x_k} \frac{\partial x_k}{\partial p} + \frac{\partial W(x_p, p, q)}{\partial y_k} \frac{\partial y_k}{\partial p} \right]$$



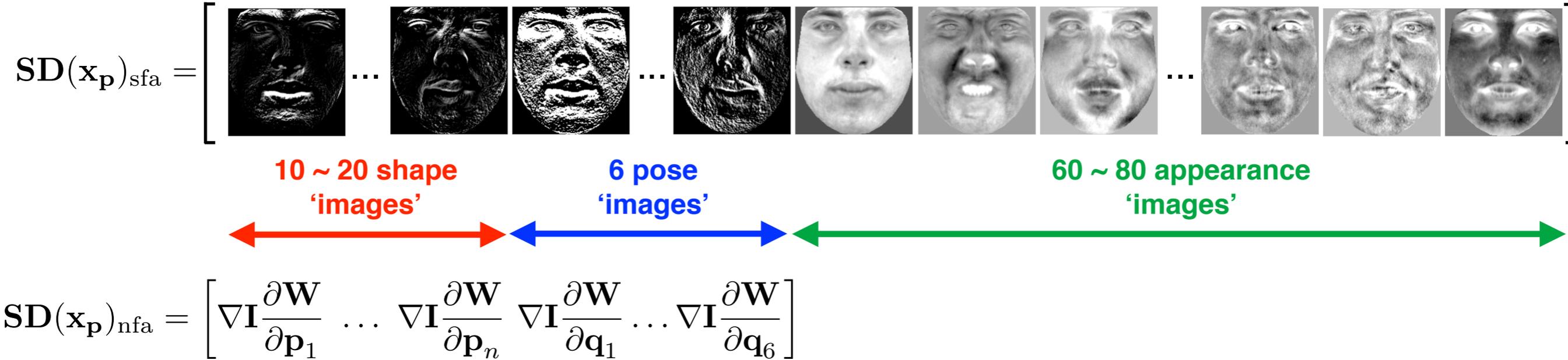
EigenFaces

$$SD(x_p)_{sfa} = \left[ \nabla I \frac{\partial W}{\partial p_1} \dots \nabla I \frac{\partial W}{\partial p_n} \nabla I \frac{\partial W}{\partial q_1} \dots \nabla I \frac{\partial W}{\partial q_6} - \mathbf{A}_1(x_p) \dots - \mathbf{A}_{m+2}(x_p) \right]$$





# Normalization Forwards Additive (NFA)



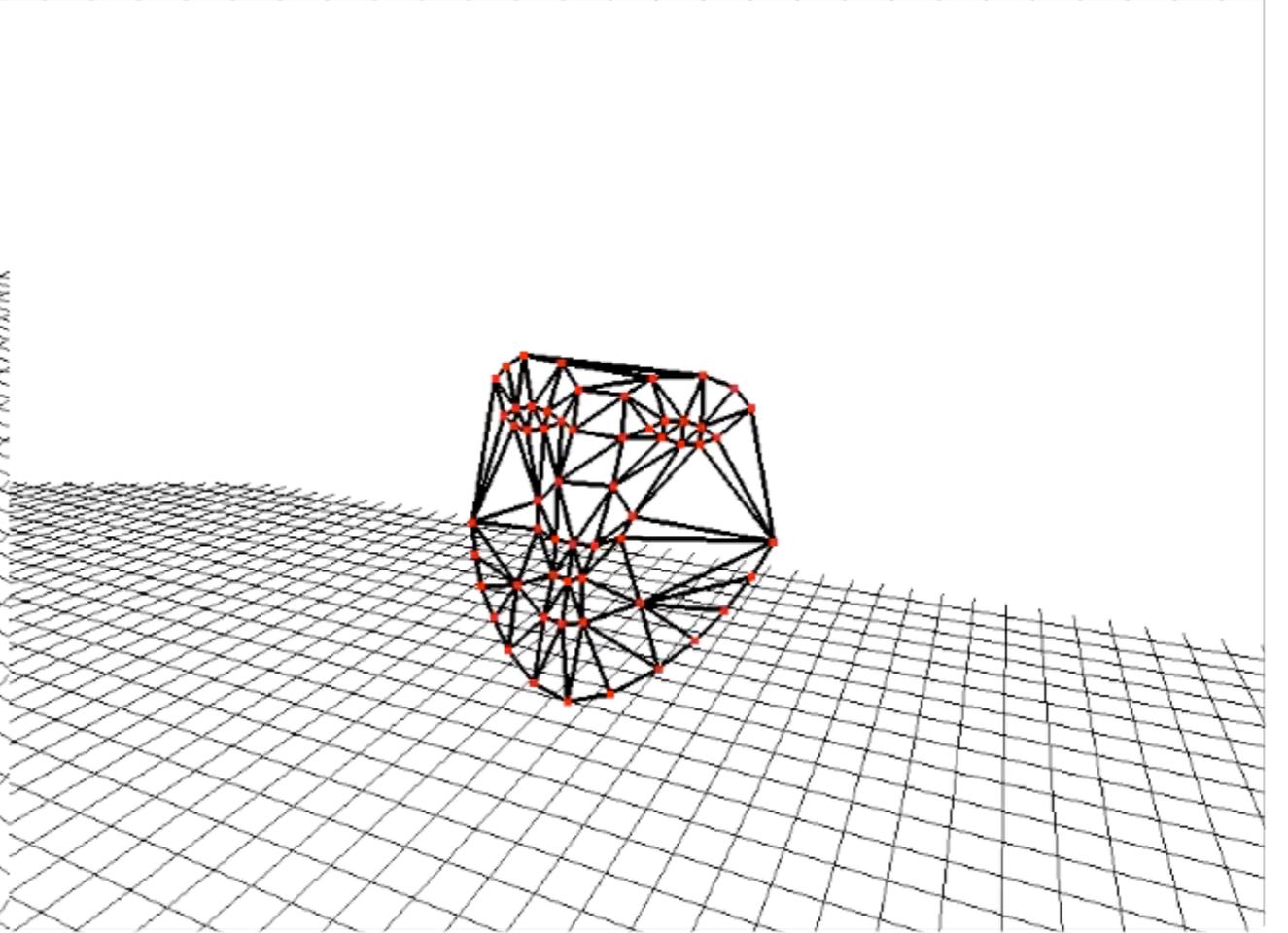
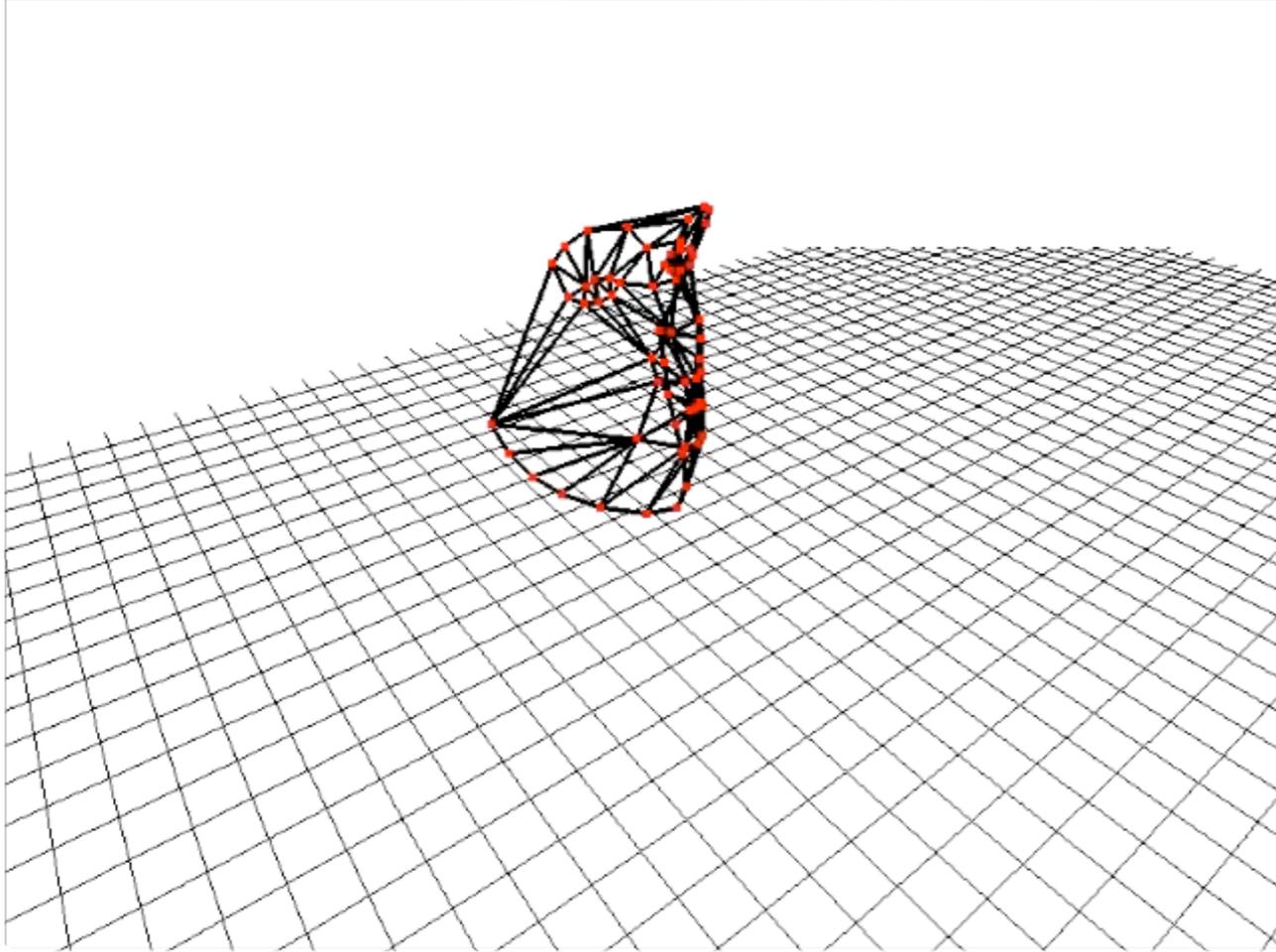
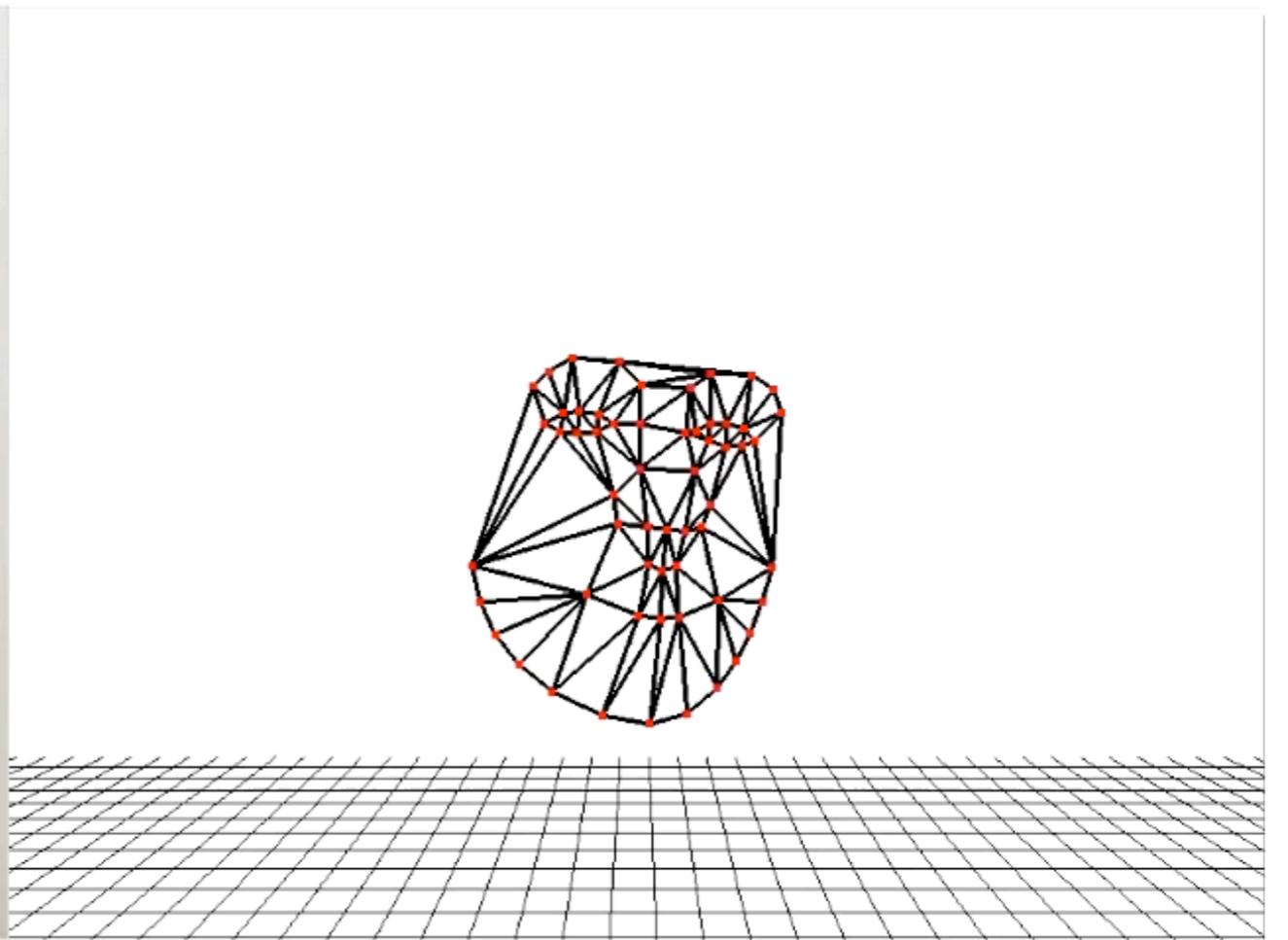
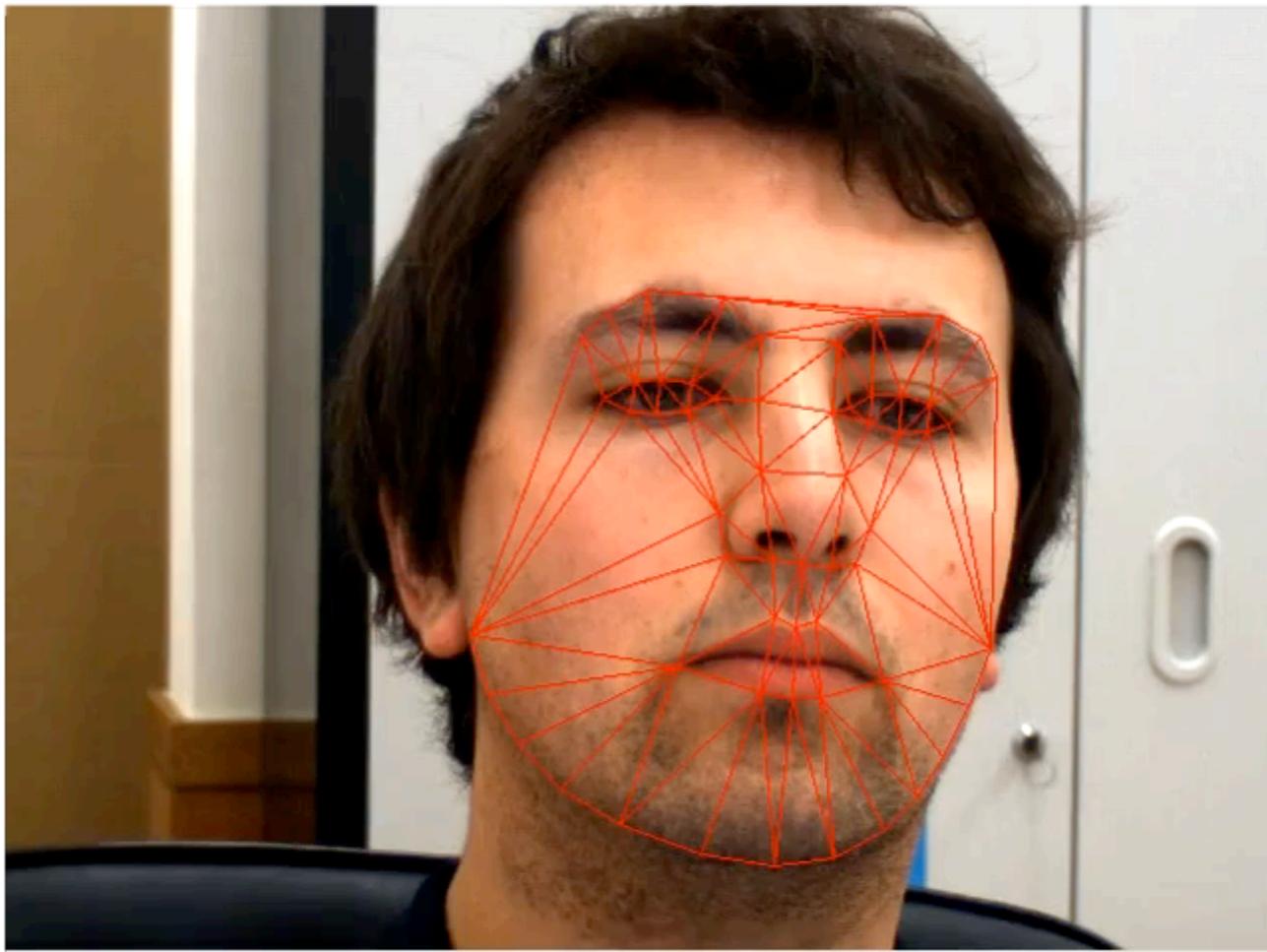
- Project Error Image into Appearance Basis

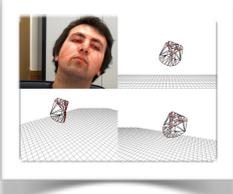
$$\lambda_i = \sum_{\mathbf{x}_p \in s_{0p}} \mathbf{A}_i(\mathbf{x}_p) \underbrace{(\mathbf{I}(\mathbf{W}(\mathbf{x}_p, \mathbf{p}, \mathbf{q})) - \mathbf{A}_0(\mathbf{x}_p))}_{\mathbf{E}(\mathbf{x}_p)_{\text{lk}}}$$

Error Image

- Normalize the Error Image

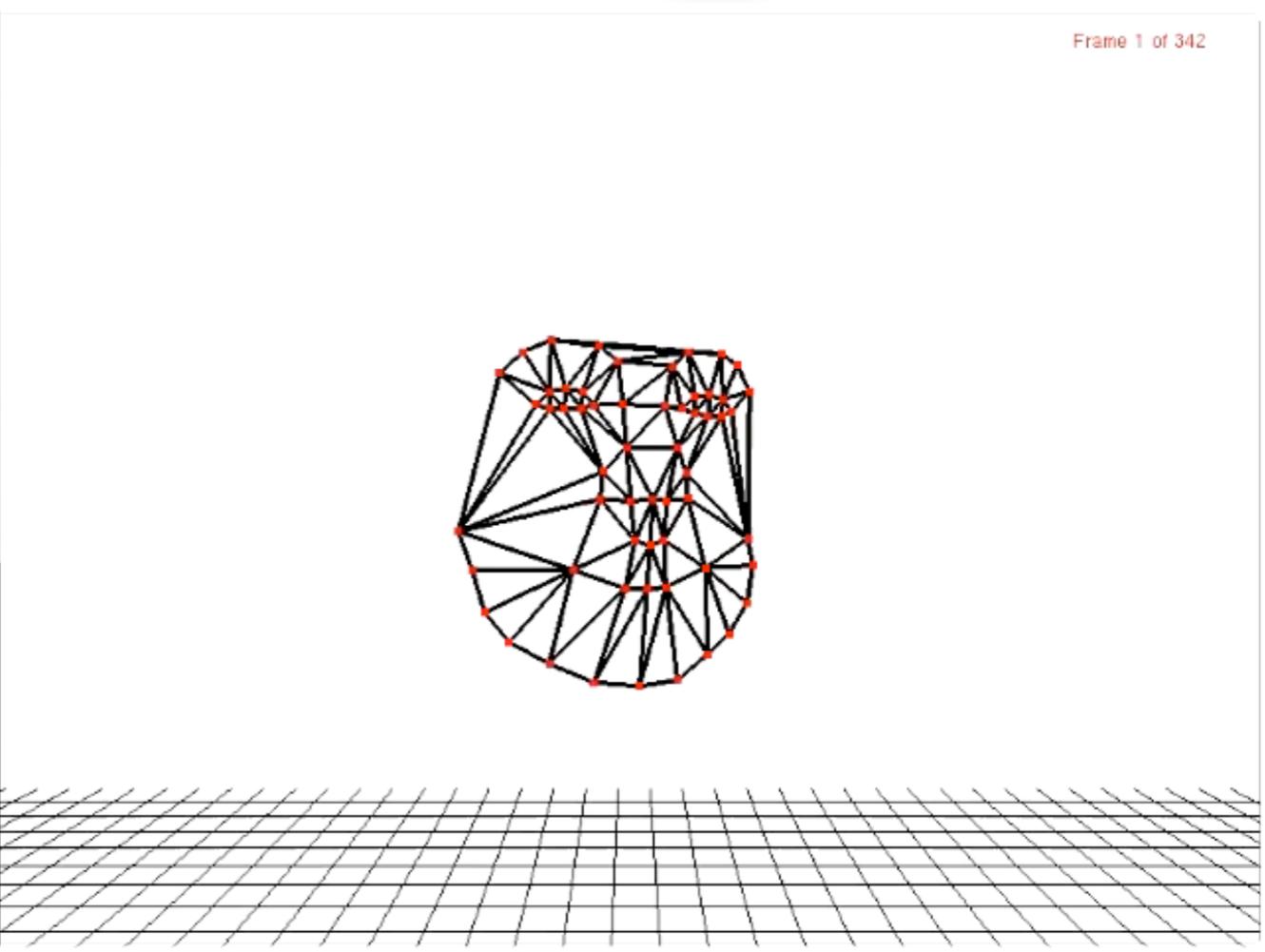
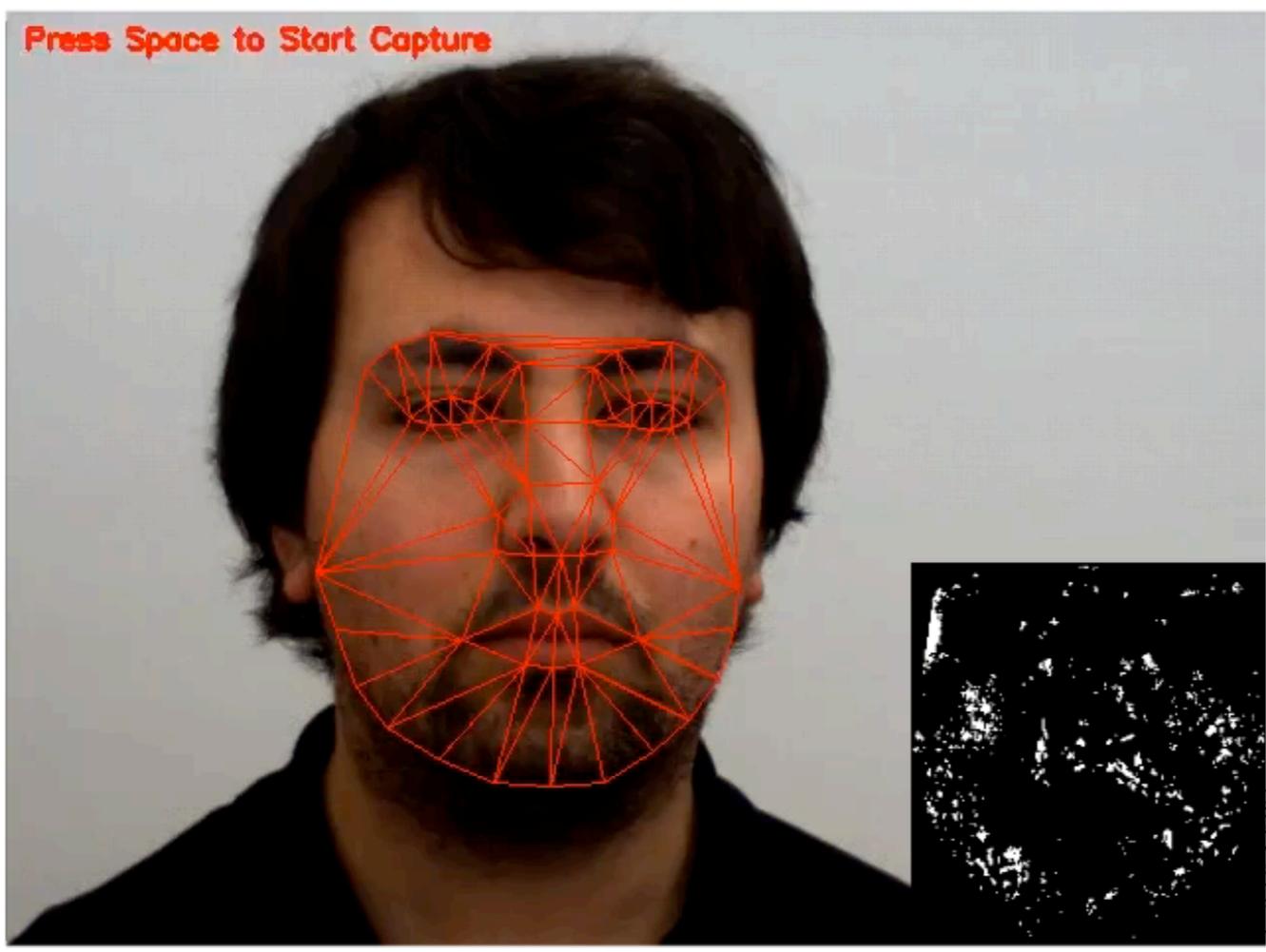
$$\mathbf{E}_{\text{nfa}}(\mathbf{x}_p) = \mathbf{E}(\mathbf{x}_p)_{\text{lk}} - \sum_{i=1}^{m+2} \lambda_i \mathbf{A}_i(\mathbf{x}_p)$$

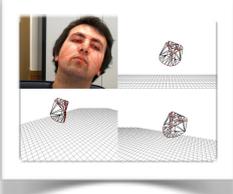




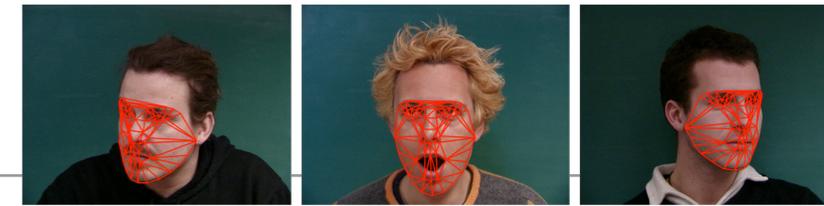
# Robust Fitting

$$\arg \min_{\mathbf{p}, \mathbf{q}, \lambda} \sum_{\mathbf{x}_p \in s_{0p}} \left[ \text{Image} - \text{Model} \right]^2$$
$$\arg \min_{\mathbf{p}, \mathbf{q}, \lambda} \sum_{\mathbf{x}_p \in s_{0p}} \rho \left( \left[ \mathbf{A}_0(\mathbf{x}_p) + \sum_{i=1}^{m+2} \lambda_i \mathbf{A}_i(\mathbf{x}_p) - \mathbf{I}(\mathbf{W}(\mathbf{x}_p, \mathbf{p}, \mathbf{q})) \right]^2, \sigma_{\mathbf{x}_p} \right) \rightarrow \text{MAD}$$





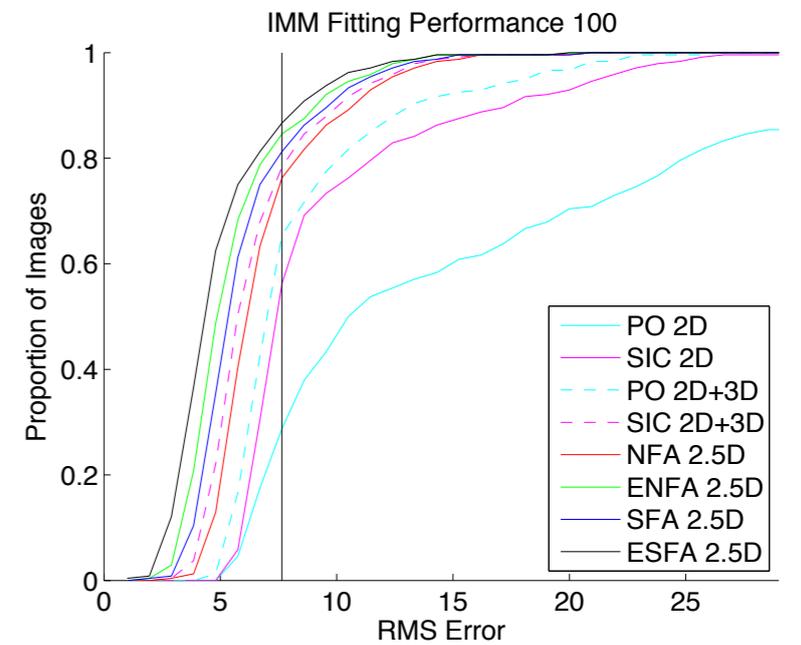
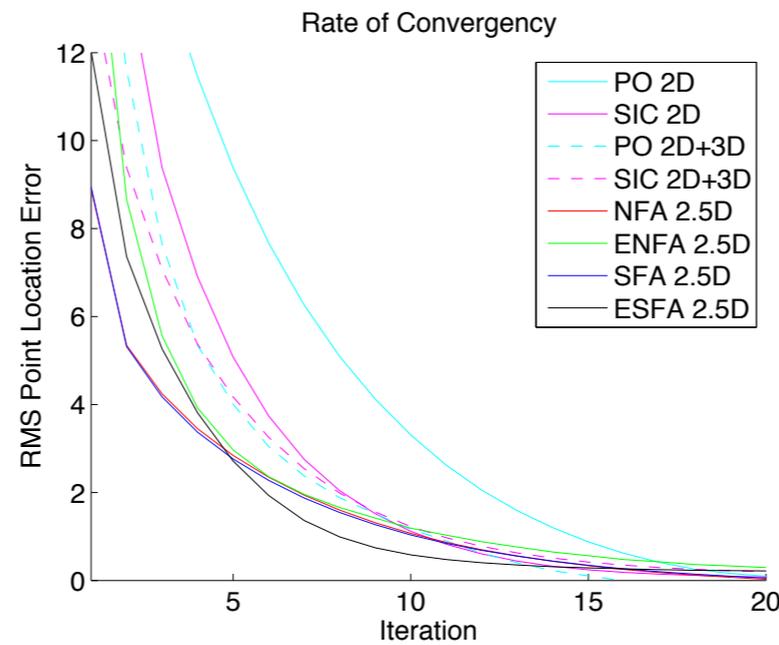
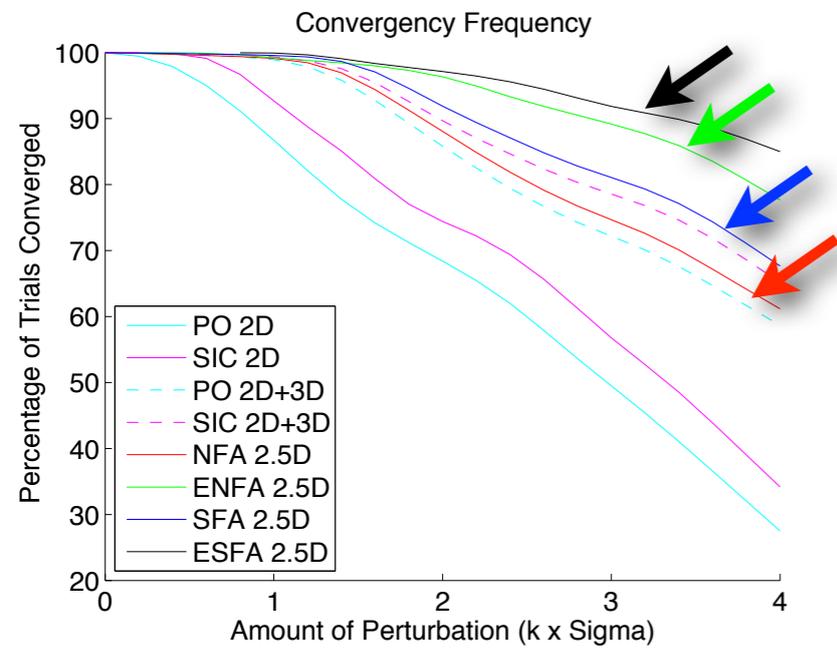
# Evaluation Results



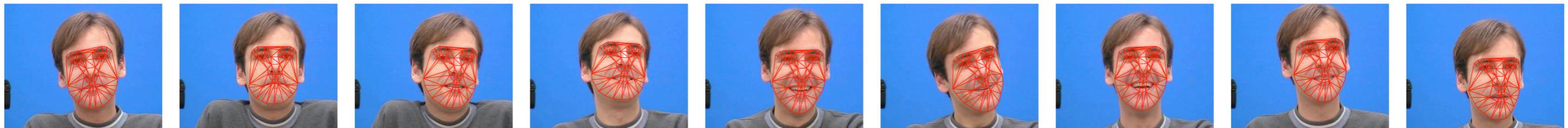
## Convergency Frequency

## Rate of Convergency

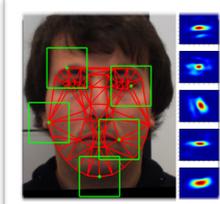
## Fitting Performance Curve



## Tracking Performance - FGNET Talking Face

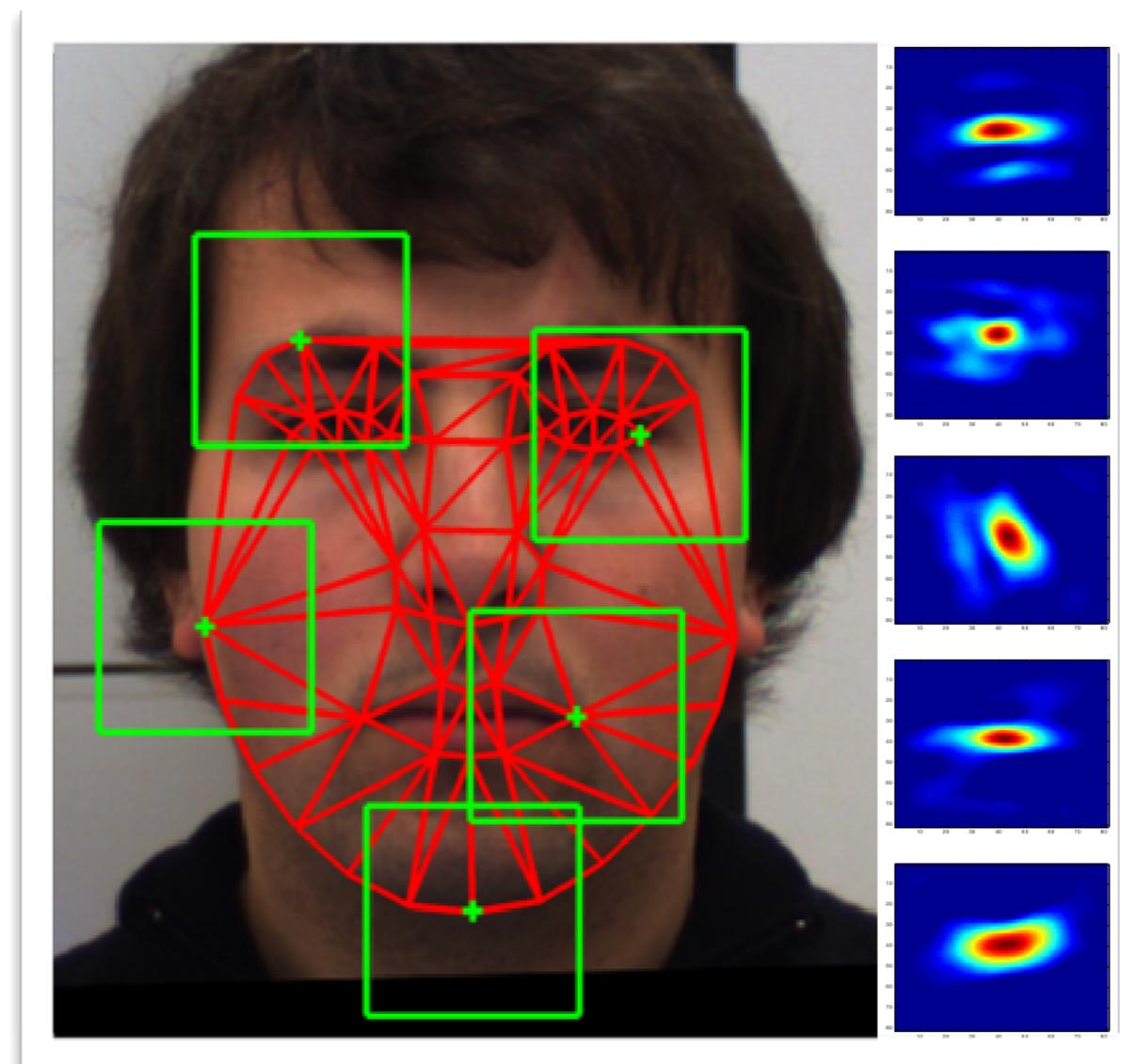


<b>RMS Error</b>	<b>PO</b>	<b>PO 2D+3D</b>	<b>NFA 2.5D</b>	<b>ENFA 2.5D</b>	<b>SIC 2D</b>	<b>SIC 2D+3D</b>	<b>SFA 2.5D</b>	<b>ESFA 2.5D</b>
<b>Mean</b>	7.4	7.0	6.6	6.2	7.1	6.6	6.4	<b>6.0</b>
<b>Standard Deviation</b>	3.4	2.5	2.1	1.3	3.3	3.2	1.4	<b>1.2</b>



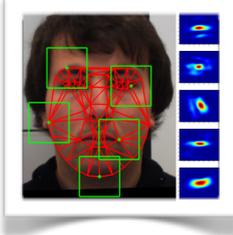
## (2) Discriminative Bayesian Active Shape Models

- Related to CLM and/or ASM, where a set of local detectors is constrained to lie in the subspace spanned by a PDM.
- Two step model fitting approach:
  - (1) Local search using the detectors.
  - (2) Global optimization strategy that finds the PDM parameters that jointly maximize all the detections.
- New Bayesian global optimization strategy that infers the overall alignment using a second order estimate of the PDM parameters.
- Extension that models the prior distribution.
- Performance in unseen data
- Efficient and simple approach.
- Fusion of multiple detectors.



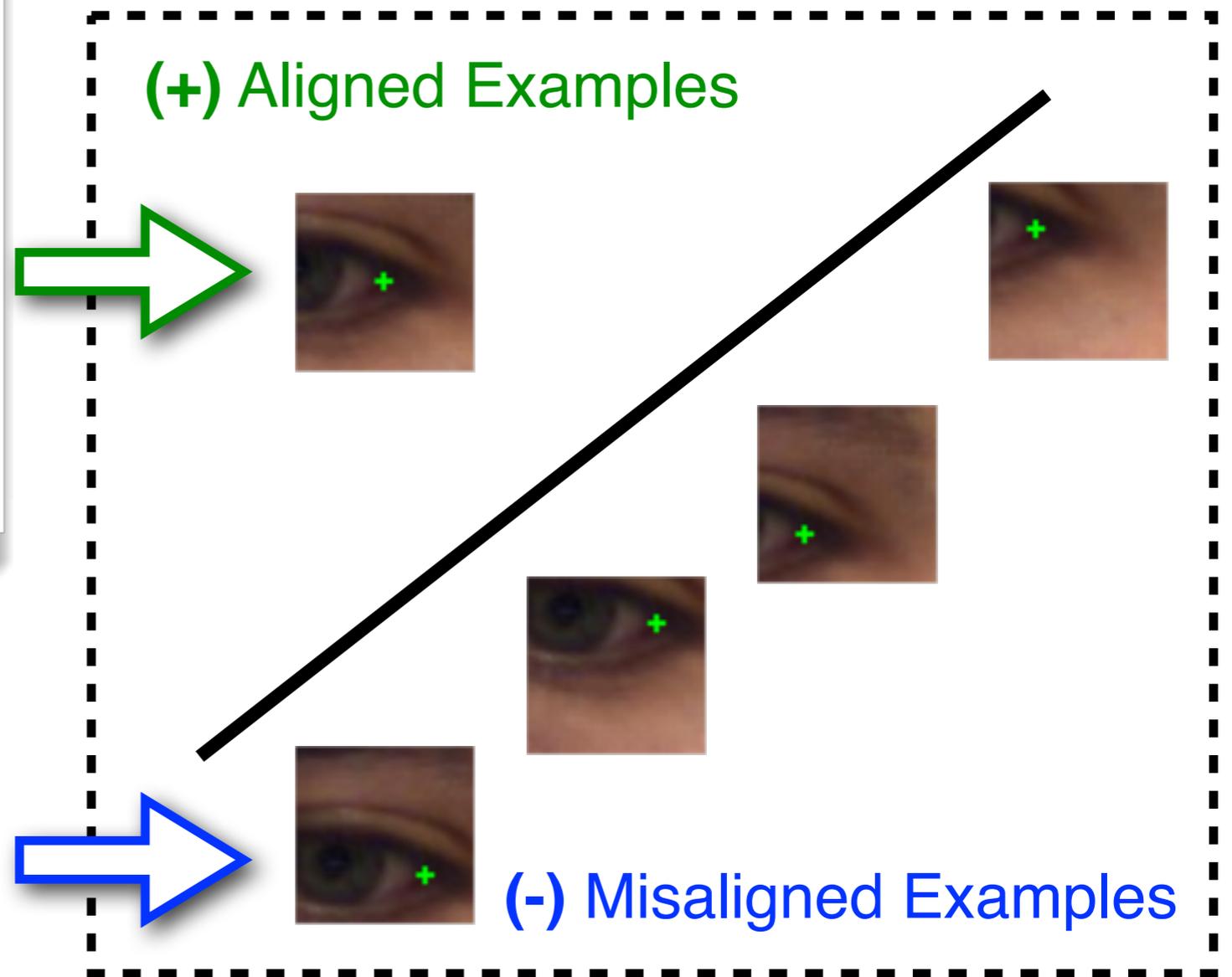
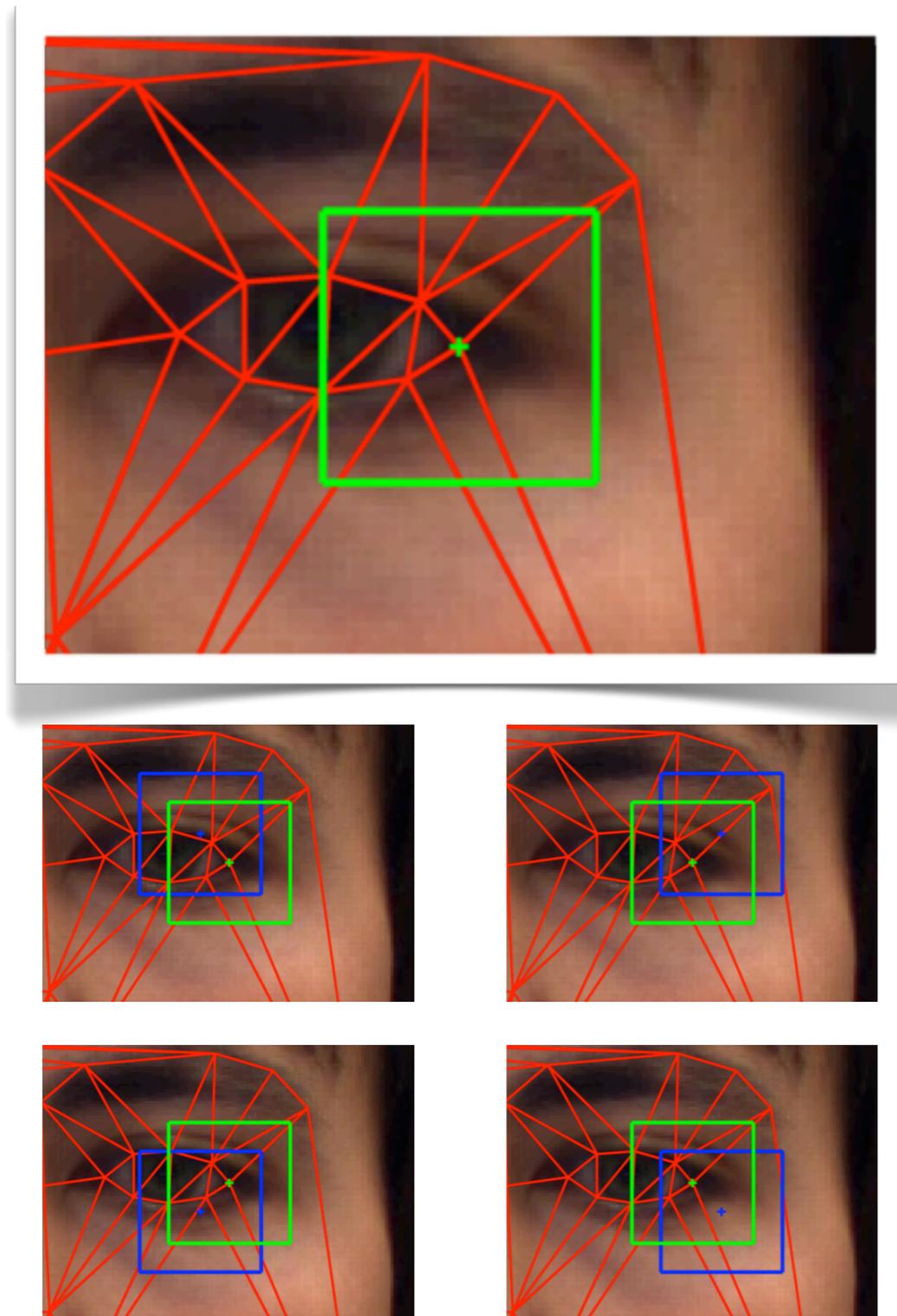
### • Previous Work:

- Active Shape Models (ASM) - CVIU 1995
- Constrained Local Model (CLM) - BMVC 2006
- Convex Quadratic Fitting (CQF) - CVPR 2008
- Subspace Constrained Mean-Shifts (SCMS) - ICCV 2009



# Local Landmark Detectors

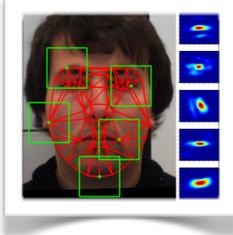
## Linear SVM



$$\mathcal{D}_i^{\text{linear}}(\mathbf{I}(\mathbf{y}_i)) = \mathbf{w}_i^T \mathbf{I}(\mathbf{y}_i) + b_i$$

$i = 1, \dots, v$  landmarks





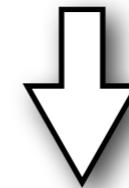
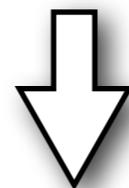
# The Alignment Goal

- Given a shape observation vector ( $\mathbf{y}$ ), find the optimal set of shape (and pose) parameters ( $\mathbf{b}$ ) that maximize the posterior probability

$$\mathbf{b}^* = \arg \max_{\mathbf{b}} p(\mathbf{b}|\mathbf{y}) \propto p(\mathbf{y}|\mathbf{b})p(\mathbf{b})$$

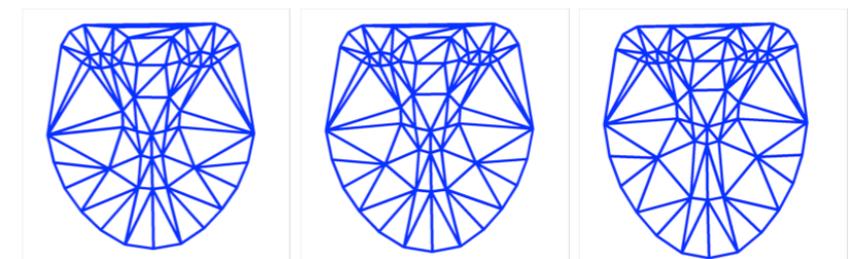
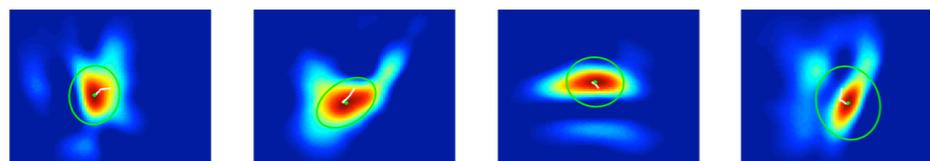
- Assuming:
  - Conditional independence between landmarks
  - Close to a solution

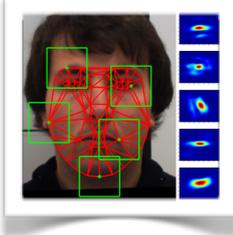
$$p(\mathbf{b}|\mathbf{y}) \propto \left( \prod_{i=1}^v p(\mathbf{y}_i|\mathbf{b}) \right) p(\mathbf{b}|\mathbf{b}_{k-1}^*)$$



**Likelihood** from the local detectors

**Prior** on how parameters change





# The Likelihood Term

- Convex energy function:

Observed shape ( $\mathbf{y}$ )

$$p(\mathbf{y}|\mathbf{b}) \propto \exp \left( -\frac{1}{2} \underbrace{(\mathbf{y} - (\mathbf{s}_0 + \Phi\mathbf{b}))}_{\Delta\mathbf{y}}^T \Sigma_{\mathbf{y}}^{-1} (\mathbf{y} - (\mathbf{s}_0 + \Phi\mathbf{b})) \right)$$

Uncertainty covariance

Difference between the **observed** and the **mean shape**

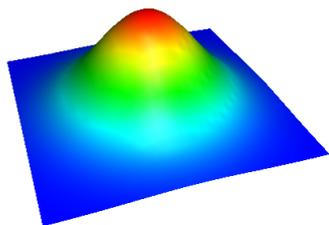
The likelihood follow a Gaussian distribution

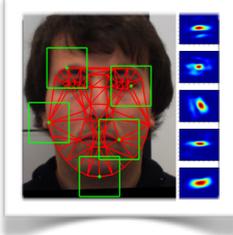
$$p(\mathbf{y}|\mathbf{b}) \propto \mathcal{N}(\Delta\mathbf{y}|\Phi\mathbf{b}, \Sigma_{\mathbf{y}})$$

$\Sigma_{\mathbf{y}}$

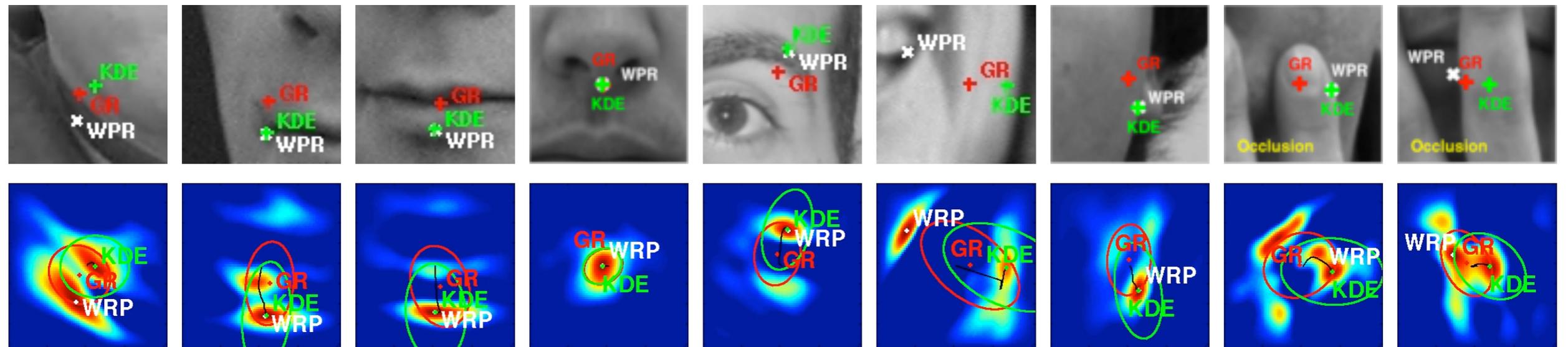
				0
		...		
0				

$2v \times 2v$  Block diagonal

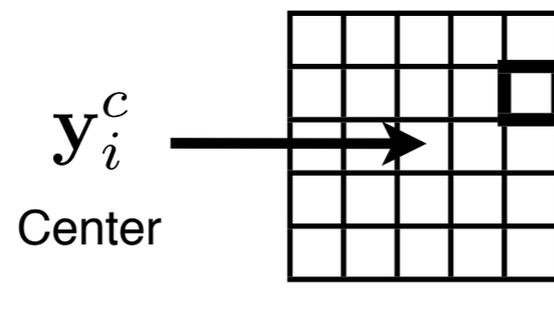




# Local Optimization Strategies



$p_i(\mathbf{z}_i)$   
Prob.  $\mathbf{z}_i$  is aligned



$\mathbf{z}_i = (x_i, y_i)$   
Pixel candidate to  $i^{\text{th}}$  landmark location  
 $\Omega_{\mathbf{y}_i^c}$  Local search grid

Patches under occlusion

**Weighted Peak Response (WPR)**

**Gaussian Response (GR)**

**Kernel Density Estimator (KDE)**

$$\mathbf{y}_i^{\text{WPR}} = \max_{\mathbf{z}_i \in \Omega_{\mathbf{y}_i^c}} (p_i(\mathbf{z}_i))$$

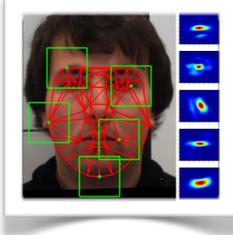
$$\Sigma_{\mathbf{y}_i}^{\text{WPR}} = \text{diag}(p_i(\mathbf{y}_i^{\text{WPR}})^{-1})$$

$$\mathbf{y}_i^{\text{GR}} = \frac{1}{d} \sum_{\mathbf{z}_i \in \Omega_{\mathbf{y}_i^c}} p_i(\mathbf{z}_i) \mathbf{z}_i \quad d = \sum_{\mathbf{z}_i \in \Omega_{\mathbf{y}_i^c}} p_i(\mathbf{z}_i)$$

$$\Sigma_{\mathbf{y}_i}^{\text{GR}} = \frac{1}{d-1} \sum_{\mathbf{z}_i \in \Omega_{\mathbf{y}_i^c}} p_i(\mathbf{z}_i) (\mathbf{z}_i - \mathbf{y}_i^{\text{GR}}) (\mathbf{z}_i - \mathbf{y}_i^{\text{GR}})^T$$

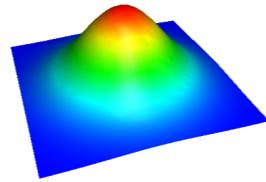
$$\mathbf{y}_i^{\text{KDE}(\tau+1)} \leftarrow \frac{\sum_{\mathbf{z}_i \in \Omega_{\mathbf{y}_i^c}} \mathbf{z}_i p_i(\mathbf{z}_i) \mathcal{N}(\mathbf{y}_i^{\text{KDE}(\tau)} | \mathbf{z}_i, \sigma_{h_j}^2 \mathbf{I}_2)}{\sum_{\mathbf{z}_i \in \Omega_{\mathbf{y}_i^c}} p_i(\mathbf{z}_i) \mathcal{N}(\mathbf{y}_i^{\text{KDE}(\tau)} | \mathbf{z}_i, \sigma_{h_j}^2 \mathbf{I}_2)}$$

$$\Sigma_{\mathbf{y}_i}^{\text{KDE}} = \frac{1}{d-1} \sum_{\mathbf{z}_i \in \Omega_{\mathbf{y}_i^c}} p_i(\mathbf{z}_i) (\mathbf{z}_i - \mathbf{y}_i^{\text{KDE}}) (\mathbf{z}_i - \mathbf{y}_i^{\text{KDE}})^T$$



# MAP Global Alignment (DBASM)

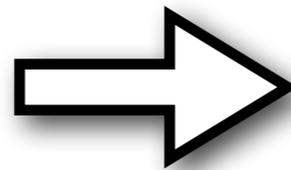
**Likelihood**



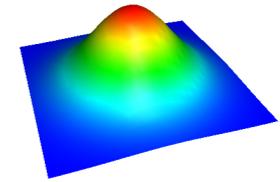
$$p(\mathbf{y}|\mathbf{b}) \propto \mathcal{N}(\Delta\mathbf{y}|\Phi\mathbf{b}, \Sigma_{\mathbf{y}})$$

Mean that is function of  $\mathbf{b}$   
Covariance independent of  $\mathbf{b}$

Bayes's Theorem for  
Gaussian variables



**Posterior**

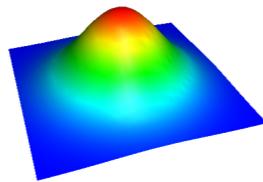


$$p(\mathbf{b}_k|\mathbf{y}) \propto \mathcal{N}(\mathbf{b}_k|\boldsymbol{\mu}, \boldsymbol{\Sigma})$$

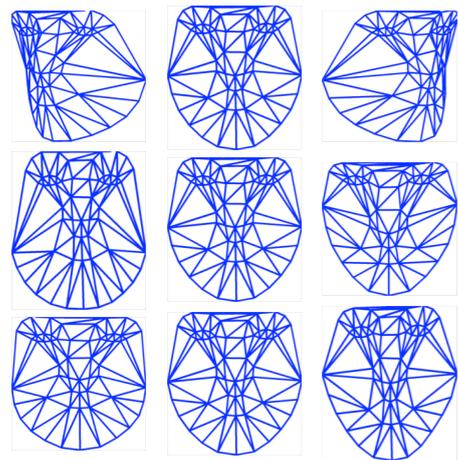
$$\boldsymbol{\Sigma} = (\boldsymbol{\Sigma}_{\mathbf{b}}^{-1} + \Phi^T \boldsymbol{\Sigma}_{\mathbf{y}}^{-1} \Phi)^{-1}$$

$$\boldsymbol{\mu} = \boldsymbol{\Sigma}(\Phi^T \boldsymbol{\Sigma}_{\mathbf{y}}^{-1} \mathbf{y} + \boldsymbol{\Sigma}_{\mathbf{b}}^{-1} \boldsymbol{\mu}_{\mathbf{b}})$$

**Prior**



$$p(\mathbf{b}_k|\mathbf{b}_{k-1}) \propto \mathcal{N}(\mathbf{b}_k|\boldsymbol{\mu}_{\mathbf{b}}, \boldsymbol{\Sigma}_{\mathbf{b}})$$



$$\boldsymbol{\Sigma}_{\mathbf{b}} = \boldsymbol{\Lambda} + \boldsymbol{\Xi}$$

PCA eigenvalues +  
additive dynamic noise

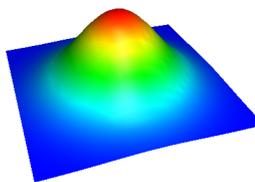
**Model the Covariance of  $\mathbf{b}$   
(2<sup>nd</sup> Order Estimate)**

Linear Dynamic System (LDS)

$$\mathbf{b}_k = \mathbf{A}\mathbf{b}_{k-1} + q \quad q \sim \mathcal{N}(\mathbf{0}, \boldsymbol{\Sigma}_{\mathbf{b}})$$

$$\Delta\mathbf{y} = \Phi\mathbf{b}_k + r \quad r \sim \mathcal{N}(\mathbf{0}, \boldsymbol{\Sigma}_{\mathbf{y}})$$

$$\mathcal{N}(\mathbf{A}\boldsymbol{\mu}_k^{\mathbf{F}}, \underbrace{(\boldsymbol{\Lambda} + \boldsymbol{\Xi}) + \mathbf{A}\boldsymbol{\Sigma}_{k-1}^{\mathbf{F}}\mathbf{A}^T}_{\mathbf{P}_{k-1}})$$

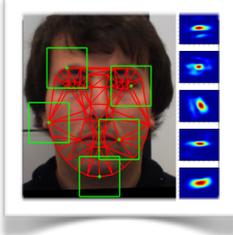


**Posterior**

$$p(\mathbf{b}_k|\mathbf{y}_k, \dots, \mathbf{y}_0) \propto \mathcal{N}(\mathbf{b}_k|\boldsymbol{\mu}_k^{\mathbf{F}}, \boldsymbol{\Sigma}_k^{\mathbf{F}})$$

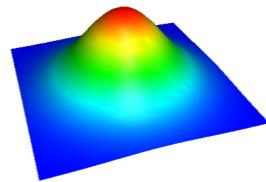
$$\boldsymbol{\mu}_k^{\mathbf{F}} = \mathbf{A}\boldsymbol{\mu}_{k-1}^{\mathbf{F}} + \mathbf{K}(\mathbf{y} - \Phi\mathbf{A}\boldsymbol{\mu}_{k-1}^{\mathbf{F}})$$

$$\boldsymbol{\Sigma}_k^{\mathbf{F}} = (\mathbf{I}_n - \mathbf{K}\Phi)\mathbf{P}_{k-1}$$



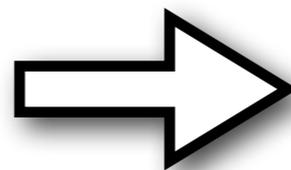
# MAP Global Alignment (BASM)

**Likelihood**

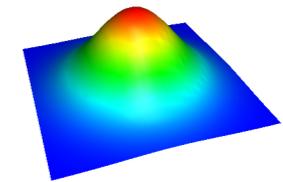


$$p(\mathbf{y}|\mathbf{b}) \propto \mathcal{N}(\Delta\mathbf{y}|\Phi\mathbf{b}, \Sigma_{\mathbf{y}})$$

- 2<sup>nd</sup> Order Estimate
- Bayesian Fusion of Multiple Detectors



**Posterior**

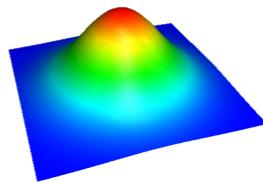


$$p(\mathbf{b}_k|\mathbf{y}_k, \dots, \mathbf{y}_0) \propto \mathcal{N}(\mathbf{b}_k|\boldsymbol{\mu}_k, \boldsymbol{\Sigma}_k)$$

$$\boldsymbol{\Sigma}_k = \left( (\boldsymbol{\Sigma}_{\mathbf{b}_k} + \boldsymbol{\Sigma}_{k-1})^{-1} + \Phi^T \sum_{m=1}^M (\boldsymbol{\Sigma}_{\mathbf{y}(m)}^{-1}) \Phi \right)^{-1}$$

$$\boldsymbol{\mu}_k = \boldsymbol{\Sigma}_k \left( \Phi^T \sum_{m=1}^M (\boldsymbol{\Sigma}_{\mathbf{y}(m)}^{-1} \Delta\mathbf{y}(m)) + (\boldsymbol{\Sigma}_{\mathbf{b}_k} + \boldsymbol{\Sigma}_{k-1})^{-1} \boldsymbol{\mu}_{\mathbf{b}_k} \right)$$

**Prior**



$$p(\mathbf{b}_k|\mathbf{b}_{k-1}) \propto \mathcal{N}(\mathbf{b}_k|\boldsymbol{\mu}_{\mathbf{b}}, \boldsymbol{\Sigma}_{\mathbf{b}})$$

**Unknown**

Observable vector  $\mathbf{b}$

$$p(\boldsymbol{\mu}_{\mathbf{b}}, \boldsymbol{\Sigma}_{\mathbf{b}}|\mathbf{b}) \propto p(\mathbf{b}|\boldsymbol{\mu}_{\mathbf{b}}, \boldsymbol{\Sigma}_{\mathbf{b}}) p(\boldsymbol{\mu}_{\mathbf{b}}, \boldsymbol{\Sigma}_{\mathbf{b}})$$

Joint Posterior

Normal Inverse-Wishart

Joint Prior

Normal Inverse-Wishart

**Conjugate Prior** for a Gaussian with unknown mean and covariance is a Normal Inverse-Wishart distribution

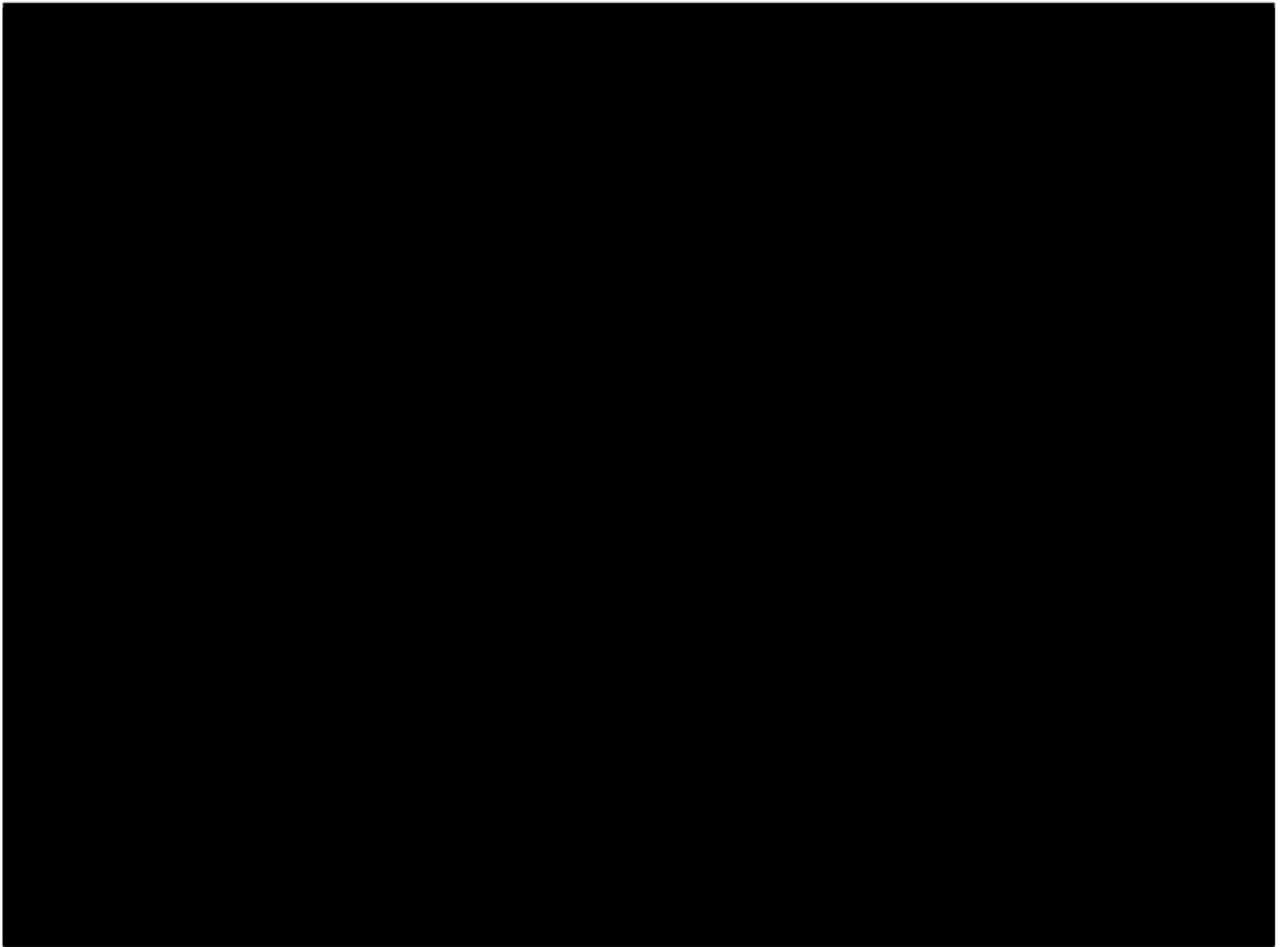
$$p(\boldsymbol{\mu}_{\mathbf{b}}|\mathbf{b}) \propto \text{Multivariate Student t}$$

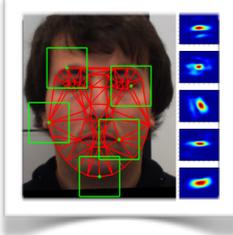
$$\boldsymbol{\mu}_{\mathbf{b}_k} = E(\boldsymbol{\mu}_{\mathbf{b}}|\mathbf{b}) = \boldsymbol{\theta}_k$$

$$p(\boldsymbol{\Sigma}_{\mathbf{b}}|\mathbf{b}) \propto \text{Inv-Wishart}$$

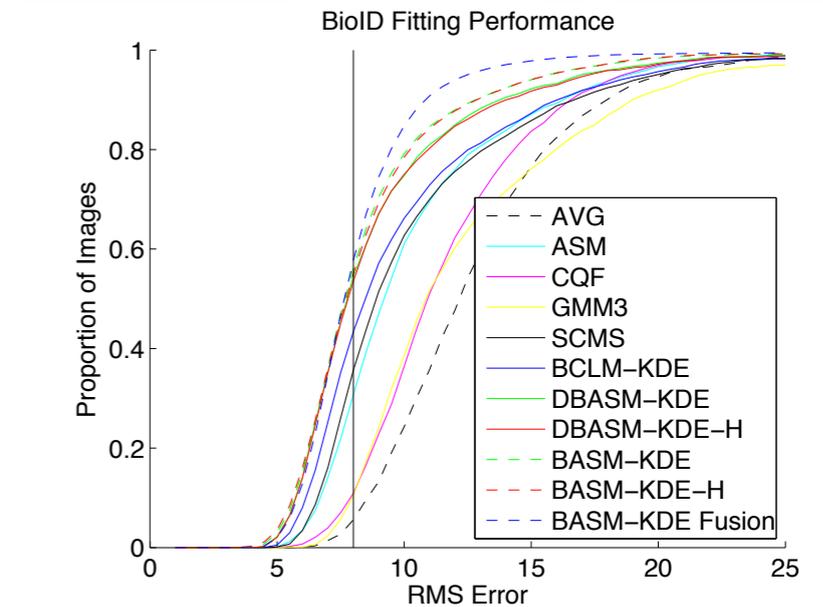
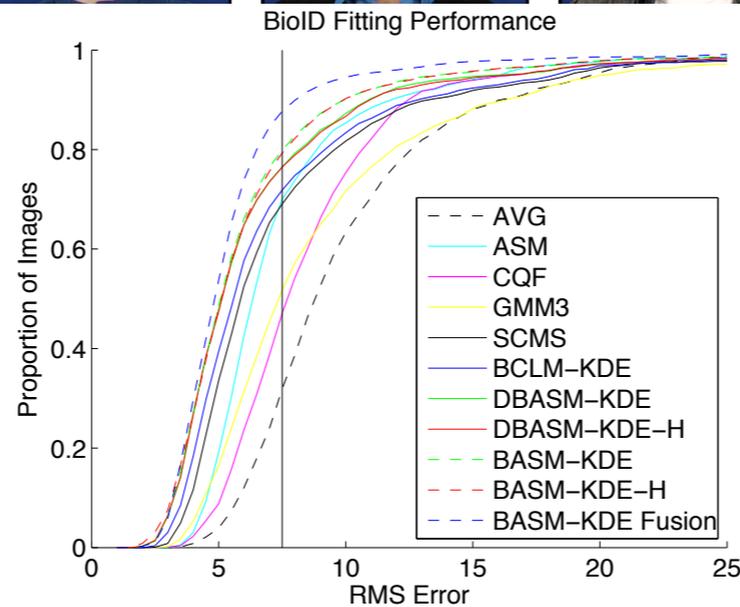
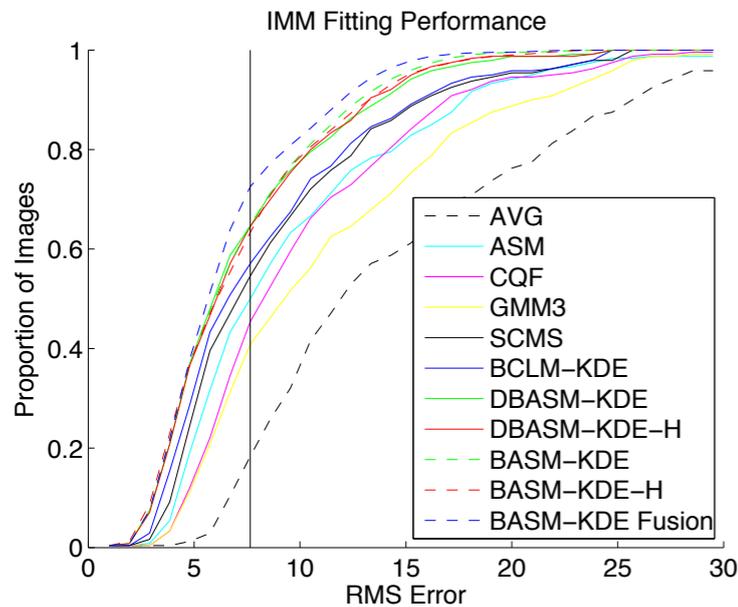
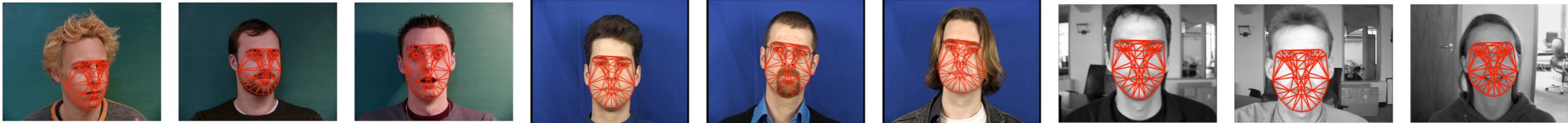
$$\boldsymbol{\Sigma}_{\mathbf{b}_k} = E(\boldsymbol{\Sigma}_{\mathbf{b}}|\mathbf{b}) = (v_k - n - 1)^{-1} \Lambda_k$$

The Prior distribution is **continuously kept up to date**

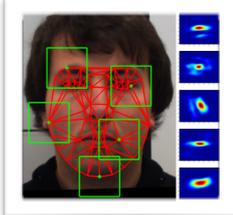




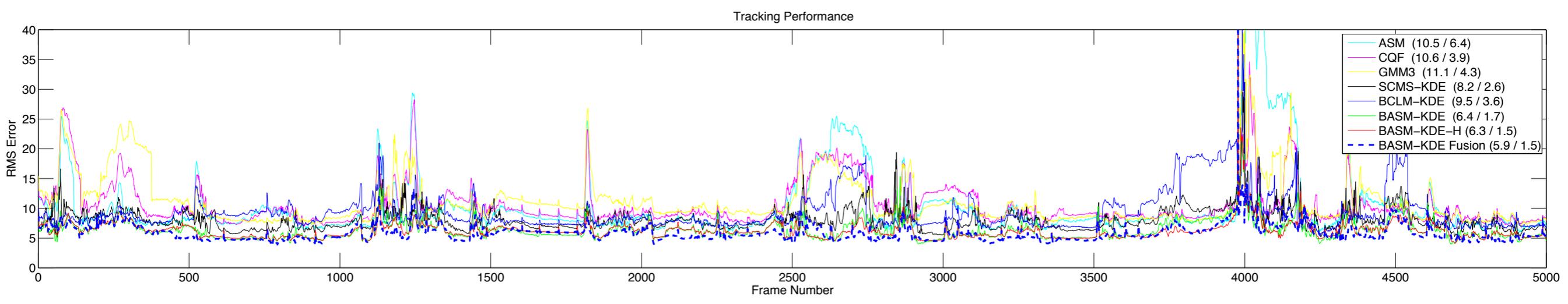
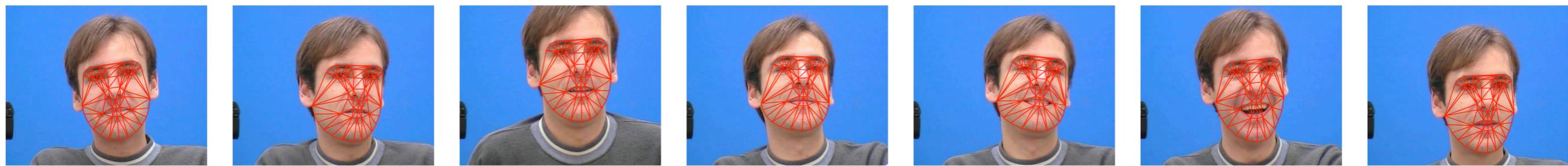
# Evaluation Results



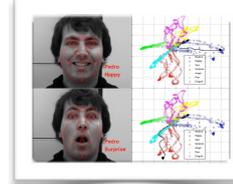
Reference 7.5 RMS	IMM (240 images)		XM2VTS (2360 images)		BioID (1521 images)	
ASM	50.0		30.7		70.0	
DBASM-WPR	56.7	(+6.7)	45.1	(+14.4)	75.4	(+5.4)
BASM-WPR	<b>58.4</b>	(+8.4)	<b>47.4</b>	(+16.7)	<b>77.1</b>	(+7.1)
CQF	45.4		10.9		47.0	
GMM3	40.8	(-4.6)	10.4	(-0.5)	51.7	(+4.7)
BCLM-GR	48.3	(+2.9)	15.9	(+5.0)	54.2	(+7.2)
DBASM-GR	50.4	(+5.0)	18.0	(+7.1)	62.2	(+15.2)
BASM-GR	<b>51.8</b>	(+6.4)	<b>19.7</b>	(+8.8)	<b>63.5</b>	(+16.5)
SCMS-KDE	54.6		35.7		69.0	
BCLM-KDE	57.1	(+2.5)	43.4	(+7.7)	71.9	(+2.9)
DBASM-KDE	64.6	(+10.0)	54.5	(+18.8)	76.5	(+7.5)
DBASM-KDE-H	64.6	(+10.0)	53.5	(+17.8)	76.5	(+7.5)
BASM-KDE	<b>65.4</b>	(+10.8)	<b>57.0</b>	(+21.3)	<b>80.3</b>	(+11.3)
BASM-KDE-H	64.0	(+9.4)	56.6	(+20.9)	79.9	(+10.9)
BASM-KDE Fusion of 2 Detectors	<b>72.5</b>	(+17.9)	<b>58.7</b>	(+23.0)	<b>88.2</b>	(+19.2)



# Tracking Performance - FGNET Talking Face

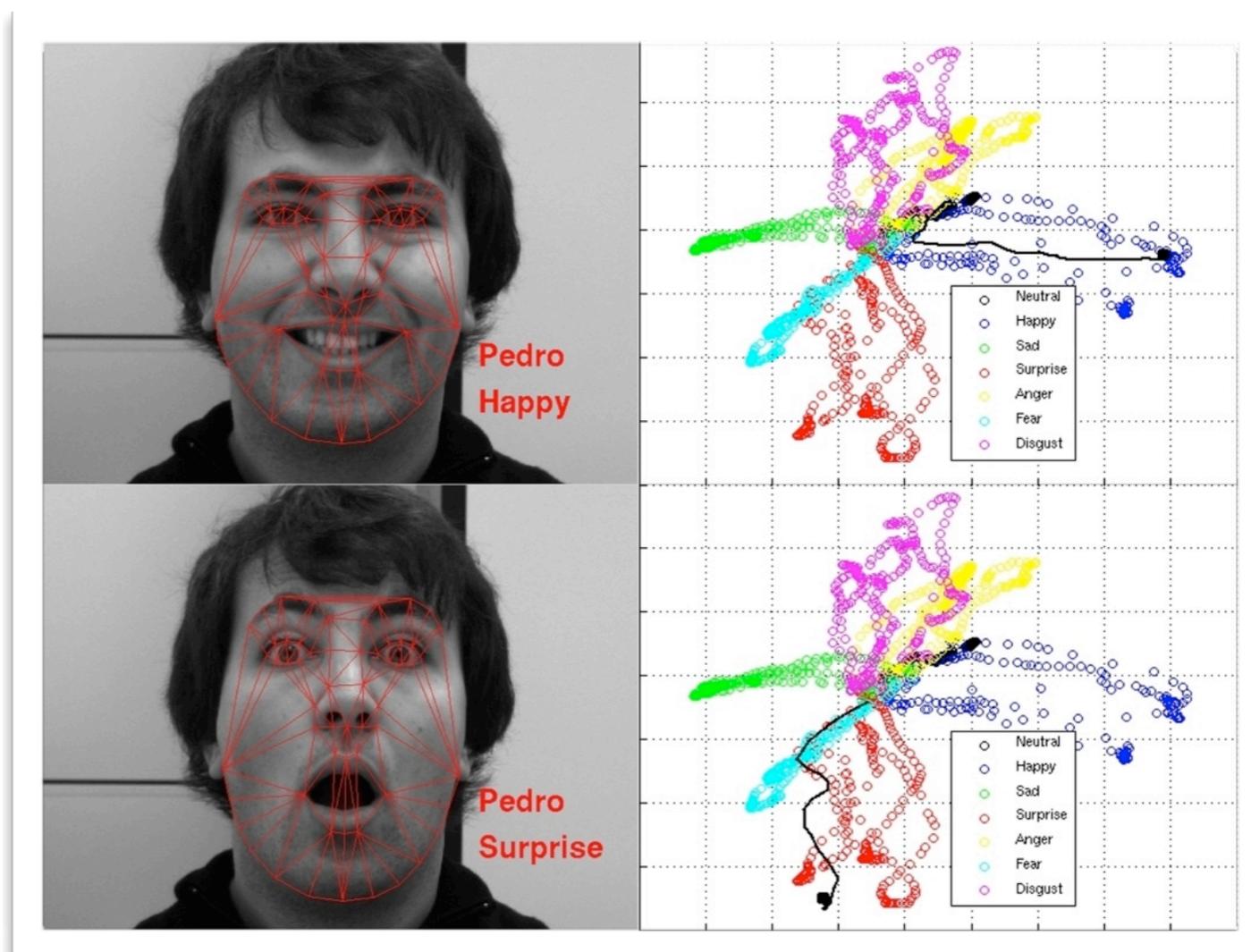


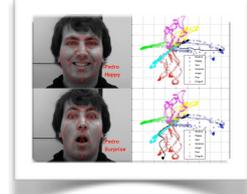
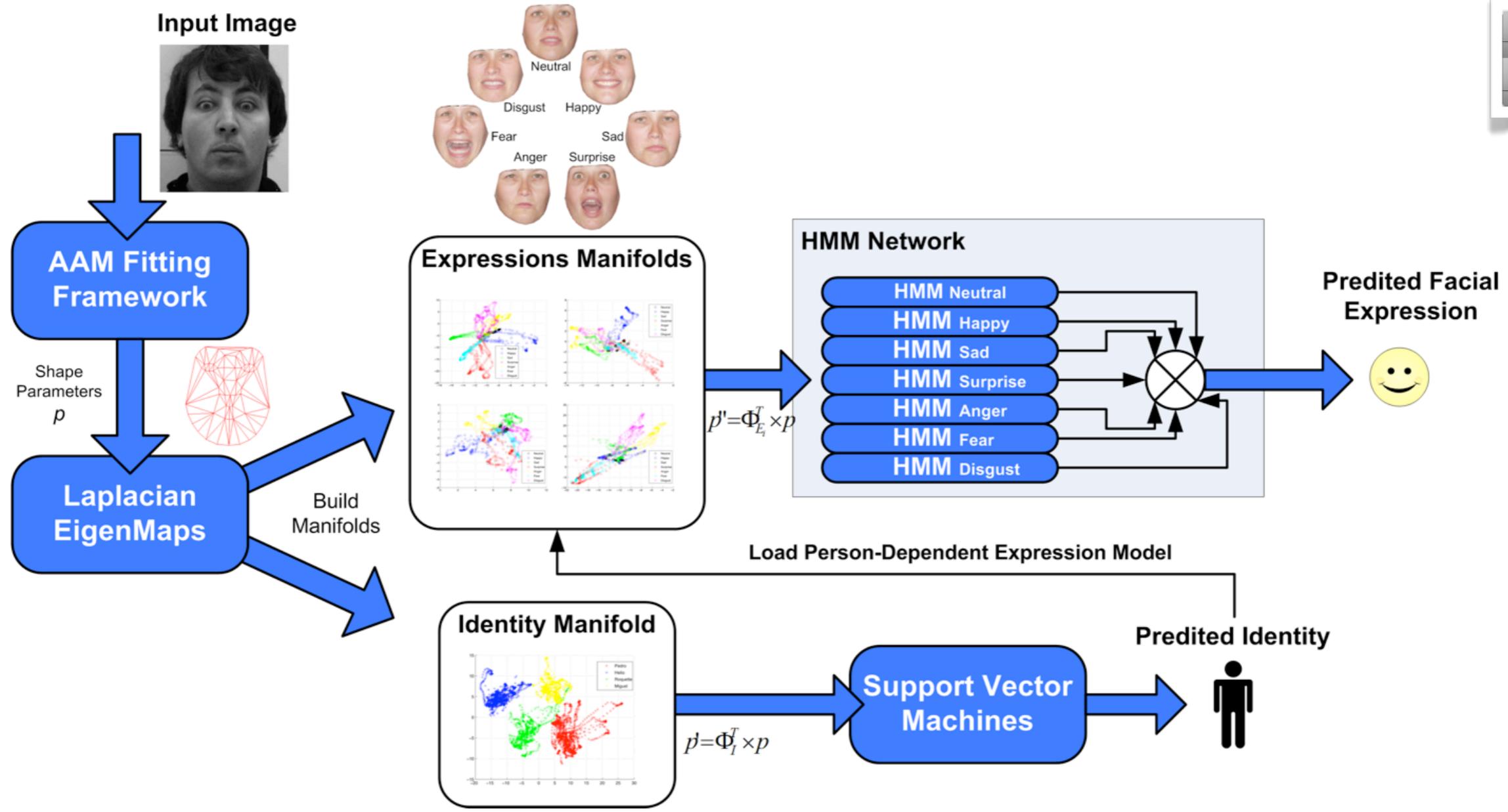
<b>RMS Error</b>	<b>ASM</b>	<b>CQF</b>	<b>GMM3</b>	<b>SCMS-KDE</b>	<b>BCLM-KDE</b>	<b>DBASM-KDE</b>	<b>DBASM-KDE-H</b>	<b>BASM-KDE</b>	<b>BASM-KDE-H</b>	<b>BASM-KDE Fusion</b>
<b>Mean</b>	10.5	10.6	11.1	8.2	9.5	7.0	7.2	6.4	6.3	5.9
<b>Standard Deviation</b>	6.4	3.9	4.3	2.6	3.6	2.1	2.2	1.7	1.5	1.5



# (3) Identity and Facial Expression Recognition

- Six basic emotions (happiness, sadness, surprise, anger, fear, disgust) plus the neutral expression.
- Identity and facial expression recognition using facial geometry (captured by the AAM).
- Low dimensional manifolds derived using Laplacian EigenMaps
  - Identity
  - Person-dependent expression
- Two step recognition approach.

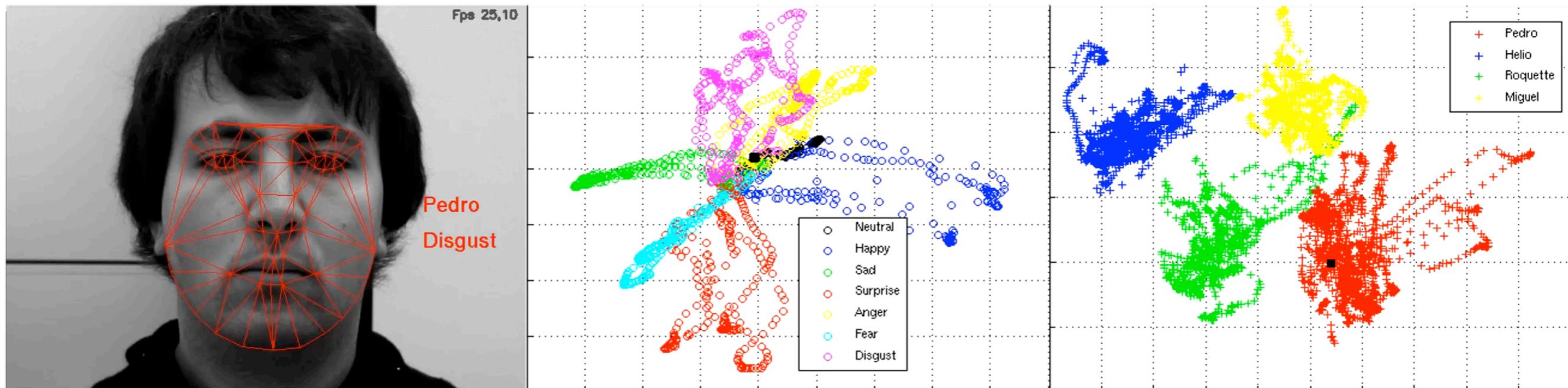




**Input (SIC Fitting)**

**Expression (HMM)**

**Identity (SVM)**



# Conclusions

---

- **(1) Generative Face Alignment (2.5D Active Appearance Models)**
  - Extension of the standard 2D Active Appearance Models to deal with a full perspective projection model.
  - Two model fitting algorithms (SFA, NFA) and their efficient approximations.
  - Robust solutions account for partial and self occlusions.
- **(2) Discriminative Face Alignment (Bayesian Active Shape Models)**
  - New Bayesian formulation for aligning faces in unseen images.
  - New global optimization strategy that infers both shape and pose parameters, in MAP sense, using second order statistics.
  - Extension that models the prior distribution.
- **(3) Identity and Facial Expression Recognition**
  - Two step recognition approach (identity then expression) using low dimensional representations of face geometry.

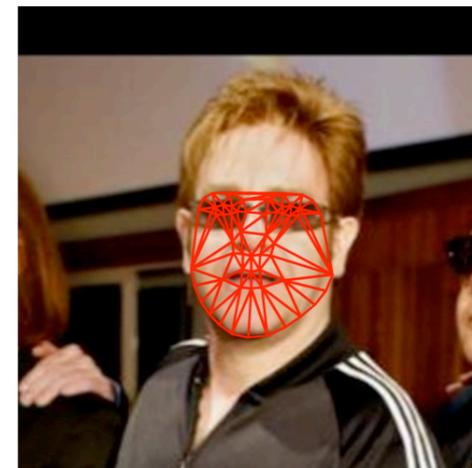
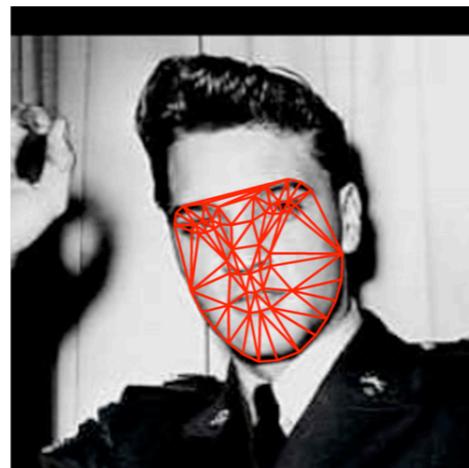
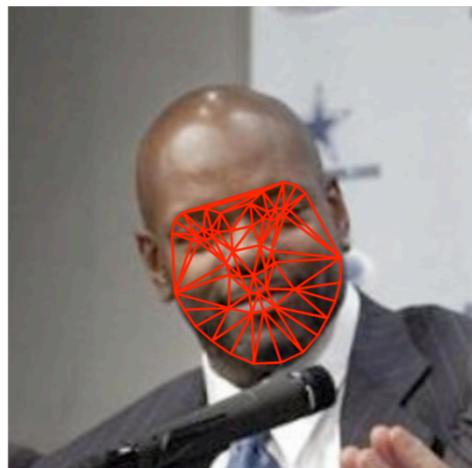
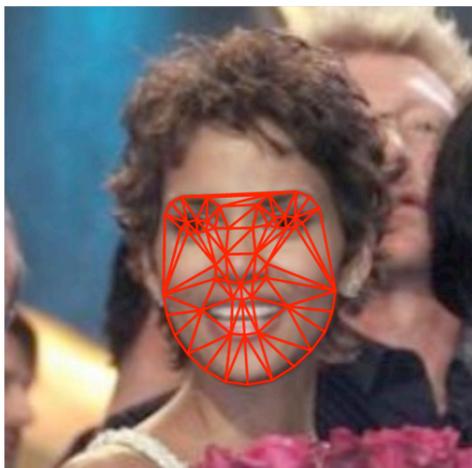
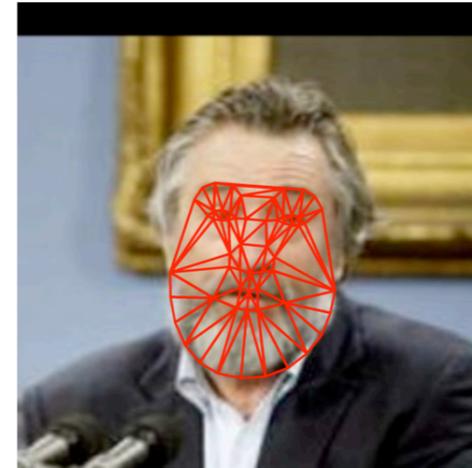
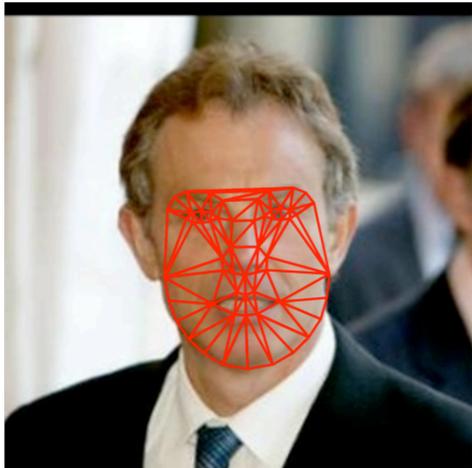
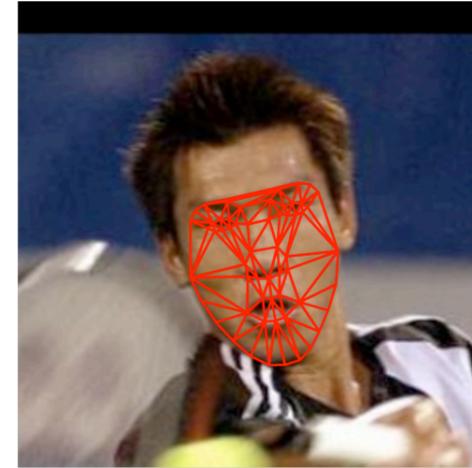
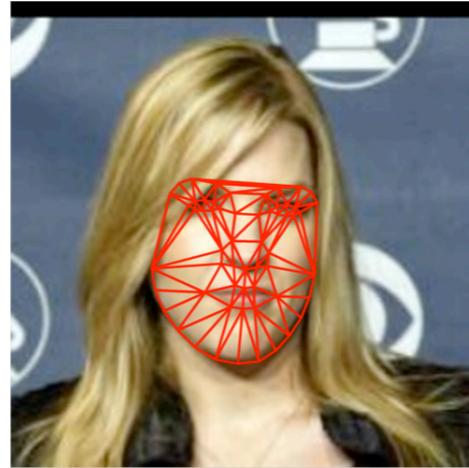
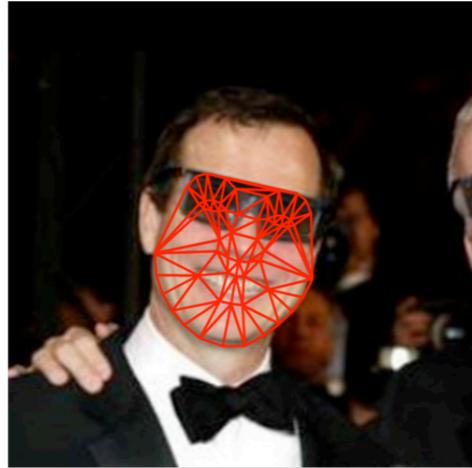
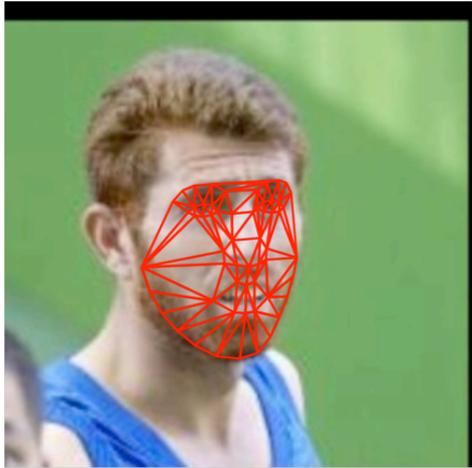
# Future Work

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- **Unconstrained Non-Rigid Registration**
  - 3D Point Distribution Model.
  - Extend the likelihood term to a non-parametric distribution.
  - Shape representation (non-parametric shape model).
  - Constrain model fitting using 3D depth data.
  - 3D dynamic recognition (identity and facial expression).

# The End

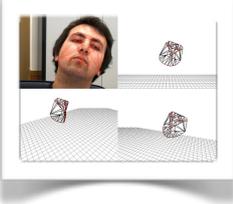
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# Additional Slides

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- Linear Pose Updates
- Efficient Approximations (ESFA, ENFA)
- Combined 2D+3D AAM
- MOSSE Filters
- KDE Landmark Updates
- BASM - The Algorithm
- Hierarchical Search (KDE-H)
- Tracking Performance - FGNET Talking Face (Video)
- The Recognition Approach (Overview)



# Linear Pose Updates

$$\mathbf{R}(\mathbf{w}, \theta) = e^{\hat{\mathbf{w}}\theta} = \sum_{n=0}^{\infty} \frac{(\hat{\mathbf{w}}\theta)^n}{n!} = \mathbf{I}_3 + \hat{\mathbf{w}}\theta + \frac{(\hat{\mathbf{w}}\theta)^2}{2!} + \frac{(\hat{\mathbf{w}}\theta)^3}{3!} + \dots$$

$$\hat{\mathbf{w}} = \begin{bmatrix} 0 & -w_z & w_y \\ w_z & 0 & -w_x \\ -w_y & w_x & 0 \end{bmatrix}$$

$$\mathbf{P}'_i = \underbrace{\begin{bmatrix} 1 & -w_z & w_y \\ w_z & 1 & -w_x \\ -w_z & w_x & 1 \end{bmatrix}}_{\mathbf{R}(\mathbf{w})} \underbrace{\begin{bmatrix} X_i \\ Y_i \\ Z_i \end{bmatrix}}_{\mathbf{P}_i} + \underbrace{\begin{bmatrix} t_x \\ t_y \\ t_z \end{bmatrix}}_{\mathbf{T}_i}$$

## Pose Parameters

$$\mathbf{q} = [w_x \ w_y \ w_z \ t_x \ t_y \ t_z]^T$$

$$\mathbf{P}'_i = \begin{bmatrix} 0 & Z_i & -Y_i & 1 & 0 & 0 \\ -Z_i & 0 & X_i & 0 & 1 & 0 \\ Y_i & -X_i & 0 & 0 & 0 & 1 \end{bmatrix} \mathbf{q}$$

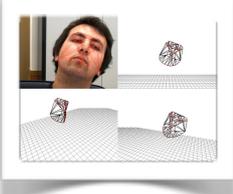
$$\sum_{j=1}^6 q_j \psi_j^{(t)}$$

$$\begin{bmatrix} 0 & s_0^{z_1} & -s_0^{y_1} & 1 & 0 & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ 0 & s_0^{z_v} & -s_0^{y_v} & 1 & 0 & 0 \\ \hline -s_0^{z_1} & 0 & s_0^{x_1} & 0 & 1 & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ -s_0^{z_v} & 0 & s_0^{x_v} & 0 & 1 & 0 \\ \hline s_0^{y_1} & -s_0^{x_1} & 0 & 0 & 0 & 1 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ s_0^{y_v} & -s_0^{x_v} & 0 & 0 & 0 & 1 \end{bmatrix} \mathbf{q}$$

$\psi_1, \dots, \psi_6$

$$\begin{bmatrix} 0 & s_0^{z_1} + s_\psi^{z_1} & -s_0^{y_1} - s_\psi^{y_1} & 1 & 0 & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ 0 & s_0^{z_v} + s_\psi^{z_v} & -s_0^{y_v} - s_\psi^{y_v} & 1 & 0 & 0 \\ \hline -s_0^{z_1} - s_\psi^{z_1} & 0 & s_0^{x_1} + s_\psi^{x_1} & 0 & 1 & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ -s_0^{z_v} - s_\psi^{z_v} & 0 & s_0^{x_v} + s_\psi^{x_v} & 0 & 1 & 0 \\ \hline s_0^{y_1} + s_\psi^{y_1} & -s_0^{x_1} - s_\psi^{x_1} & 0 & 0 & 0 & 1 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ s_0^{y_v} + s_\psi^{y_v} & -s_0^{x_v} - s_\psi^{x_v} & 0 & 0 & 0 & 1 \end{bmatrix} \mathbf{q}$$

$$s_\psi = \int_0^{t-1} \sum_{j=1}^6 q_j \psi_j^{(t)} \partial t$$



# Efficient Approximations (ESFA, ENFA)



$$\mathbf{A}_0(\mathbf{x}_p) + \sum_{i=1}^{m+2} \lambda_i \mathbf{A}_i(\mathbf{x}_p)$$

$$\left( \mathbf{A}_0(\mathbf{x}_p) + \sum_{i=1}^{m+2} \lambda_i \mathbf{A}_i(\mathbf{x}_p) \right) \approx \mathbf{I}(\mathbf{W}(\mathbf{x}_p, \mathbf{p}, \mathbf{q}))$$



$$\underbrace{\left( \underbrace{\nabla \mathbf{A}_0(\mathbf{x}_p)}_{\text{blue}} + \sum_{i=1}^{m+2} \lambda_i \nabla \mathbf{A}_i(\mathbf{x}_p) \right)}_{\nabla \mathbf{A}_i(\mathbf{x}_p, \lambda)} \approx \nabla \mathbf{I}(\mathbf{W}(\mathbf{x}_p, \mathbf{p}, \mathbf{q}))$$



$$\mathbf{I}(\mathbf{W}(\mathbf{x}_p, \mathbf{p}, \mathbf{q}))$$

$$\mathbf{SD}(\mathbf{x}_p)_{\text{enfa}} = \left[ \underbrace{\nabla \mathbf{A}_0(\mathbf{x}_p)}_{\text{blue}} \frac{\partial \mathbf{W}}{\partial \mathbf{p}_1} \dots \underbrace{\nabla \mathbf{A}_0(\mathbf{x}_p)}_{\text{blue}} \frac{\partial \mathbf{W}}{\partial \mathbf{p}_n} \underbrace{\nabla \mathbf{A}_0(\mathbf{x}_p)}_{\text{blue}} \frac{\partial \mathbf{W}}{\partial \mathbf{q}_1} \dots \underbrace{\nabla \mathbf{A}_0(\mathbf{x}_p)}_{\text{blue}} \frac{\partial \mathbf{W}}{\partial \mathbf{q}_6} \right]$$

$$\mathbf{SD}(\mathbf{x}_p)_{\text{esfa}} = \left[ \underbrace{\nabla \mathbf{A}_i(\mathbf{x}_p, \lambda)}_{\text{red}} \frac{\partial \mathbf{W}}{\partial \mathbf{p}_1} \dots \underbrace{\nabla \mathbf{A}_i(\mathbf{x}_p, \lambda)}_{\text{red}} \frac{\partial \mathbf{W}}{\partial \mathbf{p}_n} \underbrace{\nabla \mathbf{A}_i(\mathbf{x}_p, \lambda)}_{\text{red}} \frac{\partial \mathbf{W}}{\partial \mathbf{q}_1} \dots \underbrace{\nabla \mathbf{A}_i(\mathbf{x}_p, \lambda)}_{\text{red}} \frac{\partial \mathbf{W}}{\partial \mathbf{q}_6} - \mathbf{A}_1(\mathbf{x}_p) \dots - \mathbf{A}_{m+2}(\mathbf{x}_p) \right]$$

# Combined 2D+3D AAMs

---

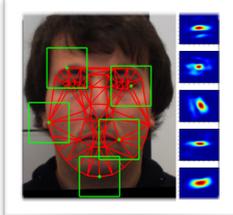
$$\sum_{\mathbf{x} \in \mathbf{s}_0} \left[ \mathbf{A}_0(\mathbf{x}) + \sum_{i=1}^m \lambda_i \mathbf{A}_i(\mathbf{x}) - \mathbf{I}(\mathcal{S}(\mathbf{W}(\mathbf{x}, \mathbf{p}), \mathbf{q})) \right]^2 +$$

$$K. \left\| \mathbf{P}(\mathbf{s}_0^{3d} + \sum_{i=1}^{n3D} p_i^{3d} \phi_i^{3d}) + \begin{pmatrix} o_x & \cdots & o_x \\ o_y & \cdots & o_y \end{pmatrix} - \mathcal{S}(s_0 + \sum_{i=1}^n p_i \phi_i, \mathbf{q}) \right\|^2$$

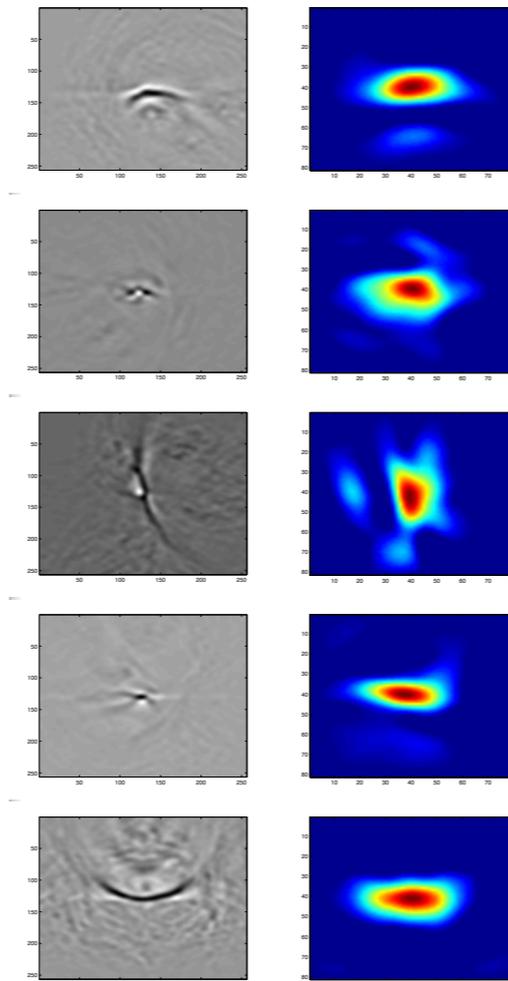
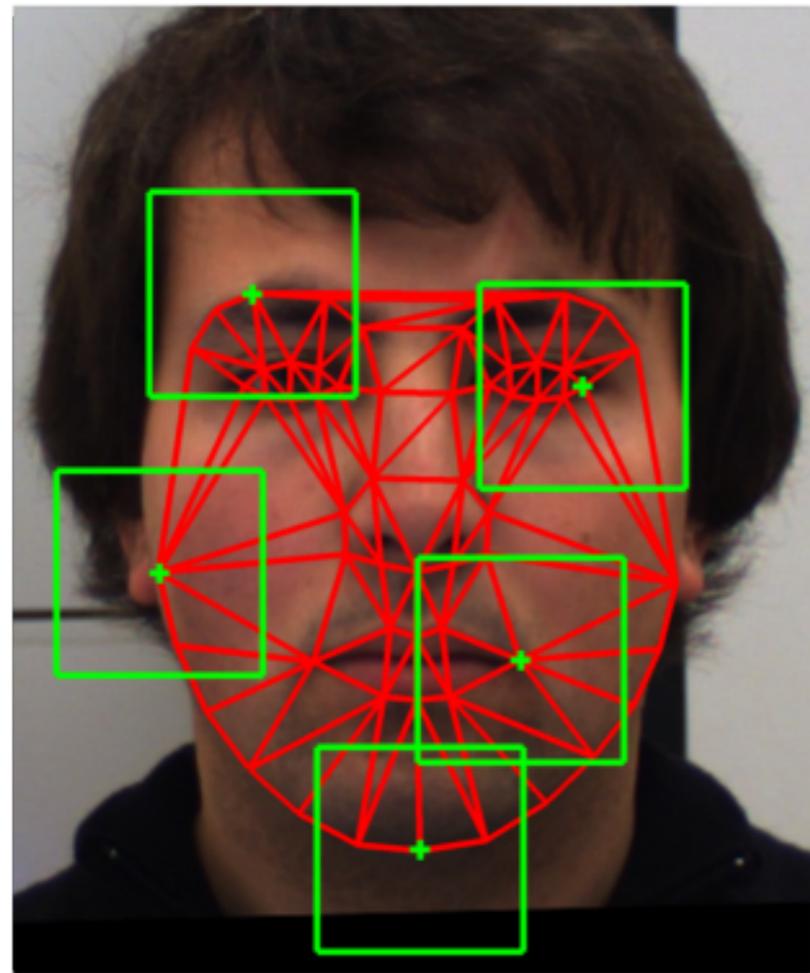
$$\mathbf{x} = \underbrace{\begin{pmatrix} i_x & i_y & i_z \\ j_x & j_y & j_z \end{pmatrix}}_{\mathbf{P}} \begin{pmatrix} X_i \\ Y_i \\ Z_i \end{pmatrix} + \begin{pmatrix} o_x \\ o_y \end{pmatrix}$$

$$\begin{pmatrix} \Delta \mathbf{p} \\ \Delta \mathbf{q} \\ \Delta \mathbf{p}^{3d} \\ \Delta \mathbf{P} \\ \Delta o_x \\ \Delta o_y \end{pmatrix} = -\mathbf{H}_{3D}^{-1} \begin{pmatrix} \Delta \mathbf{p}_{SD} \\ \Delta \mathbf{q}_{SD} \\ \mathbf{0} \\ \mathbf{0} \\ \mathbf{0} \\ \mathbf{0} \end{pmatrix} + K. \mathbf{SD}_F^T F(\mathbf{p}, \mathbf{q}, \mathbf{p}^{3D}, \mathbf{P}, o_x, o_y)$$

$$\mathbf{SD}_F = \begin{pmatrix} \frac{\partial F}{\partial \mathbf{p}} \mathbf{J}_{\mathbf{p}} & \frac{\partial F}{\partial \mathbf{q}} \mathbf{J}_{\mathbf{q}} & \frac{\partial F}{\partial \mathbf{p}^{3d}} & \frac{\partial F}{\partial \sigma} & \frac{\partial F}{\partial \Delta \theta_x} & \frac{\partial F}{\partial \Delta \theta_y} & \frac{\partial F}{\partial \Delta \theta_z} & \frac{\partial F}{\partial \Delta o_x} & \frac{\partial F}{\partial \Delta o_y} \end{pmatrix}$$

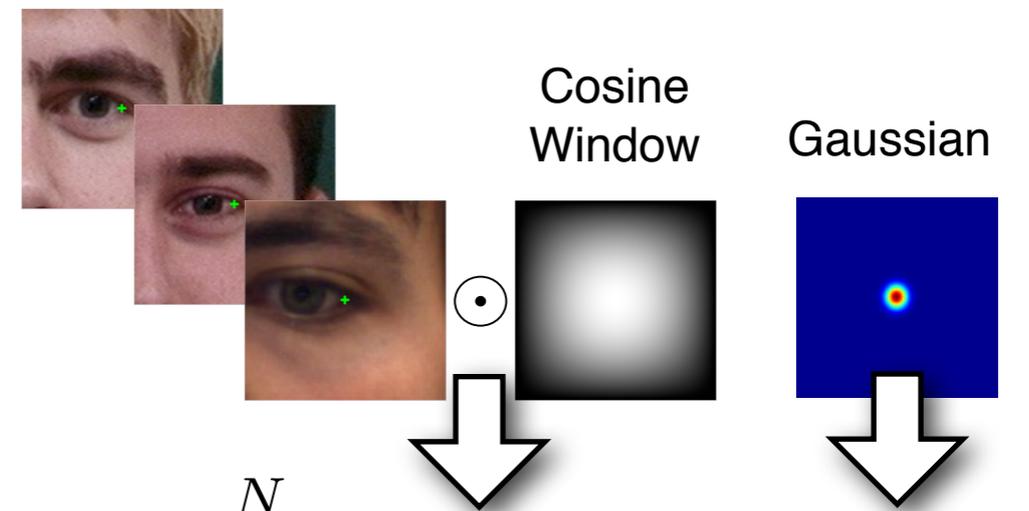


# Local Landmark Detectors - MOSSE Filters



- Correlation in Fourier Domain

$$\mathbf{G} = \mathcal{F}\{\mathbf{I}\} \odot \mathbf{H}^*$$



$$\min_{\mathbf{H}^*} \sum_{j=1}^N (\mathcal{F}\{\mathbf{I}_j\} \odot \mathbf{H}^* - \mathbf{G}_j)^2$$

## MOSSE Filter

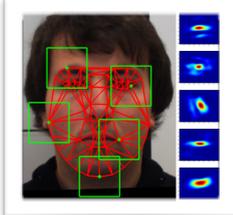
$$\mathbf{H}^* = \frac{\sum_{j=1}^N \mathbf{G}_j \odot \mathcal{F}\{\mathbf{I}_j\}^*}{\sum_{j=1}^N \mathcal{F}\{\mathbf{I}_j\} \odot \mathcal{F}\{\mathbf{I}_j\}^*}$$

$$\mathcal{F}^{-1}\{\mathbf{H}_i^*\} \mathcal{D}_i^{\text{MOSSE}}(\mathbf{I}(\mathbf{y}_i))$$

$$\mathcal{D}_i^{\text{MOSSE}}(\mathbf{I}(\mathbf{y}_i)) = \mathcal{F}^{-1}\{\mathcal{F}\{\mathbf{I}(\mathbf{y}_i)\} \odot \mathbf{H}_i^*\}$$

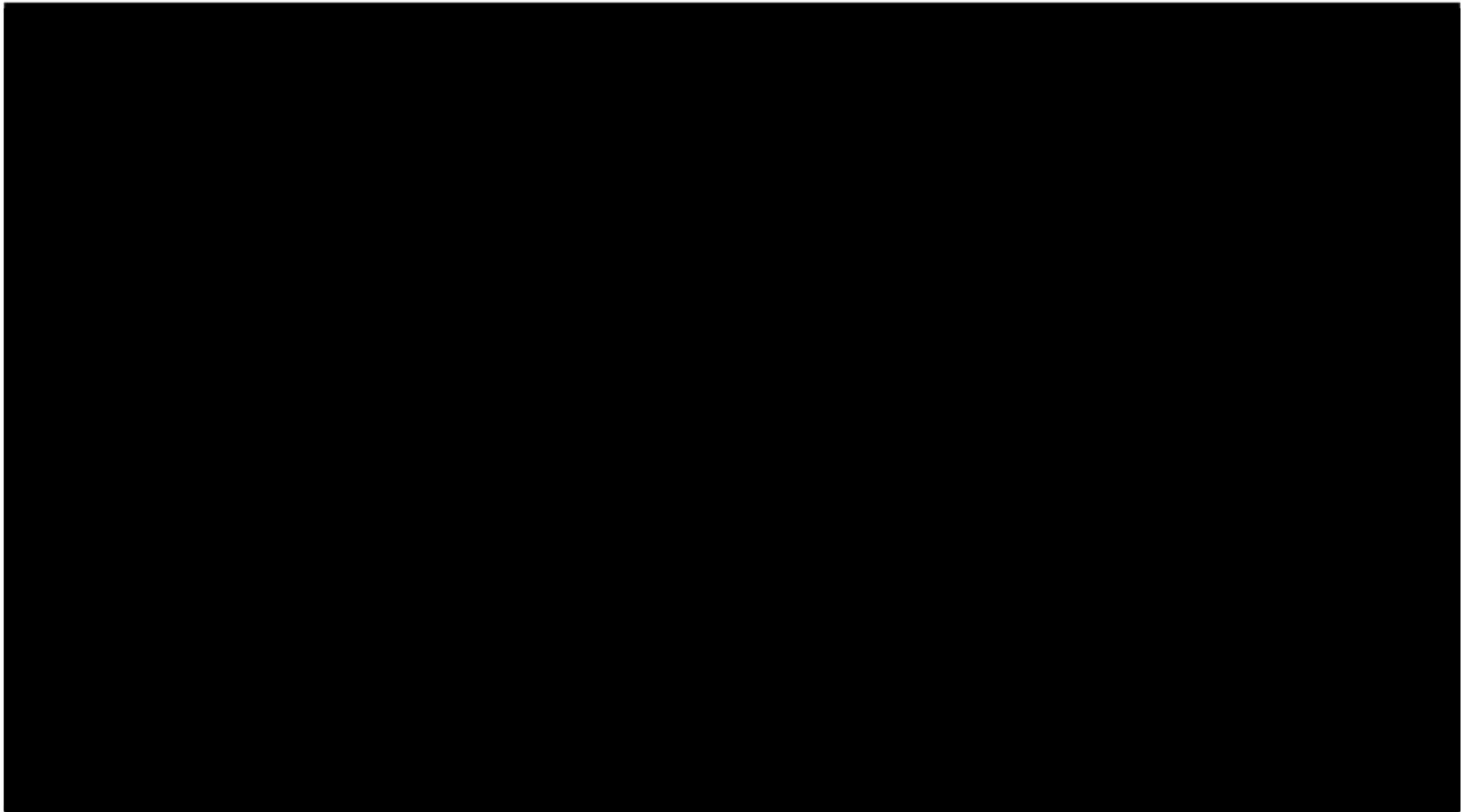
- Visual object tracking using adaptive correlation filters

D.Bolme, J.Beveridge, B.Draper, Y.Lui, CVPR 2010



# KDE Landmark Updates

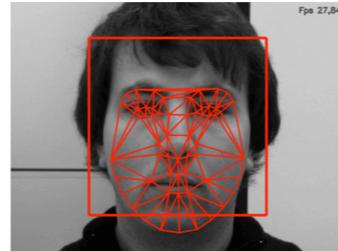
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# BASM - The Algorithm

**Precompute:** PDM:  $\mathbf{s}_0, \Phi, \Psi, \Lambda = \text{diag}(\lambda_1, \dots, \lambda_n)$

Initial estimate  $(\mathbf{b}_0, \Sigma_0), (\mathbf{q}_0, \Sigma_0^q)$

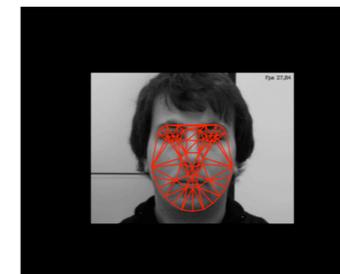


MOSSE Filters:  $\mathbf{H}_i^* \quad i=1, \dots, v$

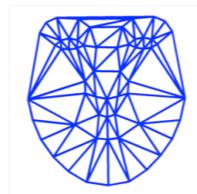


for k=1:1:MaxIterations

Warp Image to the base mesh, using the current pose parameters



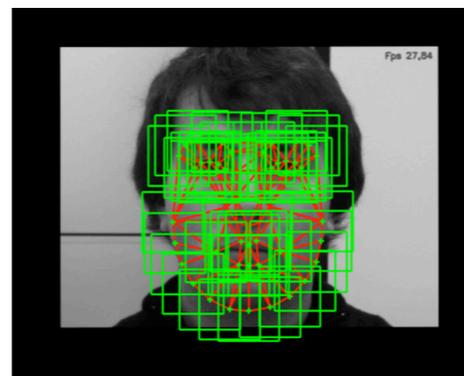
Generate current shape  $\mathbf{s} = \mathcal{S}(\mathbf{s}_0 + \Phi \mathbf{b}_k; \mathbf{q}_k)$



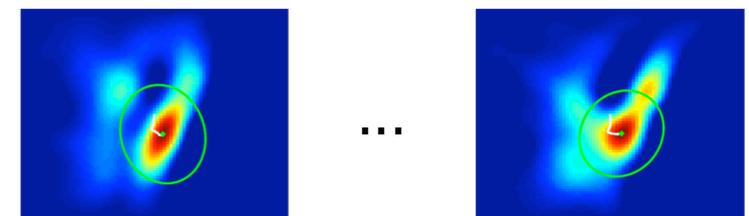
for i=1:1:Landmarks

Evaluate detectors response

Find the likelihood parameters  $\mathbf{y}_i, \Sigma_{\mathbf{y}_i}$



WPR, GR or KDE Local Strategy



end

Estimate the shape/pose parameters:

Update the parameters of Normal Inv-Wishart distribution  $\rightarrow v_k, \kappa_k, \theta_k, \Lambda_k$

Expectation of the prior shape parameters  $\longrightarrow \mu_{\mathbf{b}_k} = \theta_k, \quad \Sigma_{\mathbf{b}_k} = (v_k - n - 1)^{-1} \Lambda_k$

Evaluate the **global** shape parameters and the covariance  $\rightarrow \mu_k, \Sigma_k$

end

# Hierarchical Search (KDE-H)

- When response maps are approximated by KDE representations.

Mean-Shift Landmark Update

$$\mathbf{y}_i^{\text{KDE}(\tau+1)} \leftarrow \frac{\sum_{\mathbf{z}_i \in \Omega_{\mathbf{y}_i^c}} \mathbf{z}_i p_i(\mathbf{z}_i) \mathcal{N}(\mathbf{y}_i^{\text{KDE}(\tau)} | \mathbf{z}_i, \sigma_{h_j}^2 \mathbf{I}_2)}{\sum_{\mathbf{z}_i \in \Omega_{\mathbf{y}_i^c}} p_i(\mathbf{z}_i) \mathcal{N}(\mathbf{y}_i^{\text{KDE}(\tau)} | \mathbf{z}_i, \sigma_{h_j}^2 \mathbf{I}_2)}$$

Bandwidth schedule

$$\sigma_h^2 = (15, 10, 5, 2)$$

## Standard Search

```
for k=1:1:MaxIterations
```

```
  for i=1:1:v (LandMarks)
```

Evaluate de Detectors Response

Mean-Shift Landmark Update  $\sigma_h^2 = (15, 10, 5, 2)$

```
  end
```

Global Optimization

```
end
```

## Hierarchical Search

```
for k=1:1:MaxIterations
```

```
  for  $\sigma_h^2 = (15, 10, 5, 2)$ 
```

```
    for i=1:1:v (LandMarks)
```

Evaluate de Detectors Response

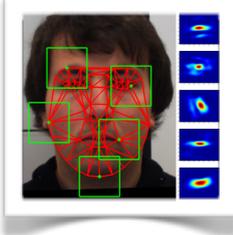
Mean-Shift Landmark Update  $\sigma_{h_j}^2$

```
    end
```

Global Optimization

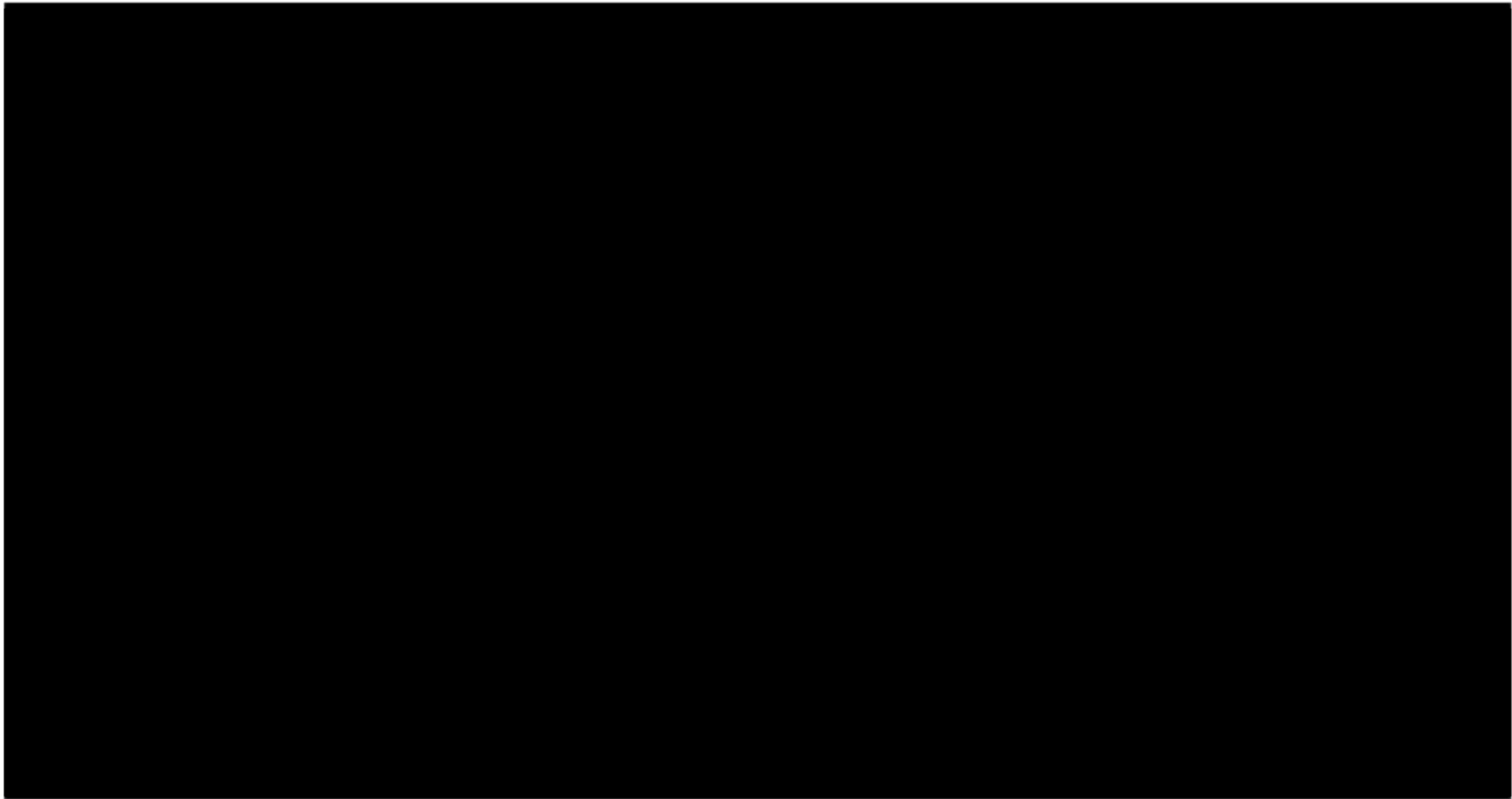
```
  end
```

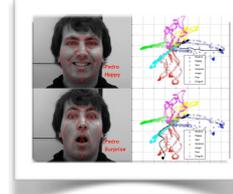
```
end
```



# Tracking Performance - FNET Talking Face

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# The Recognition Approach

