



Simultaneous Cascaded Regression

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Introduction

- Facial landmark localization with deformable models (nonrigid face alignment)
- Lucas & Kanade Image Alignment Framework
 - Simultaneous Forwards Additive / Inverse Compositional Algorithm
- Cascaded Regression Framework
- Simultaneous Algorithm: Cascaded Regression Extension
 - Regression w/ both shape and appearance structure

Outline

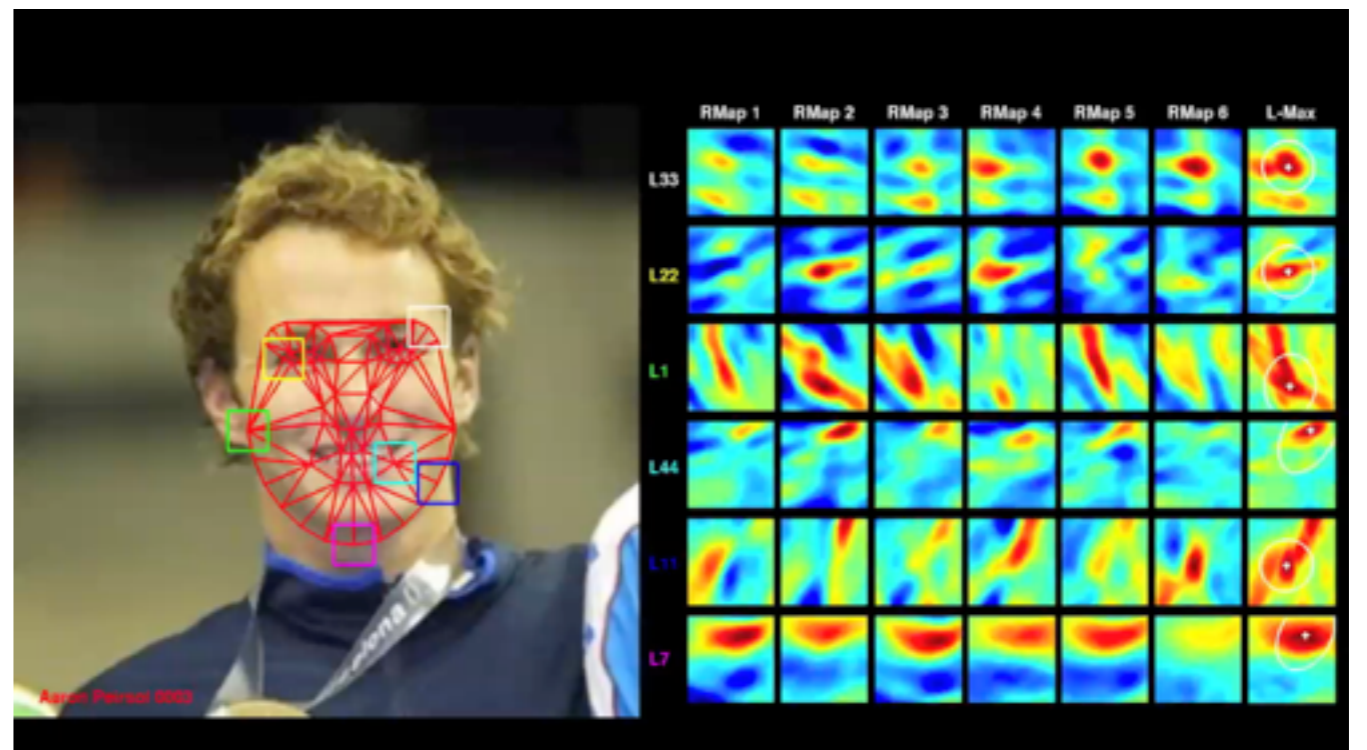
- Related Work
- Base Components
 - Warp Function
 - Parametric Models of Shape and Appearance
- Lucas & Kanade Image Alignment Framework
 - Simultaneous Forwards Additive (SFA)
 - Simultaneous Inverse Compositional (SIC)
- Simultaneous Cascaded Regression (SCR)
- Evaluation Results (LFPW, HELEN, LFW, 300W datasets)

Related Work

- Active Shape Model (ASM)
- Deformable Part Model (DPM)
- Active Appearance Model (AAM)
 - Project-Out Inverse Compositional (PO-IC)
 - Simultaneous Inverse Compositional (SIC)
- Constrained Local Model (CLM)
 - Convex Quadratic Fitting (CQF)
 - Subspace Constrained Mean-Shifts (SCMS)
 - Bayesian CLM (BCLM)
- Cascaded Regression (CR)
 - Supervised Descent Method (SDM)
 - Project-Out Cascade Regression (PO-CR)

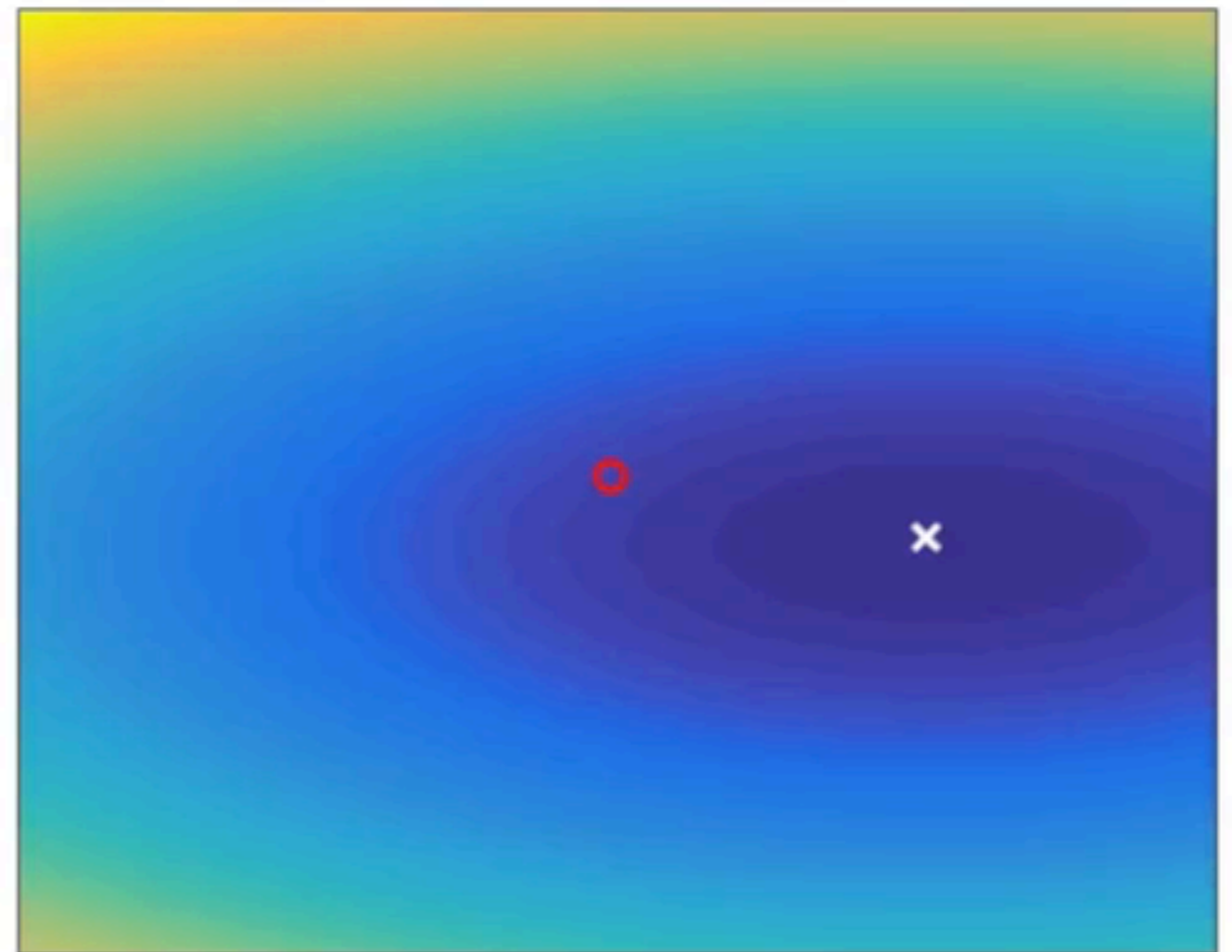
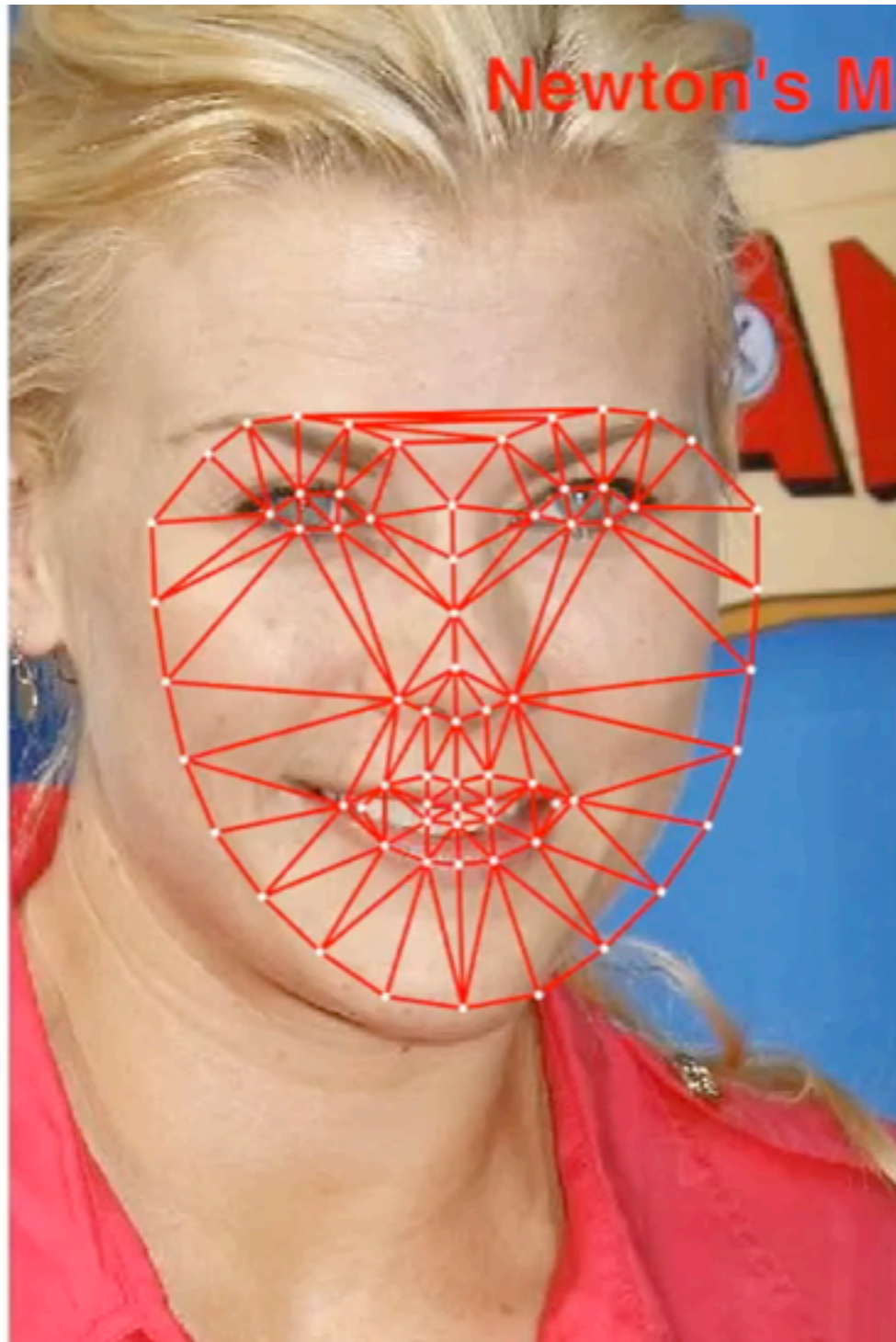


Active Appearance Model (AAM)



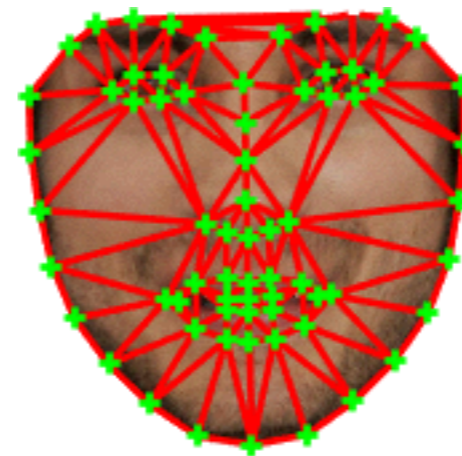
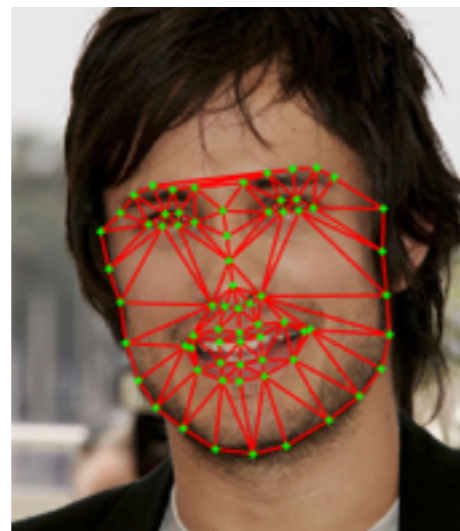
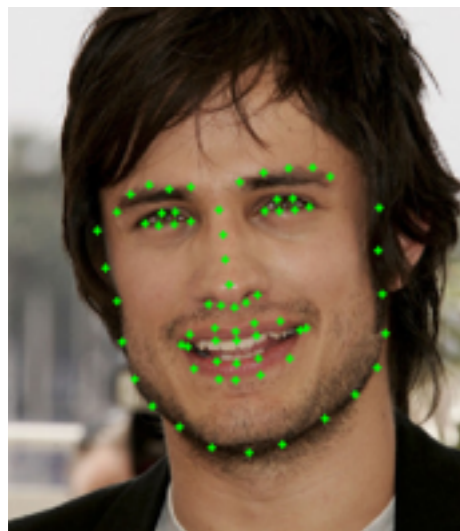
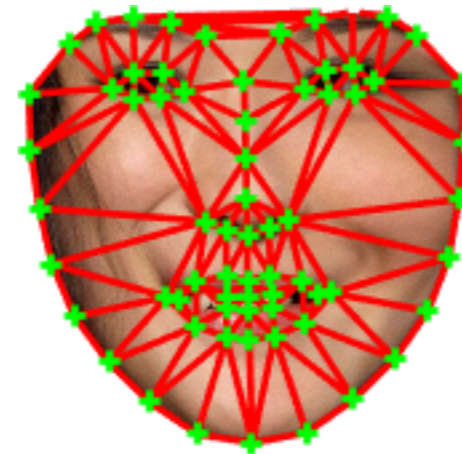
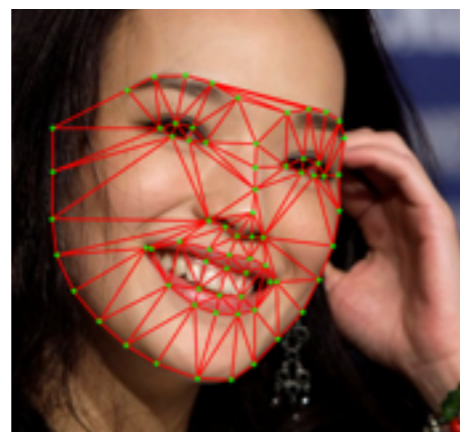
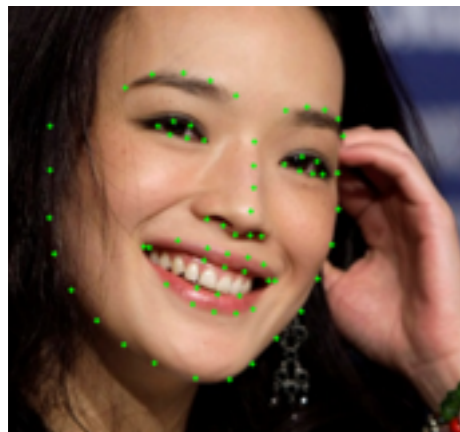
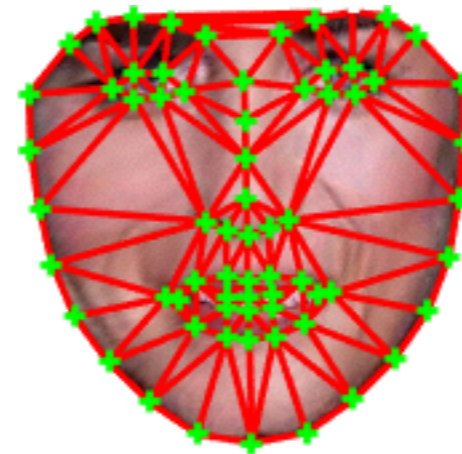
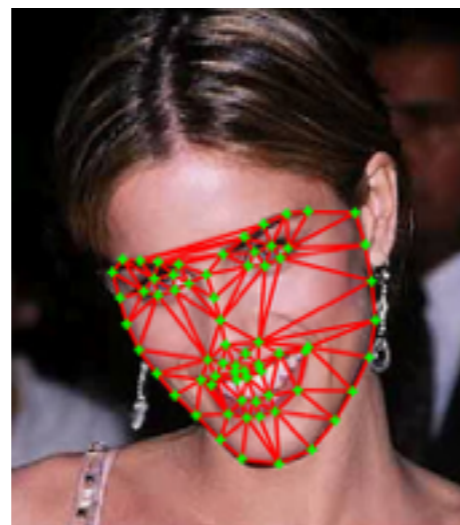
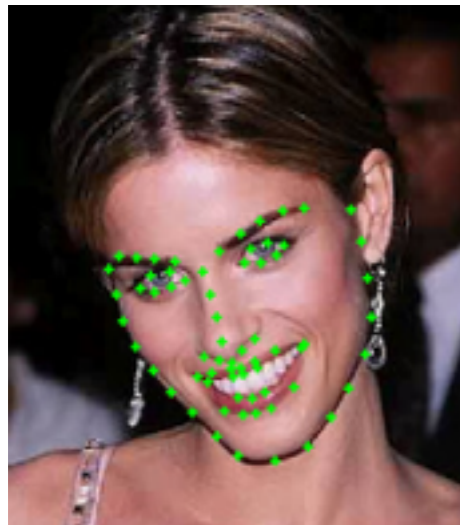
Bayesian Constrained Local Model (BCLM)

Newton Methods vs Cascaded Regression



Cost Function

Piecewise Affine Warp (@AAMs) [Not Used Here]



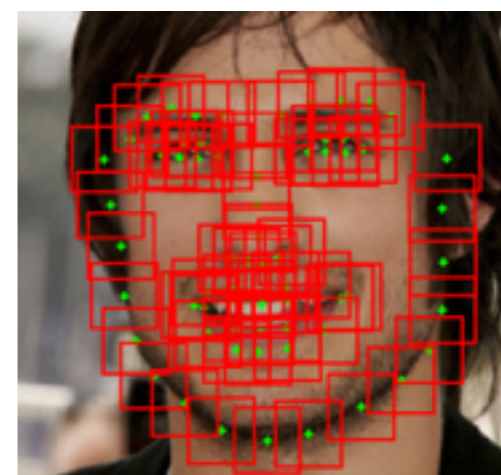
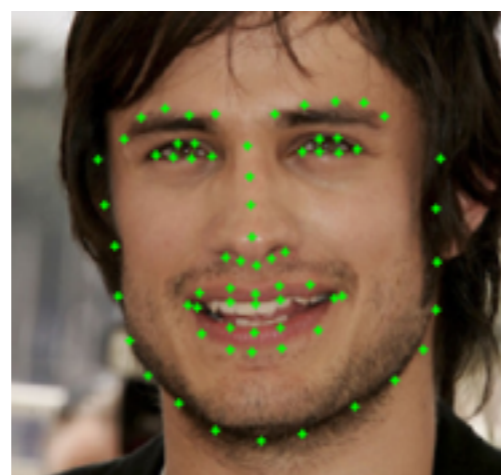
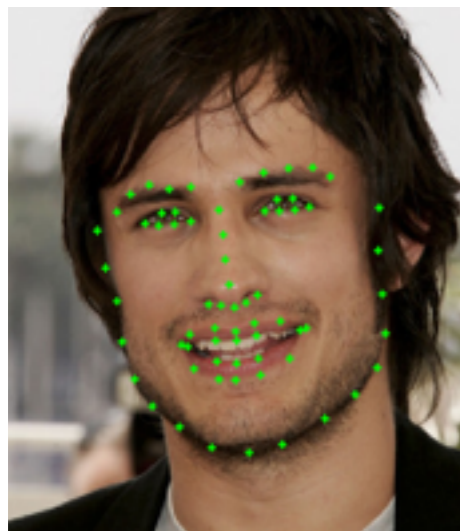
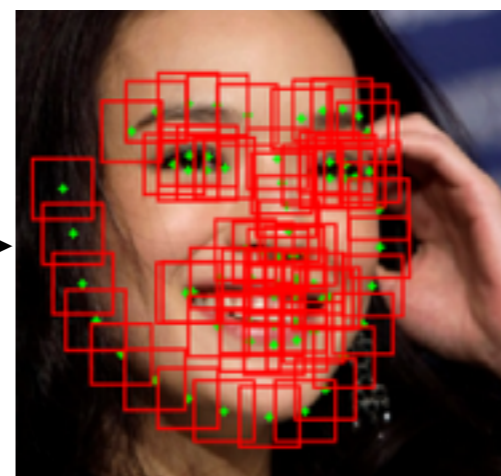
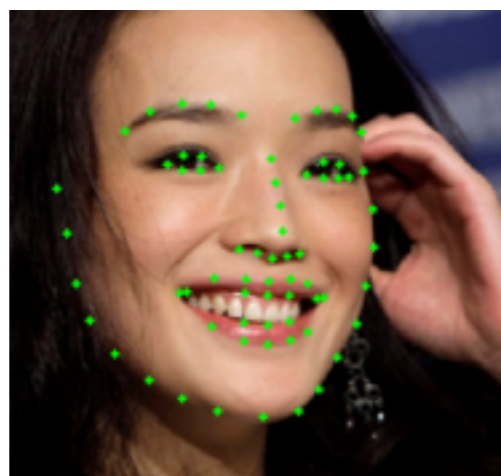
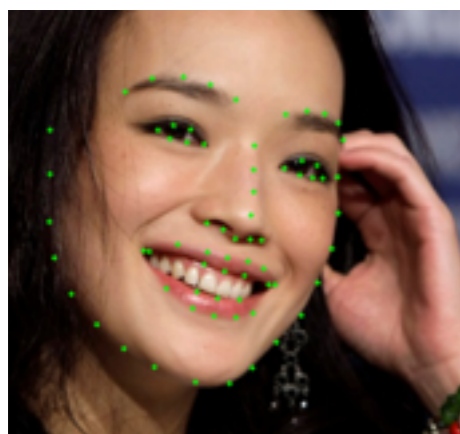
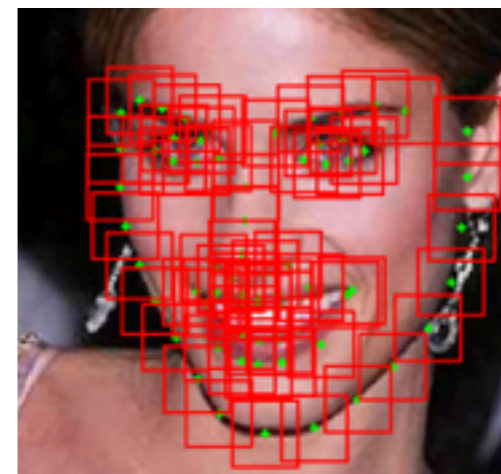
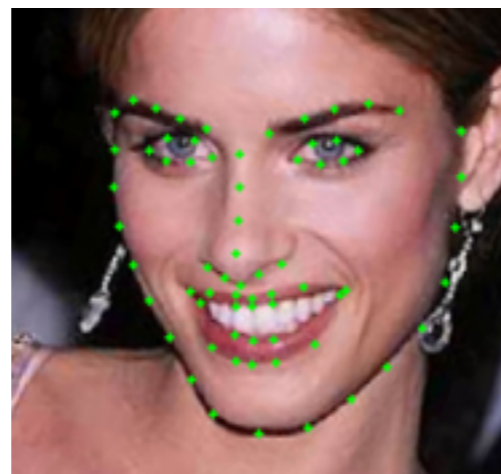
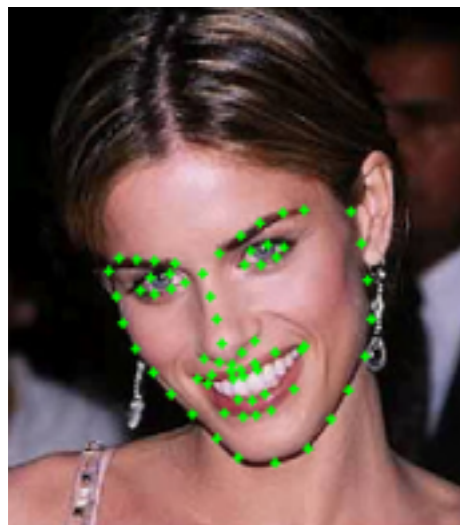
Landmarks

Delaunay Triangulation

Base Mesh

Warped Example

Patch based Local Warp



Landmarks

Similarity Warp (s, θ, t_x, t_y)

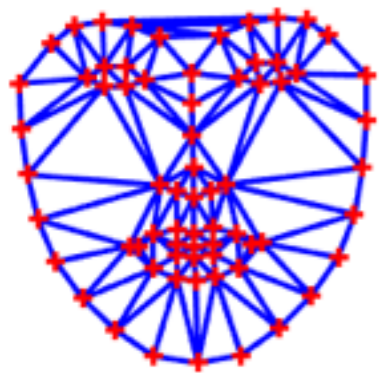
Local Patches

Local Extracted Features (HoG)

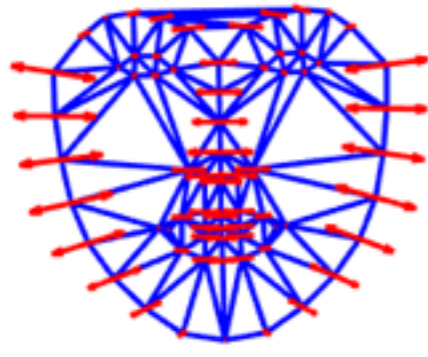
Parametric Shape and Appearance Models

$$\mathbf{s} = (x_1, \dots, x_v, y_1, \dots, y_v)^T \in \mathbb{R}^{2v}$$

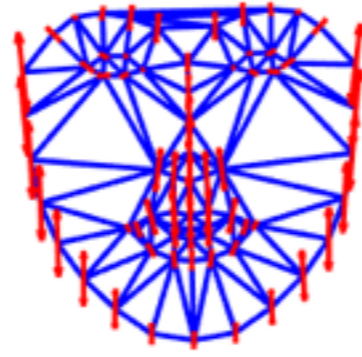
Shape Model



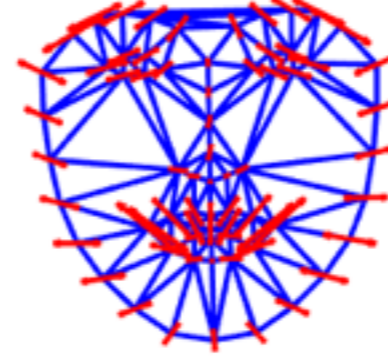
\mathbf{S}_0



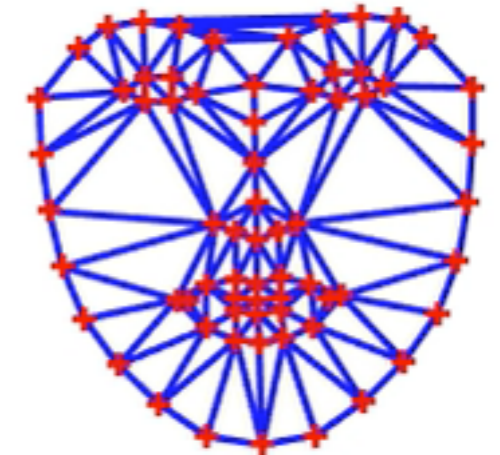
ϕ_1



ϕ_2



ϕ_3



$$\mathcal{W}(\mathbf{s}; \mathbf{p}) = \mathbf{s}_0 + \sum_{i=1}^{n+4} \phi_i p_i$$

Appearance Model



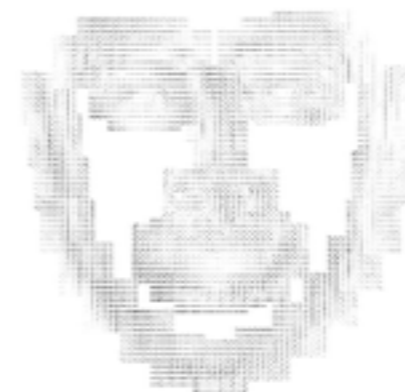
$\mathbf{A}_0(\mathbf{x})$



$-\mathbf{A}_1(\mathbf{x})$



$-\mathbf{A}_2(\mathbf{x})$



$-\mathbf{A}_3(\mathbf{x})$



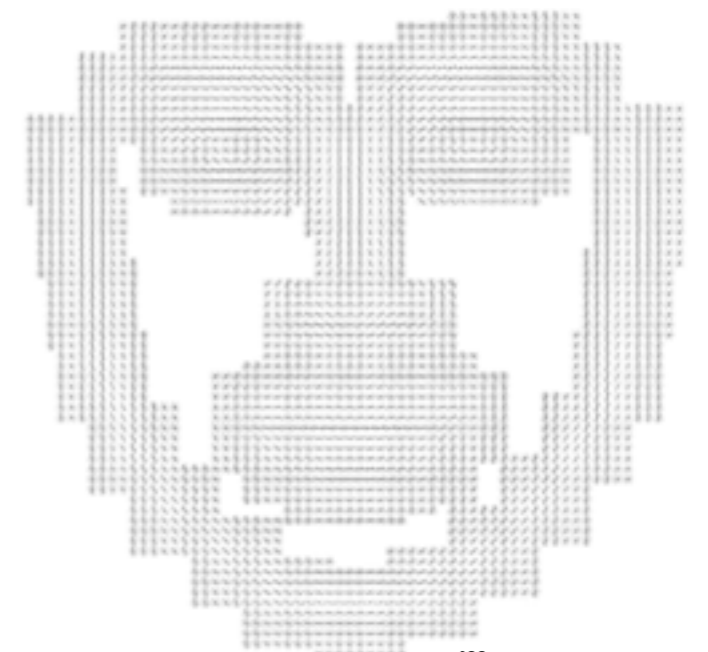
$+\mathbf{A}_1(\mathbf{x})$



$+\mathbf{A}_2(\mathbf{x})$



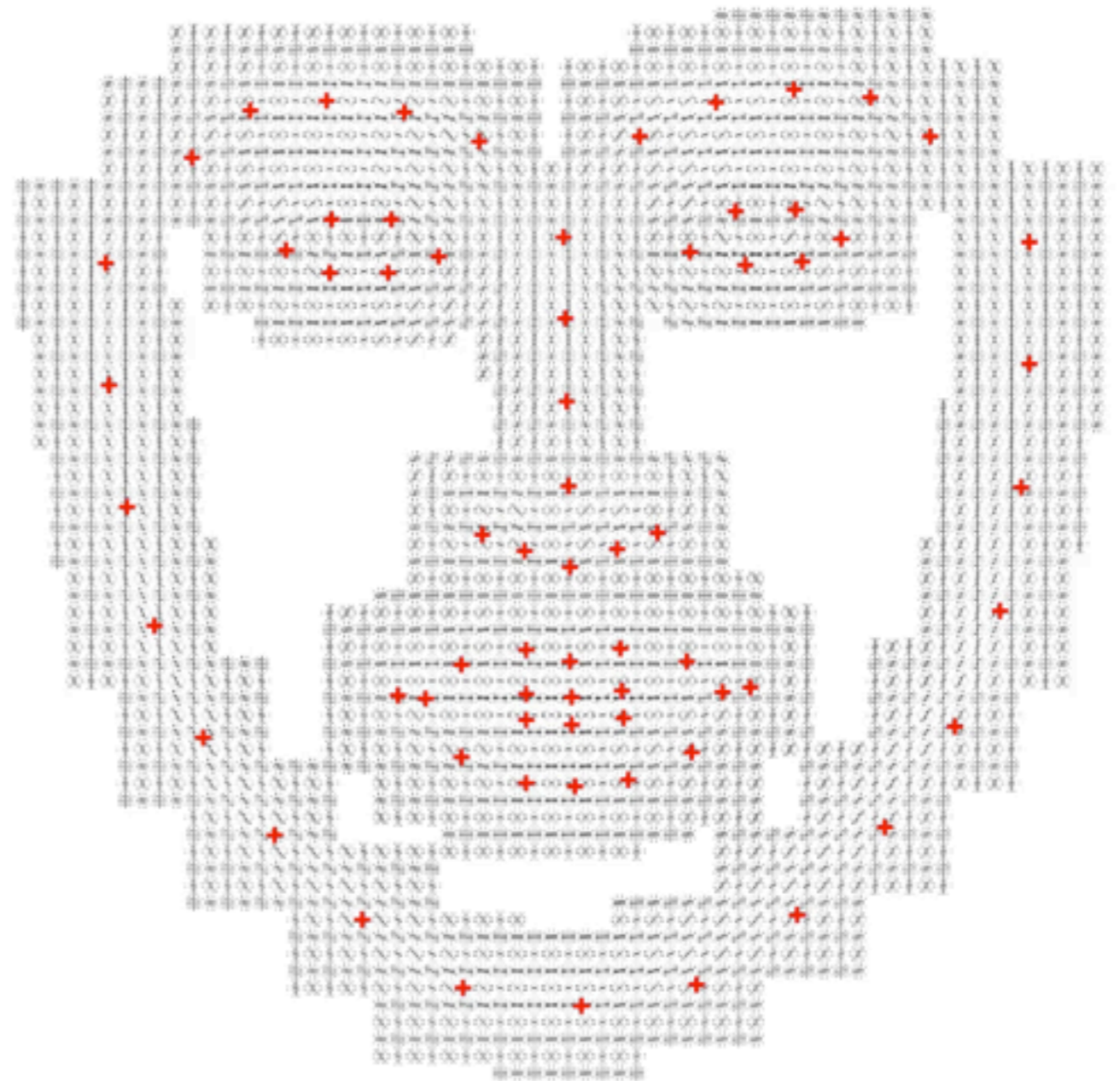
$+\mathbf{A}_3(\mathbf{x})$



$$\mathcal{A}(\mathbf{x}; \boldsymbol{\lambda}) = \mathbf{A}_0(\mathbf{x}) + \sum_{i=1}^m \mathbf{A}_i(\mathbf{x}) \lambda_i$$

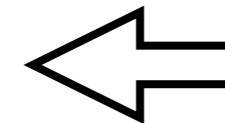
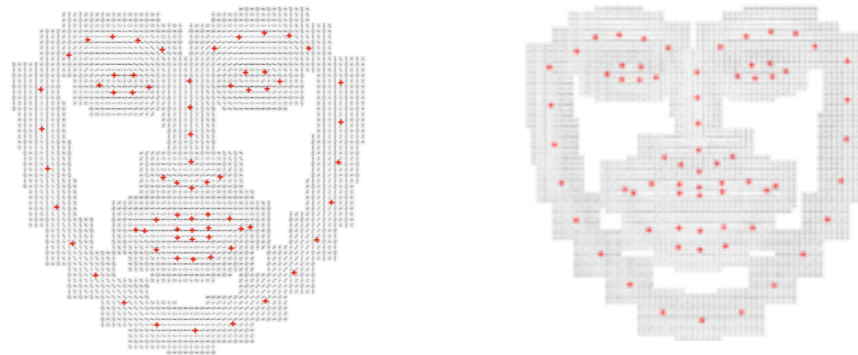
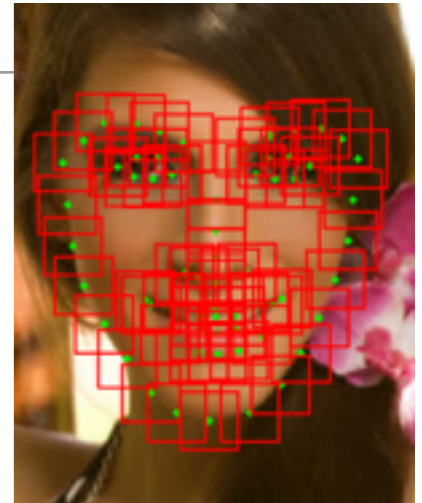
Local Appearance Model (LAM)

- Combined Parametric Model
 - Shape Regularization
 - Local Appearance (w/ HoG Features)
- Model Optimization/Fitting
 - Linear Warp Function
 - LK Framework
 - Cascaded Regression



$$\mathcal{M}(\mathbf{p}, \boldsymbol{\lambda}) \equiv \underbrace{\mathcal{W}(\mathbf{s}; \mathbf{p})}_{\text{Shape + Pose}} \cup \underbrace{\mathcal{A}(\mathbf{x}; \boldsymbol{\lambda})}_{\text{Appearance}}$$

Simultaneous Forwards Additive (SFA)

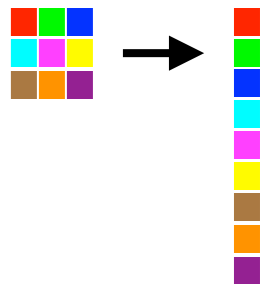


Goal

$$\arg \min_{\mathbf{p}, \lambda} \left\| \mathbf{A}_0 + \mathbf{A}\lambda - \mathbf{I}(\mathcal{W}(\mathbf{p})) \right\|^2$$

Face Model
Warped Instance

$\mathbf{I}(\mathbf{x})$



Iteratively solve for small updates

$$\arg \min_{\Delta \mathbf{p}, \Delta \lambda} \left\| \mathbf{A}_0 + \mathbf{A}(\lambda + \Delta \lambda) - \mathbf{I}(\mathcal{W}(\mathbf{p} + \Delta \mathbf{p})) \right\|^2$$

Solution

$$\begin{bmatrix} \Delta \mathbf{p} \\ \Delta \lambda \end{bmatrix} = \mathbf{H}_{\text{FA}}^{-1} \mathbf{J}_{\text{FA}}^T [\mathbf{A}_0 + \mathbf{A}\lambda - \mathbf{I}(\mathcal{W}(\mathbf{p}))]$$

Jacobian

$$\mathbf{J}_{\text{FA}} = \left(\begin{array}{c|c} \text{Image Gradients} & \text{Jacobian of the Warp} \\ \hline \nabla \mathbf{I} & \frac{\partial \mathcal{W}(\mathbf{p})}{\partial \mathbf{p}} \end{array}, \mathbf{A} \right)$$

Hessian

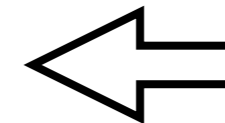
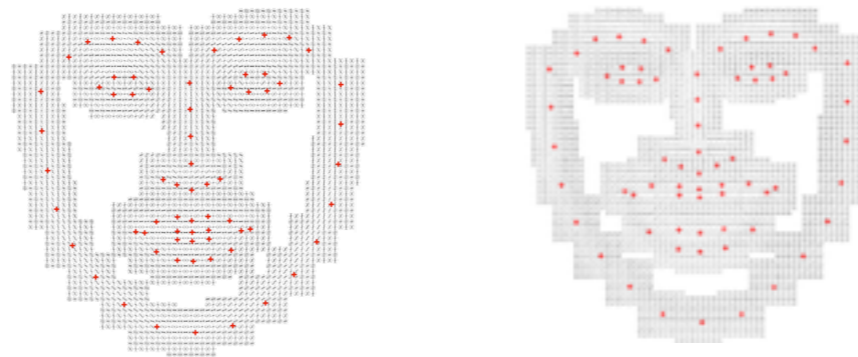
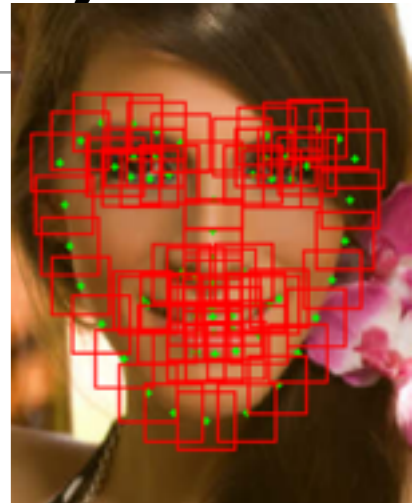
$$\mathbf{H}_{\text{FA}} = \mathbf{J}_{\text{FA}}^T \mathbf{J}_{\text{FA}} \quad \text{Gauss Newton Approximation}$$

Parameters Update

Shape Parameters
 $\mathbf{p} \leftarrow \mathbf{p} + \Delta \mathbf{p}$

Appearance Parameters
 $\lambda \leftarrow \lambda + \Delta \lambda$

Simultaneous Inverse Compositional (SIC)

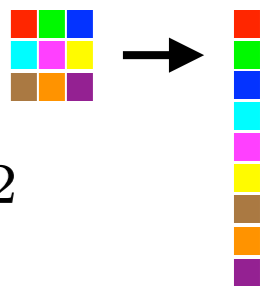


Goal

$$\arg \min_{\mathbf{p}, \lambda} \left\| \mathbf{A}_0 + \mathbf{A}\lambda - \mathbf{I}(\mathcal{W}(\mathbf{p})) \right\|^2$$

Face Model
Warped Instance

$\mathbf{I}(\mathbf{x})$



Iteratively solve for small updates

$$\arg \min_{\Delta \mathbf{p}, \Delta \lambda} \left\| \mathbf{A}_0(\mathcal{W}(\Delta \mathbf{p})) + \mathbf{A}(\mathcal{W}(\Delta \mathbf{p}))(\lambda + \Delta \lambda) - \mathbf{I}(\mathcal{W}(\mathbf{p})) \right\|^2$$

Solution

$$\begin{bmatrix} \Delta \mathbf{p} \\ \Delta \lambda \end{bmatrix} = -\mathbf{H}_{\text{IC}}^{-1} \mathbf{J}_{\text{IC}}^T [\mathbf{A}_0 + \mathbf{A}\lambda - \mathbf{I}(\mathcal{W}(\mathbf{p}))]$$

Jacobian

$$\mathbf{J}_{\text{IC}} = \left(\begin{array}{c} \text{Appearance} \\ \text{Model Gradients} \end{array} \left(\nabla \mathbf{A}_0 + \nabla \mathbf{A}\lambda \right) \begin{array}{c} \text{Jacobian} \\ \text{of the Warp} \end{array} \frac{\partial \mathcal{W}(\mathbf{0})}{\partial \mathbf{p}}, \mathbf{A} \right)$$

Shape Parameters
Appearance Parameters

Hessian

$$\mathbf{H}_{\text{IC}} = \mathbf{J}_{\text{IC}}^T \mathbf{J}_{\text{IC}} \quad \text{Gauss Newton Approximation}$$

Parameters Update

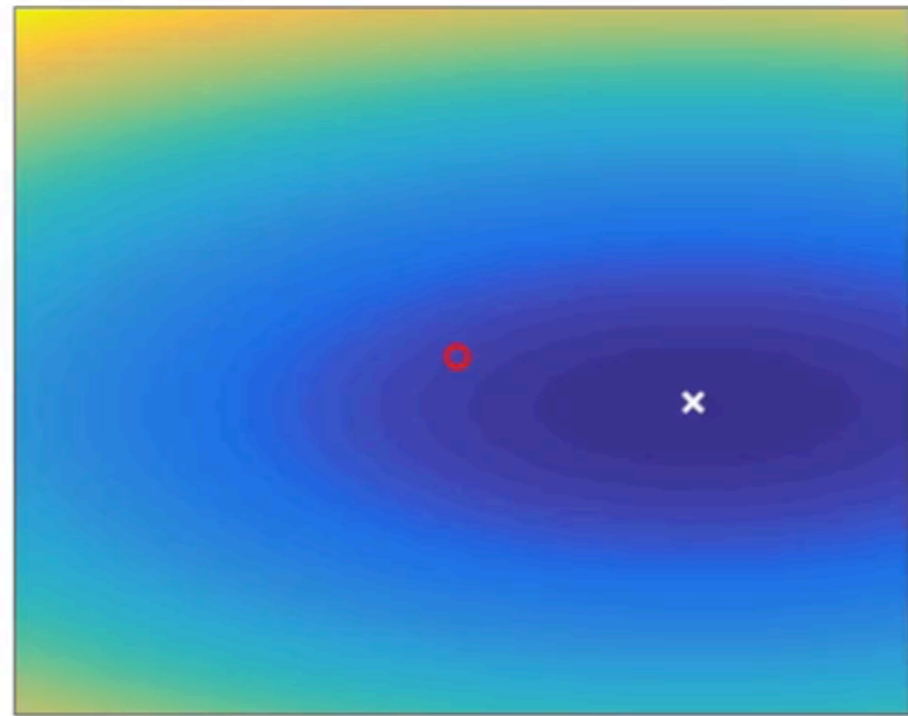
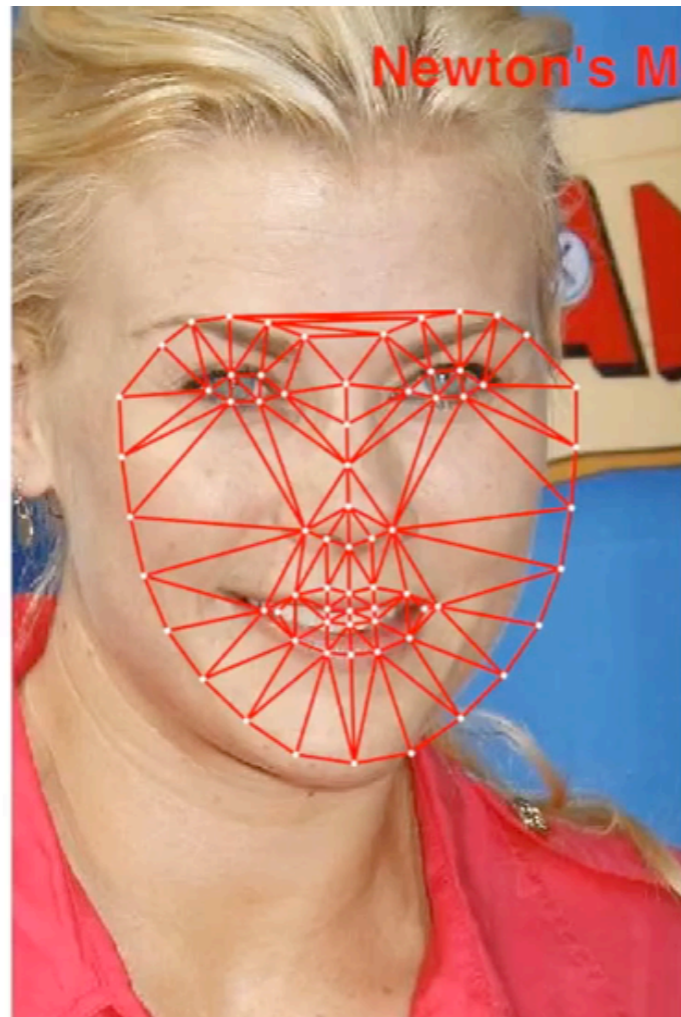
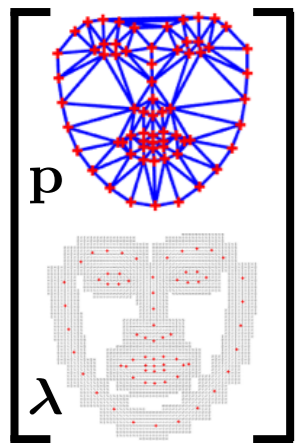
$$\begin{aligned} \mathcal{W}(\mathbf{s}, \mathbf{p}) &\leftarrow \mathcal{W}(\mathbf{s}, \mathbf{p}) \circ \mathcal{W}(\mathbf{s}, \Delta \mathbf{p})^{-1} \\ \mathbf{p} &\leftarrow \mathbf{p} - \Delta \mathbf{p} \end{aligned}$$

Appearance Parameters

$$\lambda \leftarrow \lambda + \Delta \lambda$$

Simultaneous Cascaded Regression (SCR)

Regression with both shape and appearance structure



Cost Function

Simultaneous Inverse Compositional (SIC) vs Simultaneous Cascaded Regression (SCR)



$$\begin{bmatrix} \mathbf{p} \\ \boldsymbol{\lambda} \end{bmatrix}^k = \begin{bmatrix} \mathbf{p} \\ \boldsymbol{\lambda} \end{bmatrix}^{k-1} + \mathbf{R}^{k-1} \left(\mathbf{I}(\mathcal{W}(\mathbf{p}^{k-1})) - \mathbf{A}_0 - \mathbf{A}\boldsymbol{\lambda}^{k-1} \right), \quad k = 1, \dots, K$$

Shape + Appearance parameters

Features extracted at previous level

Features generated by the Model

SCR - Learning Regression Matrices

Estimate average Jacobian under multiple initializations

$$\arg \min_{\mathbf{J}_S^k} \sum_{i=1}^N \int p(\mathbf{r}') \left\| \mathbf{A}_0 + \mathbf{A} \boldsymbol{\lambda}_i^k + \mathbf{J}_S^k \Delta \mathbf{r}_i^k - \mathbf{I}_i(\mathcal{W}(\mathbf{p}_i^k)) \right\|^2 \partial \mathbf{r}'$$

Deviation from Ground Truth

$$\Delta \mathbf{r}_i^k = \begin{bmatrix} \mathbf{p}_i^k - \mathbf{p}_* \\ \boldsymbol{\lambda}_i^k - \boldsymbol{\lambda}_* \end{bmatrix} \quad \begin{array}{l} k - \text{cascade level} \\ i - \text{training image} \\ j - \text{virtual sample} \end{array}$$

Discrete approximation

$$\arg \min_{\mathbf{J}_S^k} \sum_{i=1}^N \sum_{j=1}^M \left\| \mathbf{A}_0 + \mathbf{A} \boldsymbol{\lambda}_{ij}^k + \mathbf{J}_S^k \Delta \mathbf{r}_{ij}^k - \mathbf{I}_i(\mathcal{W}(\mathbf{p}_{ij}^k)) \right\|^2$$

Solution by Ridge Regression

$$\mathbf{J}_S^k = (\Delta \mathbf{r} \Delta \mathbf{r}^T + \lambda_1 \mathbf{I}_d)^{-1} \Delta \mathbf{r} \mathbf{E}^T$$

Advantage: do not require to invert a large data matrix

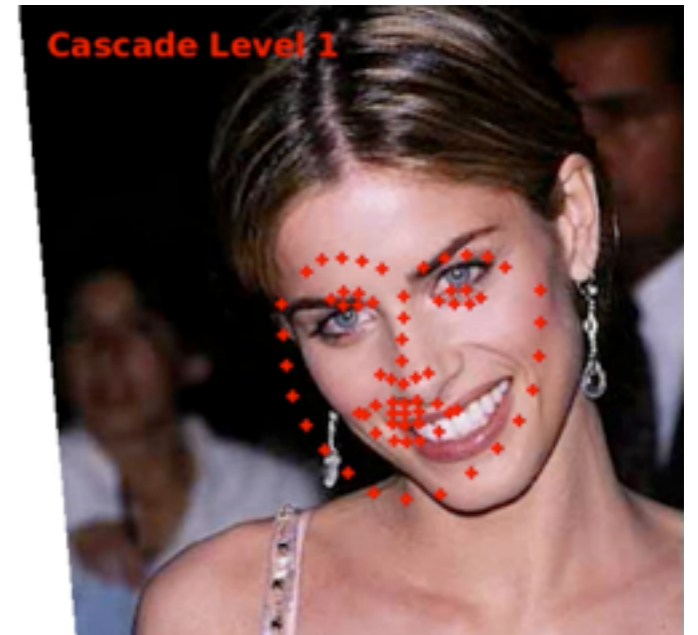
Update matrix

$$\mathbf{R}^k = \left((\mathbf{J}_S^k)^T \mathbf{J}_S^k + \lambda_2 \mathbf{I}_d \right)^{-1} (\mathbf{J}_S^k)^T$$

Cascade update

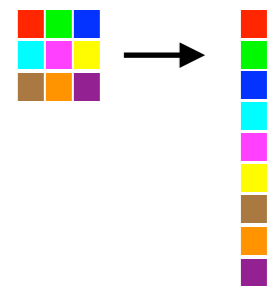
$$\Delta \mathbf{r}^k = \mathbf{R}^k \left(\mathbf{I}(\mathcal{W}(\mathbf{p}^k)) - \mathbf{A}_0 - \mathbf{A} \boldsymbol{\lambda}^k \right)$$

$$\mathbf{r}^{k+1} = \mathbf{r}^k + \Delta \mathbf{r}^k$$

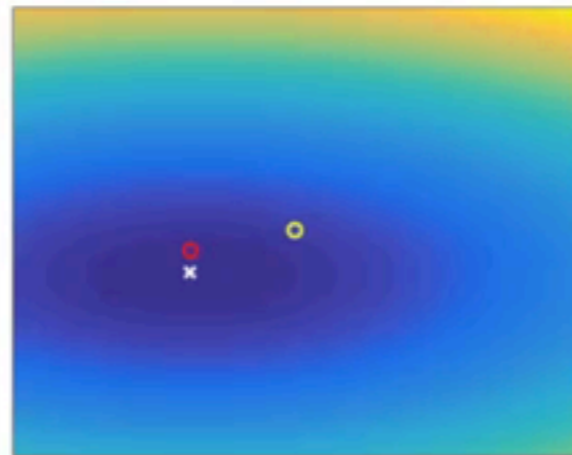
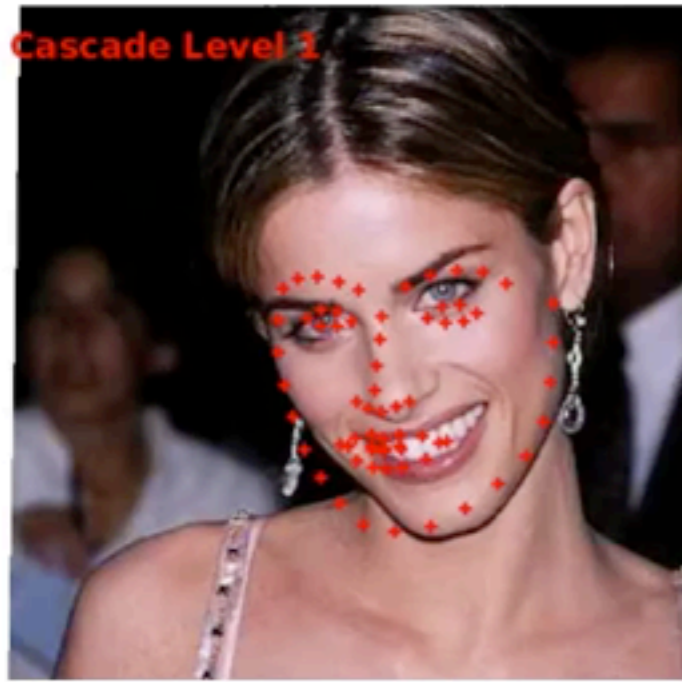


E: Data matrix w/ entries

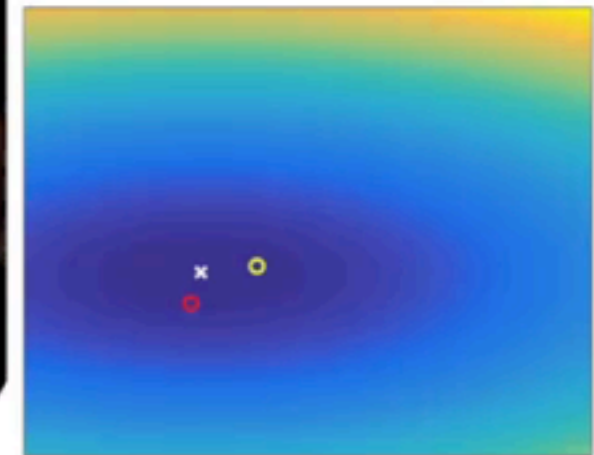
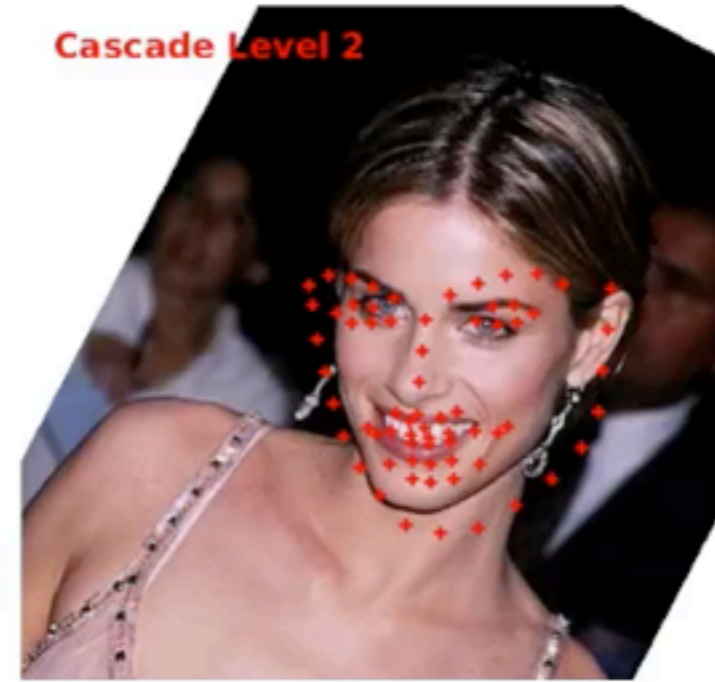
$$\mathbf{E}_{ij} = \mathbf{I}_i(\mathcal{W}(\mathbf{p}_{ij}^k)) - \mathbf{A}_0 - \mathbf{A} \boldsymbol{\lambda}_{ij}^k$$



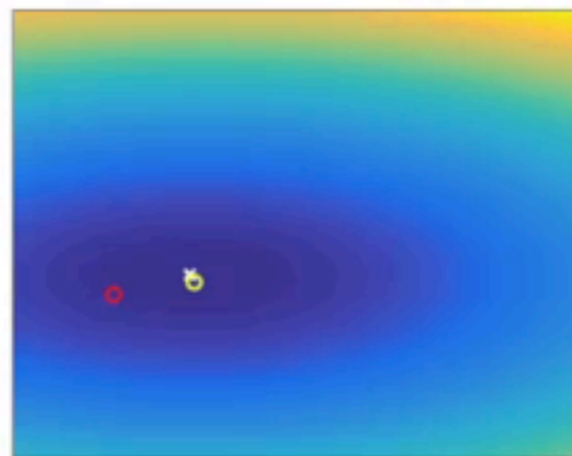
Cascaded Regression Learning



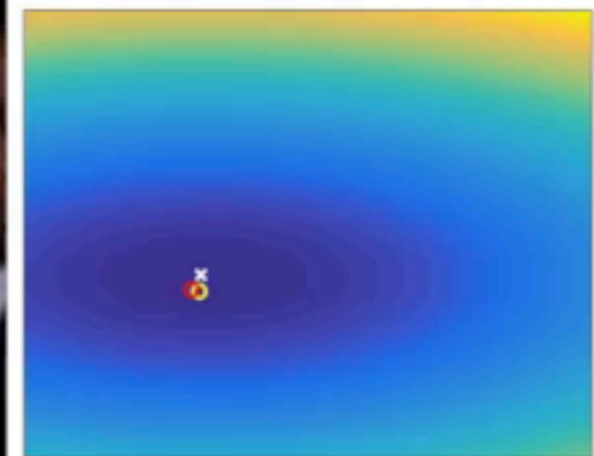
Cost Function



Cost Function



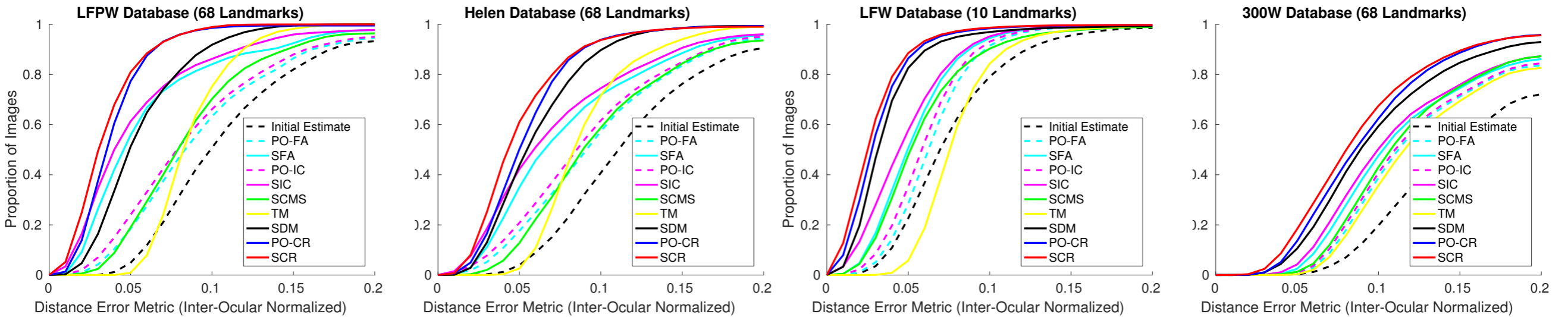
Cost Function



Cost Function

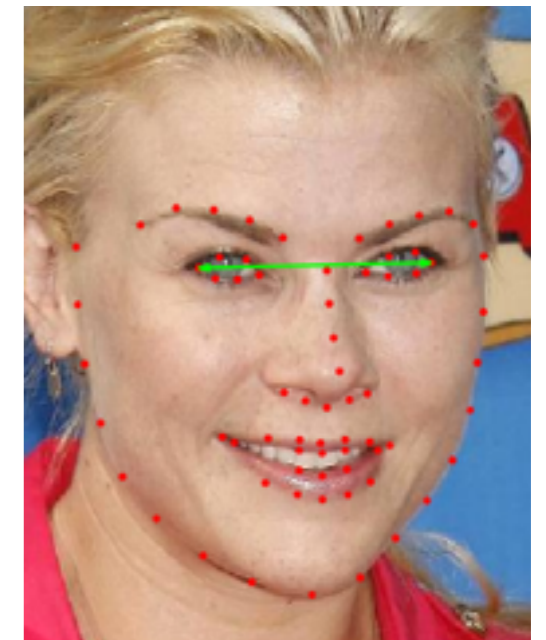
Evaluation Results

Cumulative error distribution function (CDF)



Method / AUC	LFPW	HELEN	LFW	300W
Initial Estimate	46.4	41.6	61.7	27.2
PO-FA	53.6	51.3	67.3	38.2
SFA	70.0	60.2	73.0	42.3
PO-IC	56.1	53.8	69.4	39.1
SIC	73.1	63.5	75.6	43.9
SCMS	56.9	50.7	70.7	40.9
TM	56.5	54.8	60.1	36.7
SDM	72.2	69.7	81.5	50.3
PO-CR	80.4	72.5	84.1	53.3
SCR	82.6	74.8	85.5	55.5

Area Under Curve (AUC)

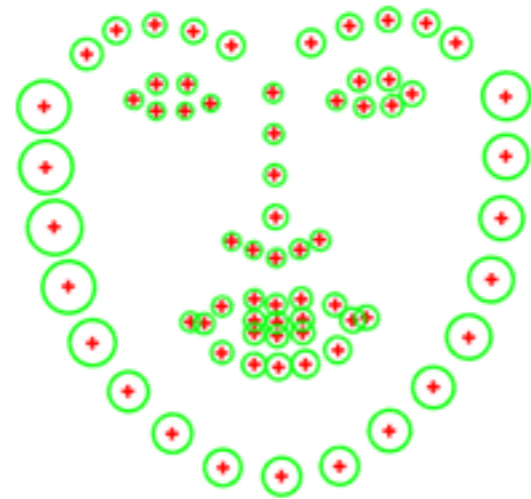
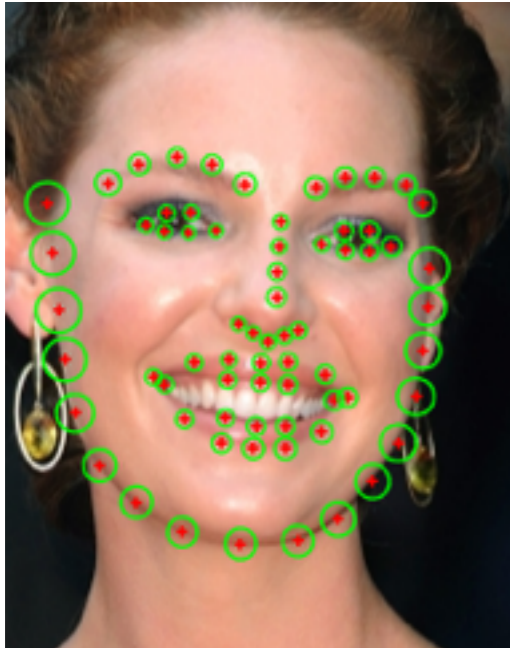


Inter-ocular normalized error

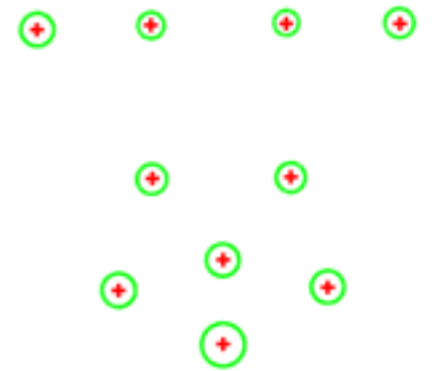
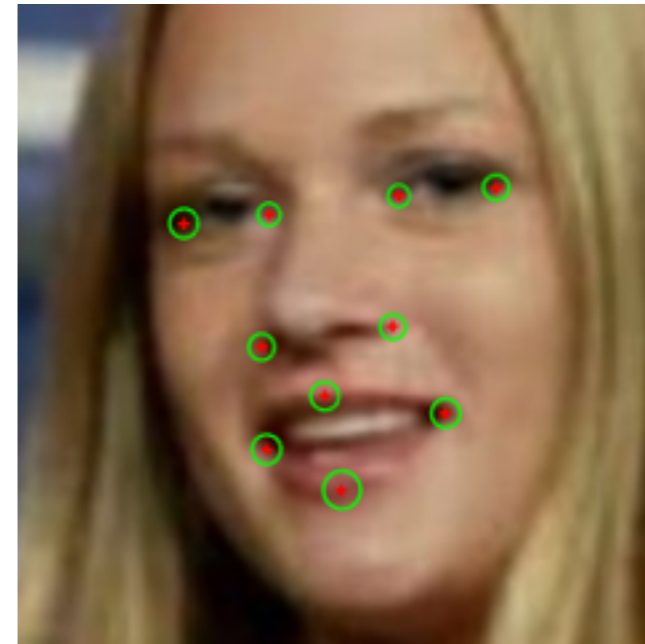
$$e_m(\mathbf{s}) = \frac{1}{v d_{\text{eyes}}} \sum_{i=1}^v \|s_i - s_i^*\|$$

Landmark Fitting Error Standard Deviation

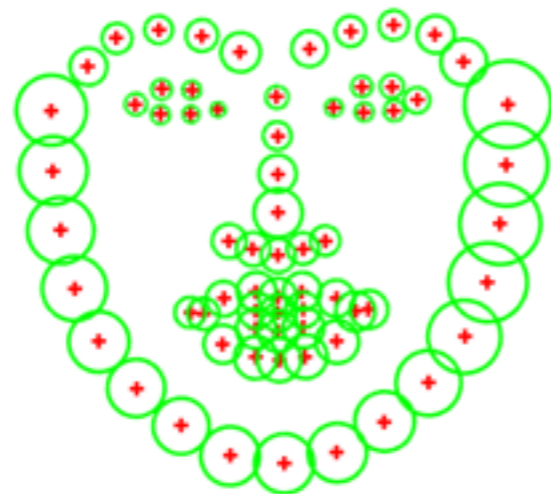
LFPW Database



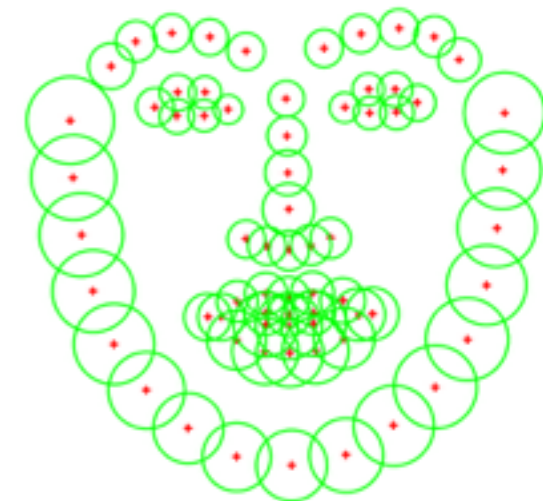
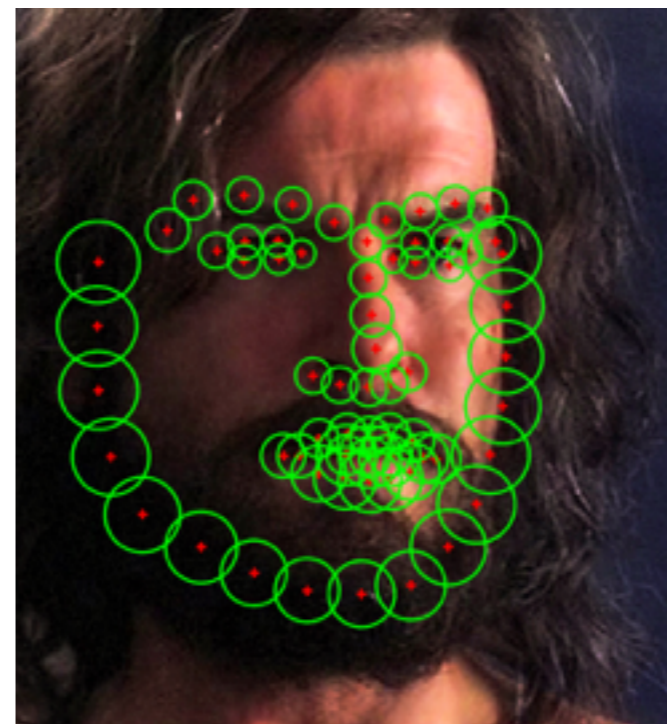
LFW Database



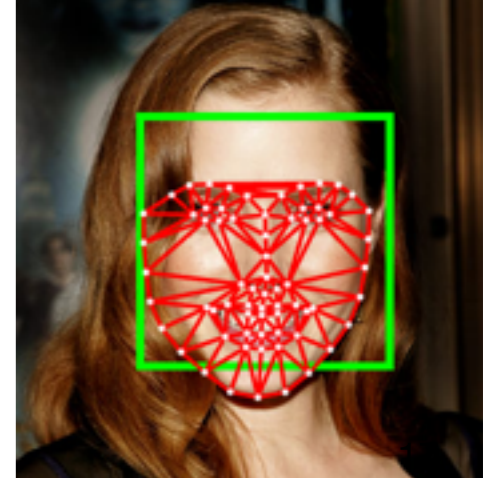
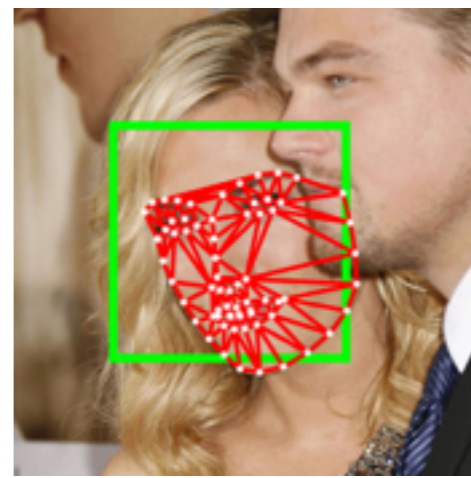
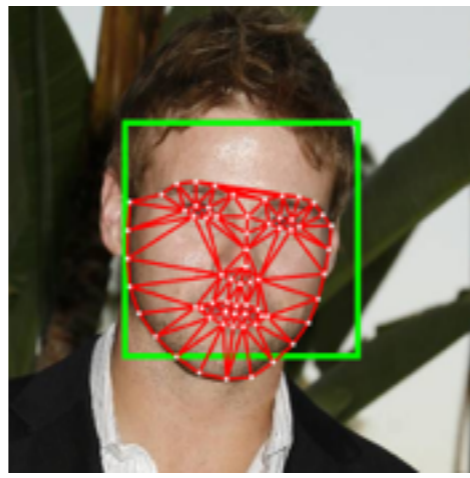
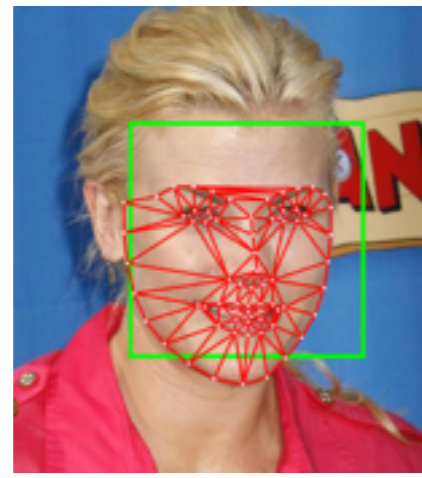
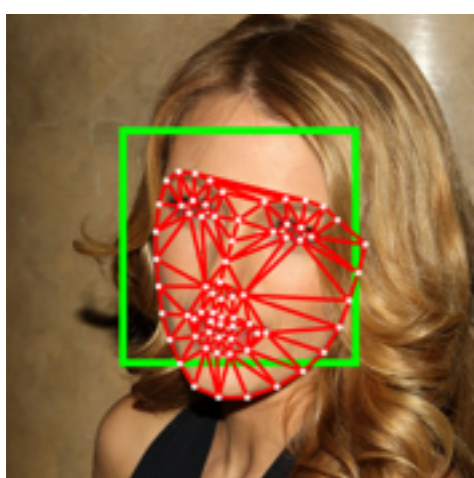
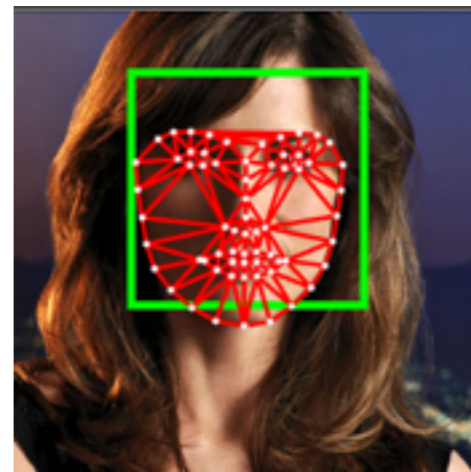
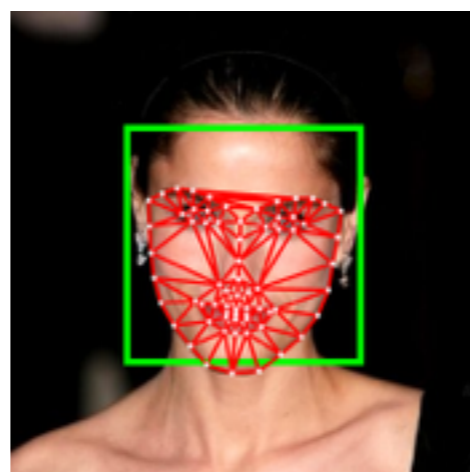
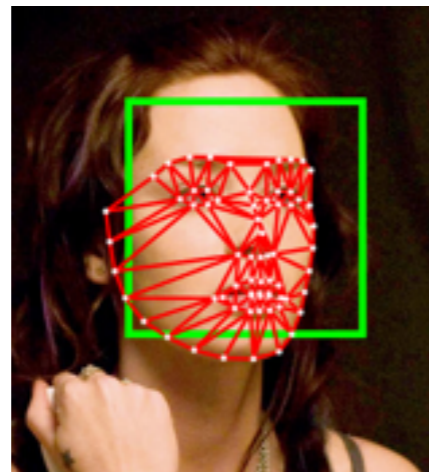
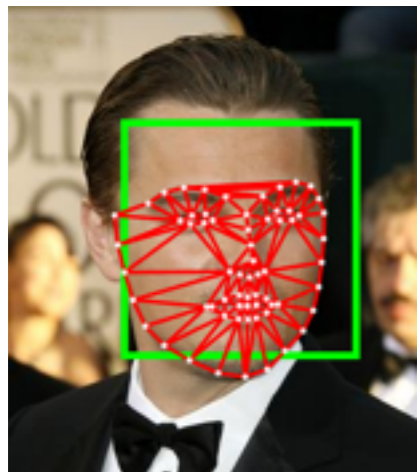
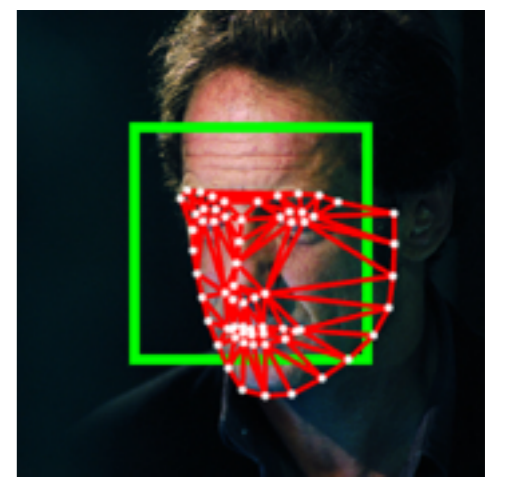
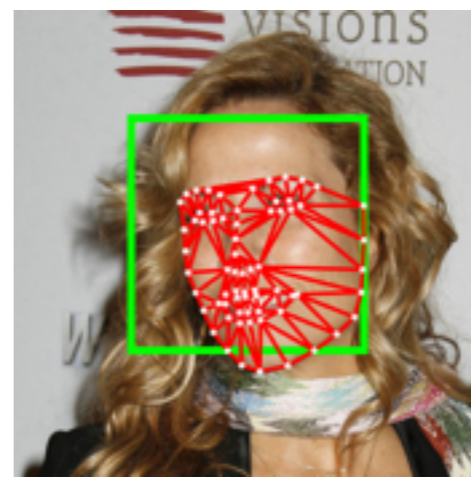
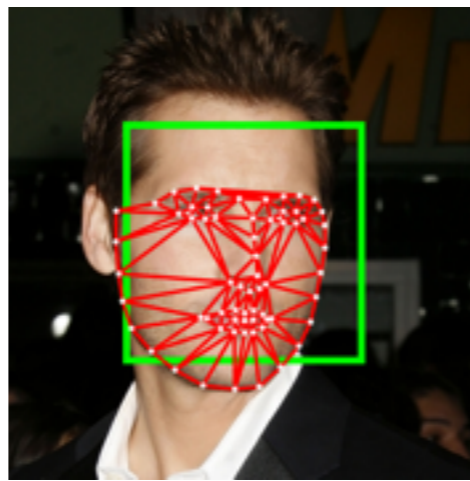
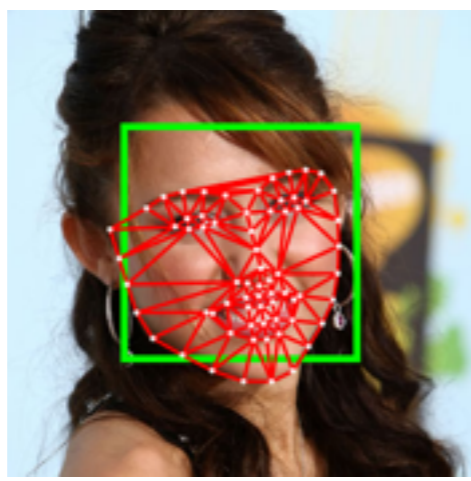
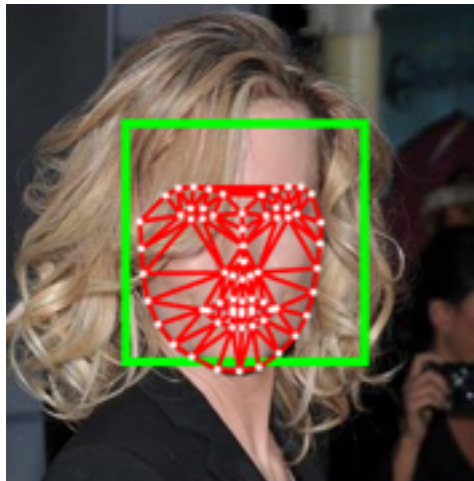
HELEN Database



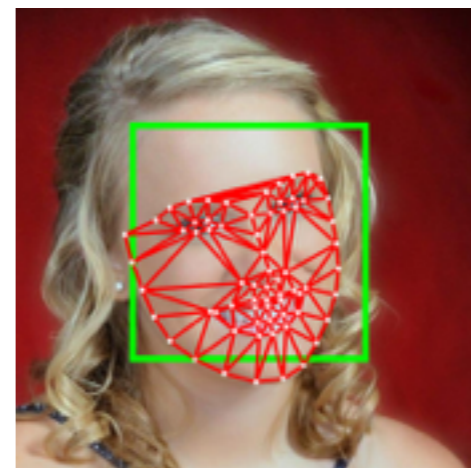
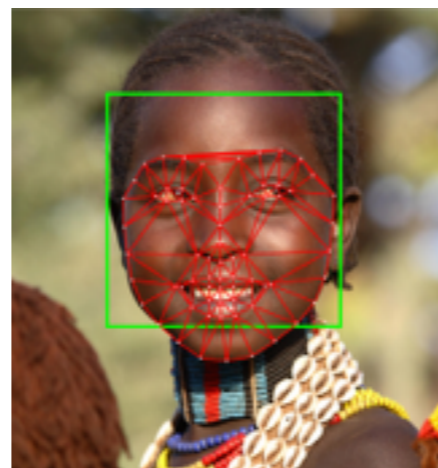
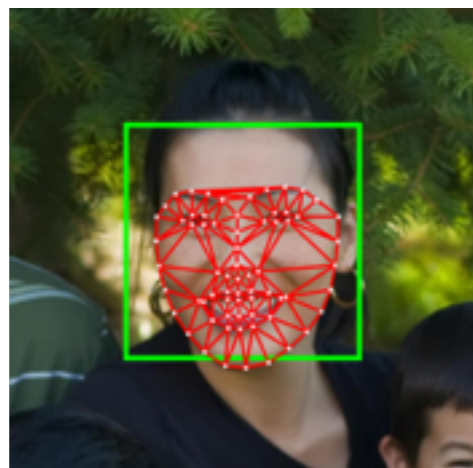
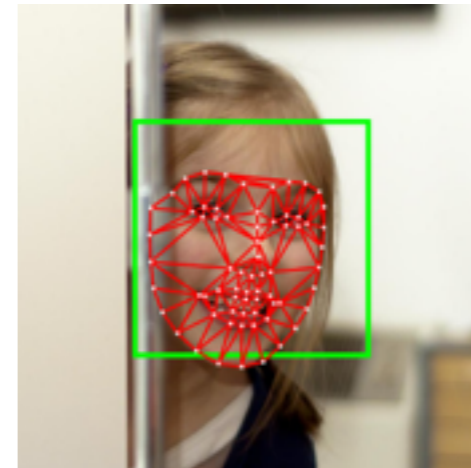
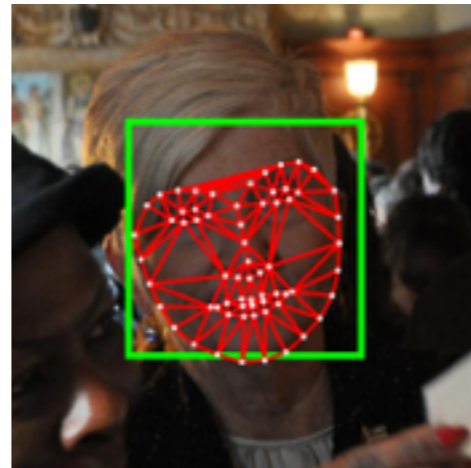
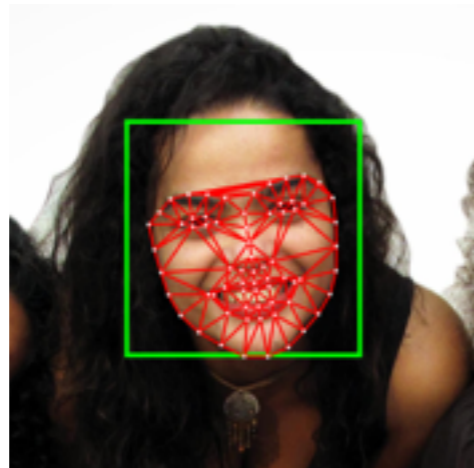
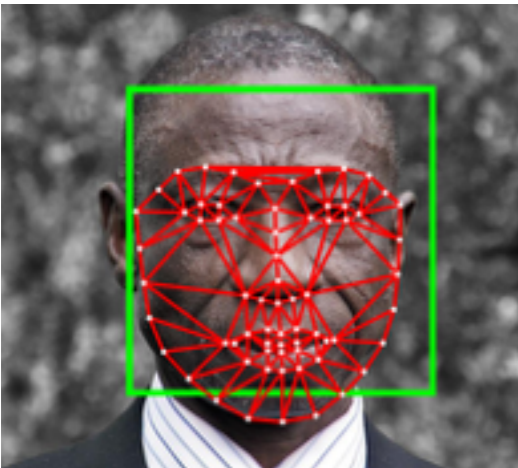
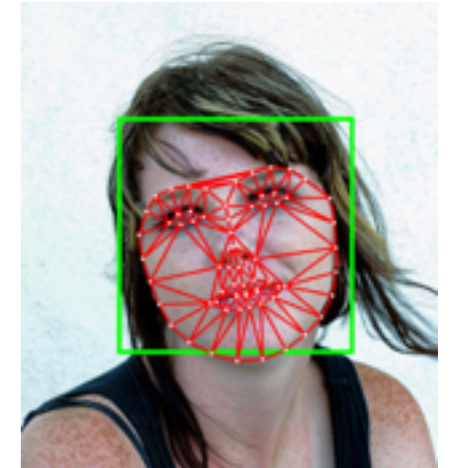
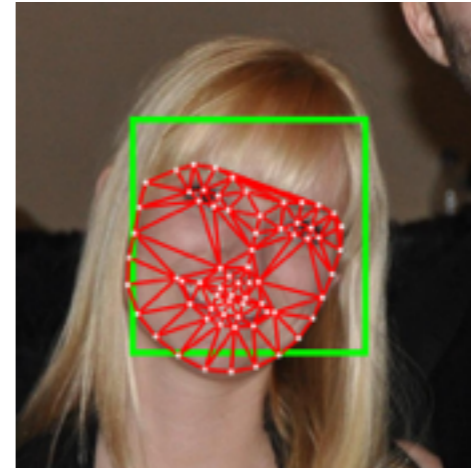
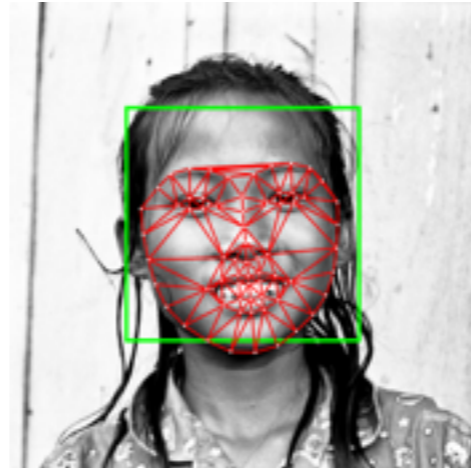
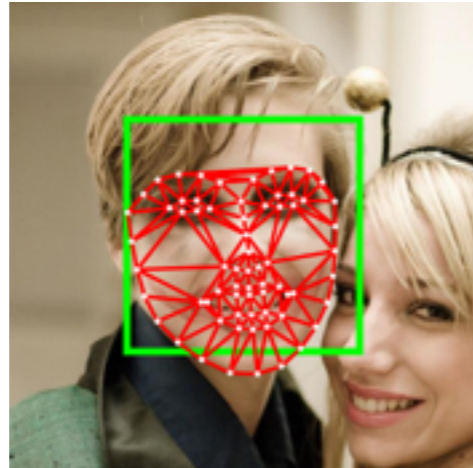
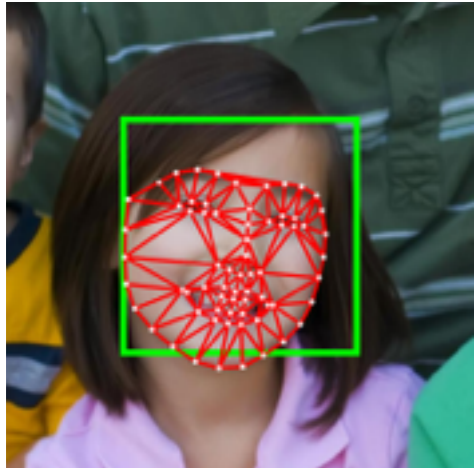
300W Database



Qualitative Results (LFPW Database)



Qualitative Results (HELEN Database)



SCR Fitting Video



Simultaneous Cascaded Regression
Pedro Martins, Jorge Batista
ISR - Institute of Systems and Robotics
University of Coimbra, Portugal

IEEE International Conference on Image Processing 2018
ICIP 2018

Conclusions

- Facial landmark localization w/ deformable face model
- Simultaneous Algorithm: Cascaded Regression Extension
 - Regression w/ both shape and appearance structure
 - Learning stage w/o inverting a large data matrix
- Evaluation Results (LFPW, HELEN, LFW, 300W datasets)
- Acknowledgements
 - Work supported by the Portuguese Science Foundation ('Fundação para a Ciência e Tecnologia - FCT') through the grant SFRH/BDP/90200/2012.

Questions?

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SCR Fitting Video



Simultaneous Cascaded Regression
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