# Facial Expression Recognition Using Active Appearance

Pedro Martins Joana Sampaio Jorge Batista



Institute of Systems and Robotics
Dep. of Electrical Engineering and Computers
University of Coimbra



#### Introduction

- Facial expression has more influence than simple audio information
- Human Computer Interface (HCI)
- Video compression

- Recognition of 7 different expressions
  - [Ekman and Friesen] said that people are born with the ability to generate and interpret only six facial expressions: happiness, sadness, surprise, anger, fear and disgust.
- Facial expression recognition in still images

## Agenda

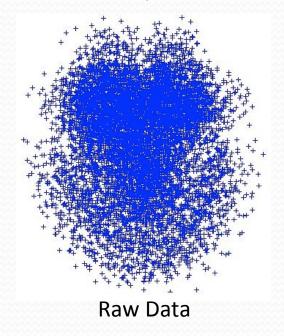
- Active Apperance Models
  - Shape Model
  - Texture Model
  - Combined Model
- Linear Discriminant Analysis
- Classification using malahonobis distance
- Results

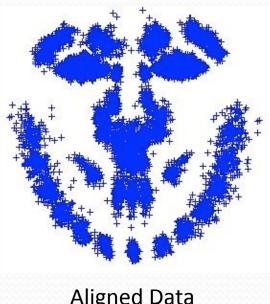
## Active Appearance Models

- AAM is a statistical based segmentation method, where the variability of shape and texture is captured from a dataset
- Able to extract relevant face information without background interference
- Describes facial characteristics in a reduced model

## Shape Model

- Shape defined as  $x = (x_1, y_1, ..., x_n, y_n)^T$
- Generalised Procrustes Analysis (GPA)
  - Remove Location, scale and rotation effects





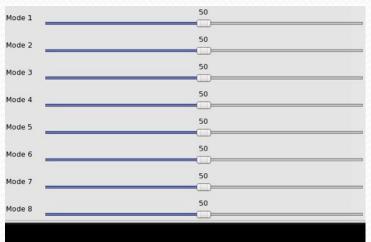
Aligned Data

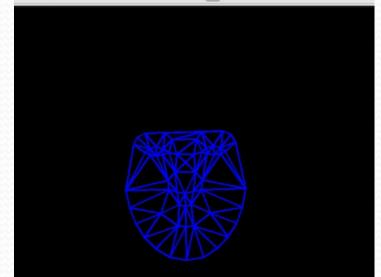
## Statistical Shape Model

Applying a PCA:

$$x = \overline{x} + \Phi_s b_s$$

- x is the synthesized
- x is the mean shape
- Фs contains the highest covariance texture eigenvectors
- bs is a vector of shape parameters representing the weights



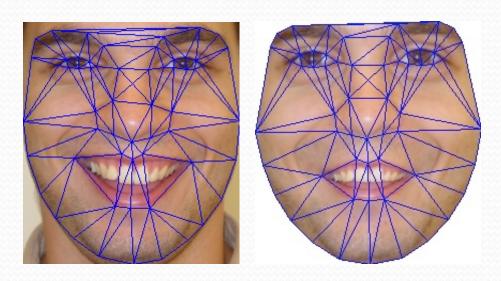


### **Texture Model**

For m pixels sampled, the texture is represented by:

$$g = (g_1, g_2, ..., g_{m-1}, g_m)^T$$

Required warping each image to a common reference frame



- Delaunay Triangulation
- Each pixel is mapped barycentric coordinates

# **Texture Mapping Examples**























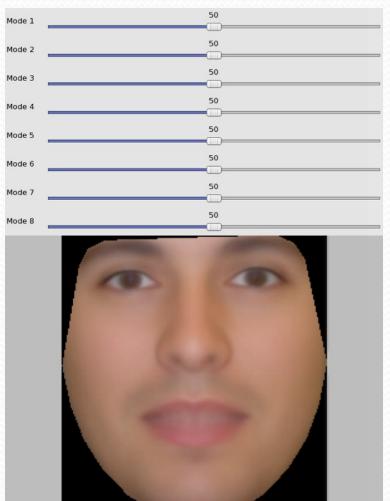


### Statistical Texture Model

• Applying a LowMemory PCA:

$$g = \overline{g} + \Phi_g b_g$$

- g is the synthesized texture
- *g* is the mean texture
- Dg contains the highest covariance texture eigenvectors
- bg is a vector of texture parameters



#### **Combined Model**

 To remove correlations between bs and bg a third PCA is performed

$$b = \left(\frac{W_s b_s}{b_g \dot{j}}\right) = \left(\frac{W_s \Phi_s^T (x - x)}{\Phi_g^T (g - g)}\right) \dot{j}$$

$$W_s = rI$$

$$r = \frac{\sum_i \lambda_{gi}}{\sum_j \lambda_{sj}}$$

$$b = \Phi_c c$$

$$\Phi_c = \left(\frac{\Phi_{cs}}{\Phi_{cg}}\right) \dot{j}$$

$$x = \overline{x} + \Phi_s W_s^{-1} \Phi_{cs} c$$

$$g = \overline{g} + \Phi_g \Phi_{cg} c$$

Building an AAM instance



Shape

Texture in the mean shape frame

AAM instance





# **AAM Instance Examples**

















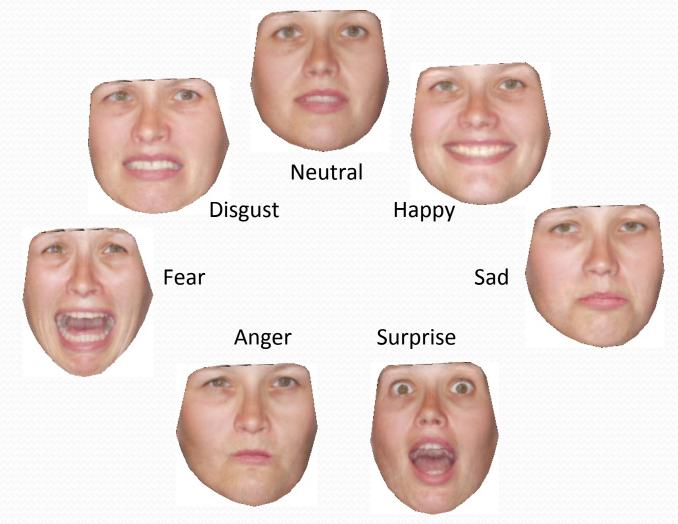








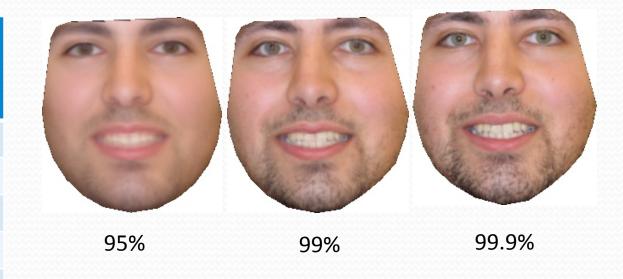
# Facial Expression Recognition



#### **AAM Retained Variance**

 How much variance should be retained in AAM building process?

Variance (%)	Number of Combined EigenVectors			
95	17			
97	29			
98	42			
99	70			
99.5	97			
99.9	133			



## Linear Discriminant Analysis

 Supervised method that maximizes the betweenclass variance as well that minimizes the within-class variance

 Classification using malahanobis distance

$$D = (c - \overline{c_i}) \sum^{-1} (c - \overline{c_i})$$

$$S_b = \sum_{i=1}^{n_c} n_i (x_i - x)(x_i - x)^T$$

Between-class scatter matrix

$$S_{w} = \sum_{i=1}^{n_{c}} \sum_{j=1}^{n_{i}} (x_{i,j} - \overline{x}_{i}) (x_{i,j} - \overline{x}_{i})^{T}$$

Within-class scatter matrix

 $x_{i,j}$  is the  $y^{th}$  sample in class i  $x_i$  mean of class i  $x_i$  mean of all classes  $x_i$  number of classes  $x_i$  number of samples in class i

### LDA Evaluation Metric

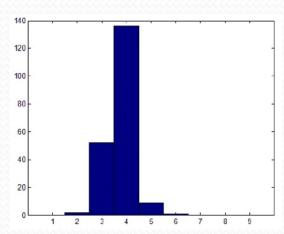
How many eigenvectors hold on LDA?

- k-means clustering on result of LDA
- Discrimination quality given by:

$$DQuality = \sum_{i=1}^{n_{classes}} \max(row(i)) - \min(row(i))$$

	Neut	Нарр	Sad	Surp	Ang	Fear	Disg
Neut	N	0	0	0	0	0	0
Нарр	0	N	0	0	0	0	0
Sad	0	0	N	0	0	0	0
Surp	0	0	0	N	0	0	0
Ang	0	0	0	0	N	0	0
Fear	0	0	0	0	0	N	0
Disg	0	0	0	0	0	0	N

K-means clustering result for ideal LDA



Histogram for best LDA modes on 250 trials

#### Experimental Results 7 Expressions

	Neut	Нарр	Sad	Surp	Ang	Fear	Disg
Neut	19.0	0	58.38	0	9.52	19.05	0
Нарр	0	90.48	0	0	0	4.77	4.77
Sad	9.52	0	61.90	4.77	9.52	14.29	0
Surp	0	0	0	80.95	0	19.05	0
Ang	0	0	14.29	0	33.33	9.52	42.86
Fear	0	4.77	9.52	19.05	14.29	52.38	0
Disg	0	14.29	0	0	38.10	0	47.62

	Neut	Нарр	Sad	Surp	Ang	Fear	Disg
Neut	33.33	0	61.90	0	0	4.76	0
Нарр	0	80.95	0	0	0	9.52	9.52
Sad	0	4.76	66.67	0	19.05	9.52	0
Surp	0	0	0	71.43	0	28.57	0
Ang	0	4.76	4.76	0	42.86	14.29	33.33
Fear	0	4.76	9.52	19.05	9.52	52.38	4.76
Disg	0	9.52	0	0	38.10	4.76	47.62

Confusion Matrix 97% Overal Recognition Rate = 55%

Confusion Matrix 98% Overal Recognition Rate = 56.5%

	Neut	Нарр	Sad	Surp	Ang	Fear	Disg
Neut	52.38	0	42.86	0	4.76	0	0
Нарр	0	90.48	4.76	0	0	4.76	0
Sad	4.76	4.76	76.19	0	4.76	4.76	4.76
Surp	0	0	0	76.19	0	23.81	0
Ang	4.76	0	9.52	0	33.33	23.81	28.57
Fear	0	9.52	4.76	14.29	4.76	66.67	0
Disg	0	23.81	4.76	0	33.33	4.76	33.33

Confusion Matrix 99% Overal Recognition Rate = 61.2%

 Results by a Leave-one-out cross-validation scheme

#### Experimental Results 7 Expressions

	Neut	Нарр	Sad	Surp	Ang	Fear	Disg	
Neut	19.0	0	58.38	0	9.52	19.05	0	ľ
Нарр	0	90.48	0	0	0	4.77	4.77	H
Sad	9.52	0	61.90	4.77	9.52	14.29	0	
Surp	0	0	0	80.95	0	19.05	0	9
Ang	0	0	14.29	0	33.33	9.52	42.86	
Fear	0	4.77	9.52	19.05	14.29	52.38	0	1
Disg	0	14.29	0	0	38.10	0	47.62	ı

	Neut	Нарр	Sad	Surp	Ang	Fear	Disg
Neut	33.33	0	61.90	0	0	4.76	0
Нарр	0	80.95	0	0	0	9.52	9.52
Sad	0	4.76	66.67	0	19.05	9.52	0
Surp	0	0	0	71.43	0	28.57	0
Ang	0	4.76	4.76	0	42.86	14.29	33.33
Fear	0	4.76	9.52	19.05	9.52	52.38	4.76
Disg	0	9.52	0	0	38.10	4.76	47.62

• Confusion Matrix 97% Overal Recognition Rate = 55%

Confusion Matrix 98% Overal Recognition Rate = 56.5%

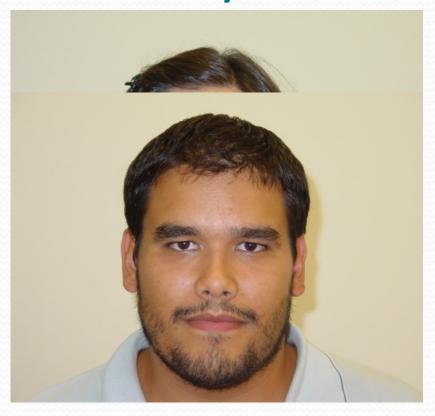
	Neut	Нарр	Sad	Surp	Ang	Fear	Disg
Neut	52.38	0	42.86	0	4.76	0	0
Нарр	0	90.48	4.76	0	0	4.76	0
Sad	4.76	4.76	76.19	0	4.76	4.76	4.76
Surp	0	0	0	76.19	0	23.81	0
Ang	4.76	0	9.52	0	33.33	23.81	28.57
Fear	0	9.52	4.76	14.29	4.76	66.67	0
Disg	0	23.81	4.76	0	33.33	4.76	33.33

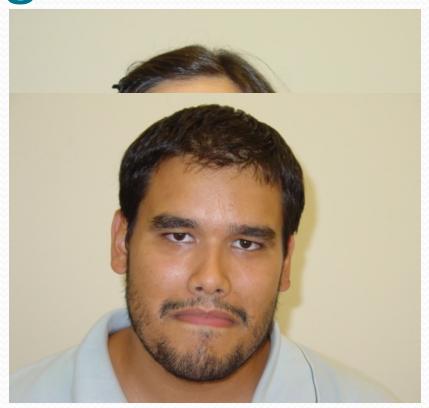
Confusion Matrix 99% Overal Recognition Rate = 61.2%

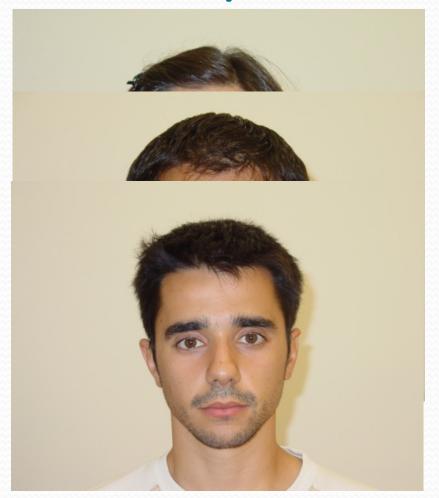
 Results by a Leave-one-out cross-validation scheme

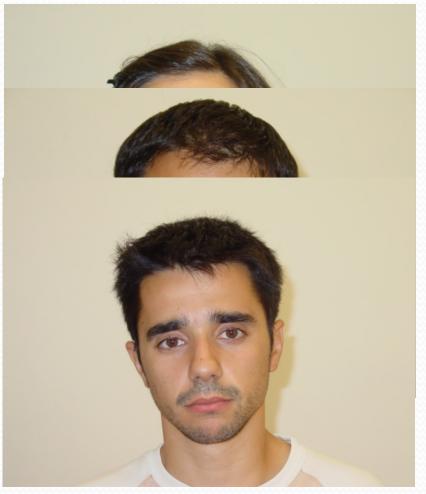












#### Experimental Results 7 Expressions

	Neut	Нарр	Sad	Surp	Ang	Fear	Disg
	recut	парр	Juu	Juip	Alig	i cai	Disg
Neut	19.0	0	58.38	0	9.52	19.05	0
Нарр	0	90.48	0	0	0	4.77	4.77
Sad	9.52	0	61.90	4.77	9.52	14.29	0
Surp	0	0	0	80.95	0	19.05	0
Ang	0	0	14.29	0	33.33	9.52	42.86
Fear	0	4.77	9.52	19.05	14.29	52.38	0
Disg	0	14.29	0	0	38.10	0	47.62

					****		
	Neut	Нарр	Sad	Surp	Ang	Fear	Disg
Neut	33.33	0	61.90	0	0	4.76	0
Нарр	0	80.95	0	0	0	9.52	9.52
Sad	0	4.76	66.67	0	19.05	9.52	0
Surp	0	0	0	71.43	0	28.57	0
Ang	0	4.76	4.76	0	42.86	14.29	33.33
Fear	0	4.76	9.52	19.05	9.52	52.38	4.76
Disg	0	9.52	0	0	38.10	4.76	47.62

Confusion Matrix 97% Overal Recognition Rate = 55%

Confusion Matrix 98% Overal Recognition Rate = 56.5%

	Neut	Нарр	Sad	Surp	Ang	Fear	Disg
Neut	52.38	0	42.86	0	4.76	0	0
Нарр	0	90.48	4.76	0	0	4.76	0
Sad	4.76	4.76	76.19	0	4.76	4.76	4.76
Surp	0	0	0	76.19	0	23.81	0
Ang	4.76	0	9.52	0	33.33	23.81	28.57
Fear	0	9.52	4.76	14.29	4.76	66.67	0
Disg	0	23.81	4.76	0	33.33	4.76	33.33

Confusion Matrix 99% Overal Recognition Rate = 61.2%

#### Experimental Results 7 Expressions

	Neut	Нарр	Sad	Surp	Ang	Fear	Disg
Neut	19.0	0	58.38	0	9.52	19.05	0
Нарр	0	90.48	0	0	0	4.77	4.77
Sad	9.52	0	61.90	4.77	9.52	14.29	0
Surp	0	0	0	80.95	0	19.05	0
Ang	0	0	14.29	0	33.33	9.52	42.86
Fear	0	4.77	9.52	19.05	14.29	52.38	0
Disg	0	14.29	0	0	38.10	0	47.62

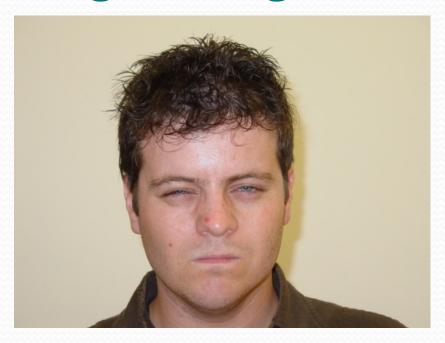
<u> </u>							
	Neut	Нарр	Sad	Surp	Ang	Fear	Disg
Neut	33.33	0	61.90	0	0	4.76	0
Нарр	0	80.95	0	0	0	9.52	9.52
Sad	0	4.76	66.67	0	19.05	9.52	0
Surp	0	0	0	71.43	0	28.57	0
Ang	0	4.76	4.76	0	42.86	14.29	33.33
Fear	0	4.76	9.52	19.05	9.52	52.38	4.76
Disg	0	9.52	0	0	38.10	4.76	47.62

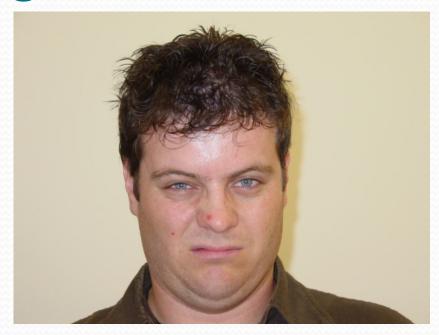
• Confusion Matrix 97% Overal Recognition Rate = 55%

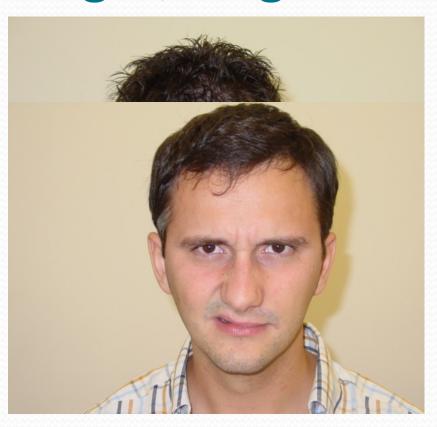
Confusion Matrix 98% Overal Recognition Rate = 56.5%

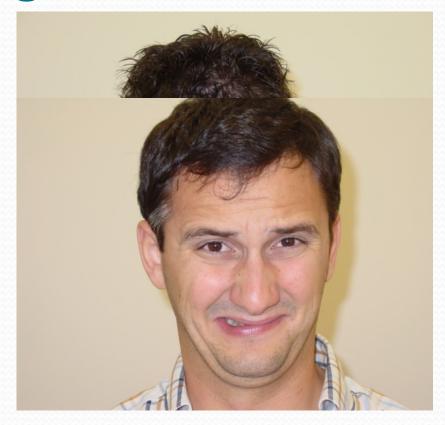
	Neut	Нарр	Sad	Surp	Ang	Fear	Disg
Neut	52.38	0	42.86	0	4.76	0	0
Нарр	0	90.48	4.76	0	0	4.76	0
Sad	4.76	4.76	76.19	0	4.76	4.76	4.76
Surp	0	0	0	76.19	0	23.81	0
Ang	4.76	0	9.52	0	33.33	23.81	28.57
Fear	0	9.52	4.76	14.29	4.76	66.67	0
Disg	0	23.81	4.76	0	33.33	4.76	33.33

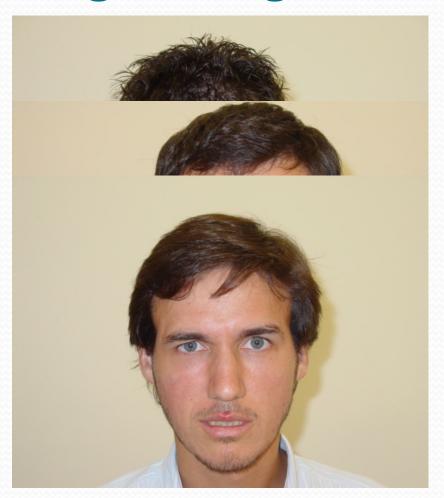
Confusion Matrix 99% Overal Recognition Rate = 61.2%

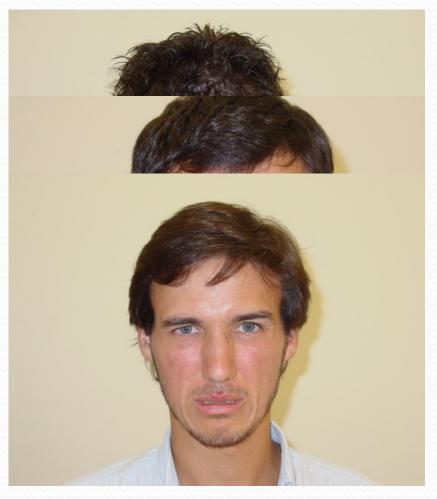




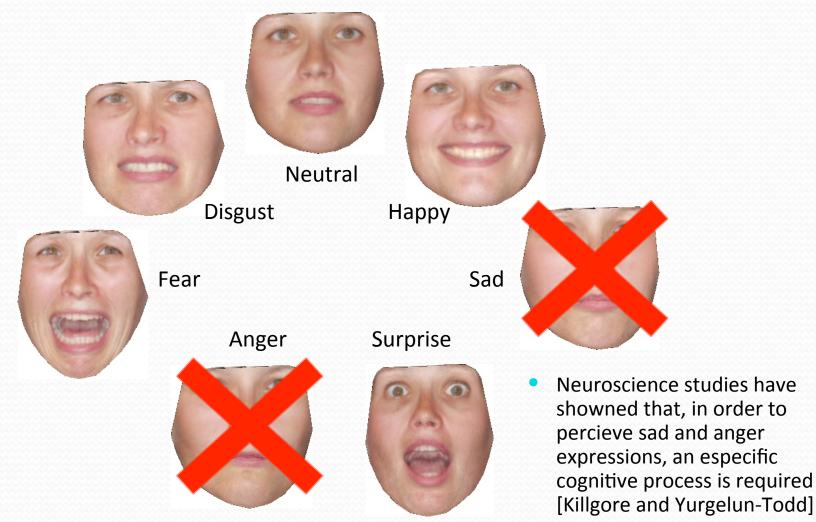








## Facial Expression Recognition



## **Experimental Results 5 Expressions**

	Neut	Нарр	Surp	Fear	Disg
Neut	76.19	0	0	23.8	0
Нарр	0	95.23	0	4.76	0
Surp	0	0	61.9	38.09	0
Fear	33.33	4.76	14.28	42.85	4.76
Disg	0	9.52	0	0	90.47

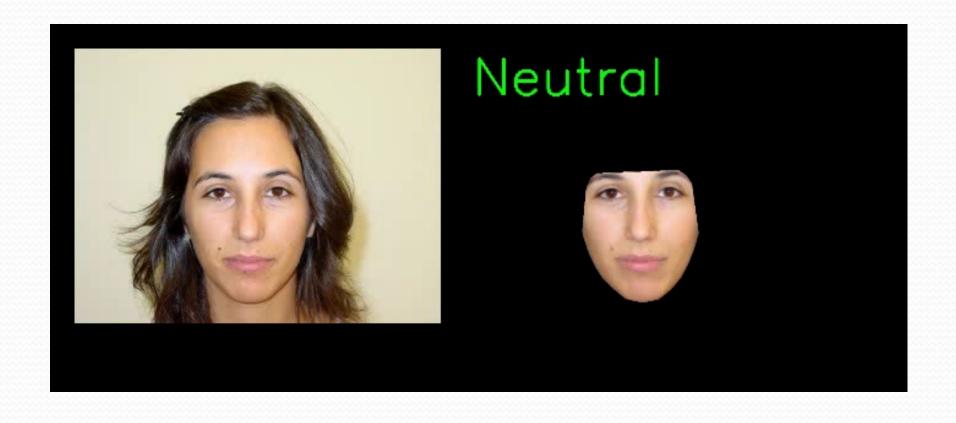
	Neut	Нарр	Surp	Fear	Disg
Neut	95.23	0	0	4.76	0
Нарр	0	95.23	0	0	4.76
Surp	9.52	0	76.19	14.28	0
Fear	19.04	4.76	19.04	52.38	4.76
Disg	0	19.04	4.76	4.76	71.42

- Confusion Matrix 97% Overal Recognition Rate = 73.3%
- Confusion Matrix 98% Overal Recognition Rate = 78.09%

	Neut	Нарр	Surp	Fear	Disg
Neut	85.71	4.76	4.76	4.76	0
Нарр	9.52	76.19	0	4.76	9.52
Surp	0	0	71.42	28.57	0
Fear	4.76	9.52	33.33	47.61	4.76
Disg	9.52	14.28	4.76	0	71.42

Confusion Matrix 99% Overal Recognition Rate = 70.47%

## 5 Expressions Classification Video



#### **Final Notes**

- Standart AAM to describe faces in a compact way
- LDA
  - Discrimination quality given by k-means
- Classification by mahalanobis distance
  - 7 Expressions: Best recognition rate=61.2% (with 99% AAM variance)
  - 5 Expressions: Best recognition rate=78.4% (with 98% AAM variance)
- Future work:
  - Classify expression in a video sequence using HMM